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AN INVESTIGATION OF THE  
CONSOLIDATION OF SOILS UNDER  
CONDITIONS OF TIME-DEPENDENT  
LOADING AND VARYING PERMEABILITY

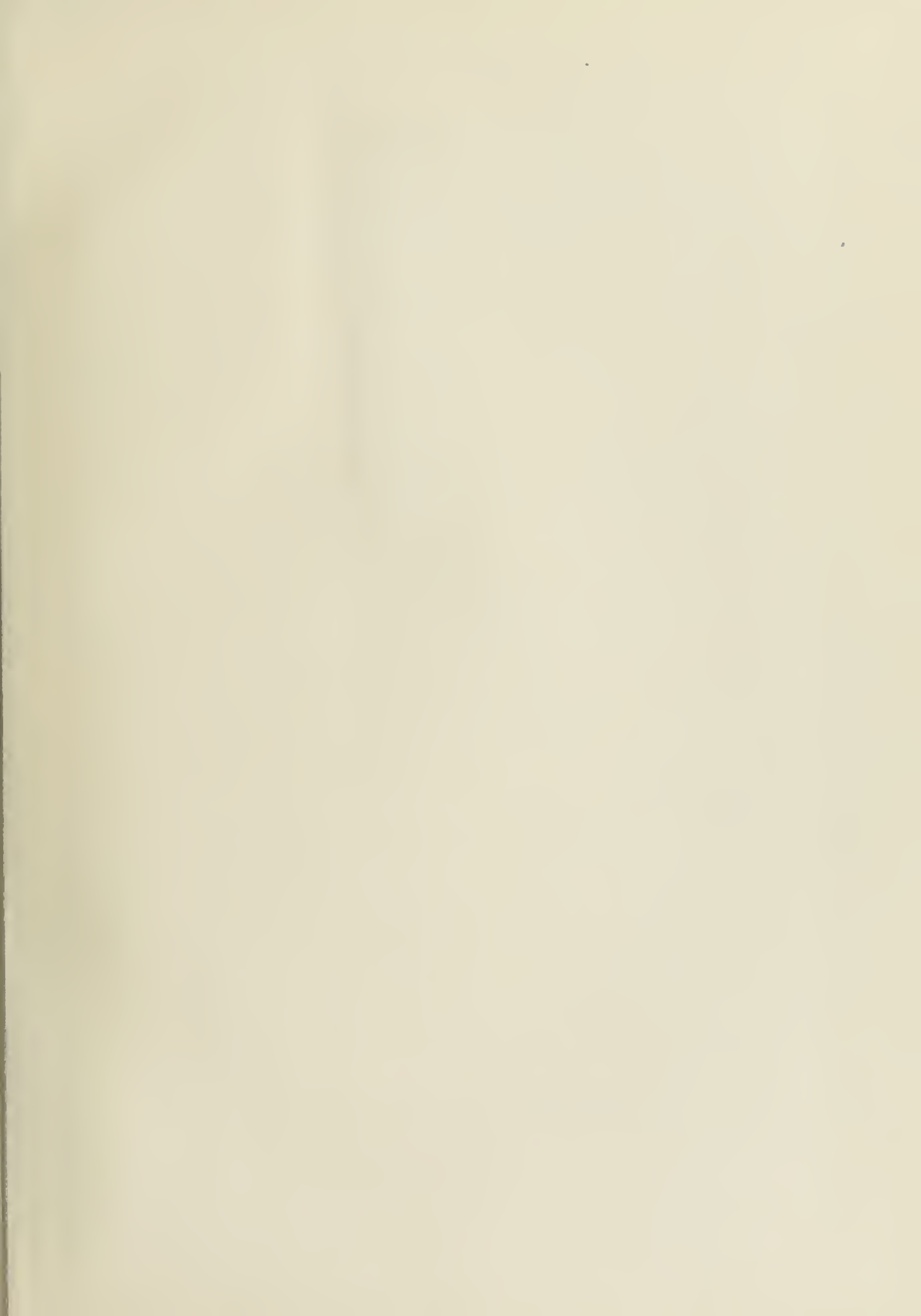
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AN INVESTIGATION OF THE  
CONSOLIDATION OF SOILS UNDER CONDITIONS OF  
TIME-DEPENDENT LOADING  
AND  
VARYING PERMEABILITY

by

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Civil Engineer Corps. United States Navy

A Thesis Submitted to the Faculty  
of the Department of Civil Engineering  
in Partial Fulfillment of the  
Requirements for the Degree of  
Master of Civil Engineering

Approved:

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Advisor

Rensselaer Polytechnic Institute

Troy, New York

June, 1958



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## FORWORD

The author wishes to express his sincere appreciation to Assistant Professor Robert L. Schiffman, for his assistance in selection of the topic, and his guidance and constructive advice in setting up and conducting the experimental phases of the research conducted. His timely suggestions and explanations of research objectives and requirements have been of inestimable value in this work.

In addition, the author wishes to acknowledge with gratitude, the innumerable helpful hints and practical suggestions offered by Associate Professor Stanley V. Best, without whose excellent class-room instruction the understanding of the subject matter would have been many times more difficult.



## ABSTRACT

The Terzaghi Theory of Consolidation does not consider the time-dependent loading conditions, encountered in ordinary construction practice, except in a graphical approximation. The development of a rigorous mathematical solution to this problem by Schiffman requires simplifying assumptions relative to the permeability and consolidation characteristics of the soil in order that the general differential equation for consolidation under such loading may be linearized.

The investigation of the validity of these assumptions for the case of one-dimensional flow was conducted, utilizing both standard lever-arm and bellows type consolidation equipment. The assembly and use of a constant-head permeameter to measure flow volume through a consolidating soil mass provided, for the first time, an opportunity to correlate instantaneous and average values of the coefficient of permeability, with the porosity existant at the time of reading. The wide variance in instantaneous values dictated the use of finite incremental average values. By limiting the time increment to 15 minutes, it was found that analysis of data was considerably improved.

Four consolidation tests were conducted, using instantaneous standard incremental loading, time-dependent loading and small incremental loading. A proposed fifth test



using small incremental loading was cancelled due to failure of a metal casting in the equipment under 16TSF loading. A pure Kaolin clay was tested in order to limit the number of variables entering into the problem. It was considered that the use of undisturbed natural soil samples would introduce intangible factors which would seriously interfere with the objectives of this pilot study.

Analysis of test data shows that, for construction-type (i.e. time-dependent loading), the assumption of linear variation of permeability with porosity, utilized by Schiffman in his solution of the general differential equation of consolidation, is valid, but only for small load increments. The linearity of this relationship does not appear to hold under conditions of large absolute loads applied over a short time period. It is hypothesized that the apparent exponential relationship is the result of the shearing of adsorbed water from the clay particle during an intense structural densification under such loading. Further study of this problem was strongly recommended.

The approximation technique utilized by Schiffman, in the solution of the variable permeability case, was found to be limited in accuracy only by the time-increment used by the investigator. A wide variance in average values of the coefficient of permeability was found to exist under all conditions of loading, which factor requires almost constant



attendance if the average value is to approach the instantaneous value.

No conclusion was drawn relative to the consolidation-permeability-time relationship under time dependent loading, since fitting procedures for the test curves were not established during this investigation.





## PART 1.

### INTRODUCTION

#### A. Objective

The furnishing of a reasonably accurate engineering estimate of the settlement to be encountered in the founding of man's structures on soil strata which have been subjected to the vagaries and assaults of natural forces for millenia of time, has been one of the most important contributions of the field of soil mechanics to the Engineering Profession. The complexity of the solution to this problem cannot be overstated, since both interdependent and non-dependent, linear and non-linear, variables are encountered throughout any analysis of the settlement characteristics of Engineering Soils.

It is the current practice of Soil Mechanics and Foundation Engineers to compute total settlement and the time-rate of settlement of loaded compressible strata in accordance with the mathematical analysis developed by Dr. Karl Terzaghi in his theory of consolidation. Although rigidly correct for the assumptions used by Dr. Terzaghi, the use of the Terzaghi theory does not always render satisfactory results, since the simplifying assumptions of the theory cannot usually be found in the field. Among the assumptions used by Dr. Terzaghi is the concept that loads are applied to the soil instantaneously without changing its



permeability characteristics. Although several others of the basic assumptions of the theory of consolidation are subject to critical revue, an extension to the Terzaghi theory as developed by Assistant Professor R.L. Schiffman of the Civil Engineering Department, Rensselaer Polytechnic Institute, proposes a solution to the settlement problem which considers the loading to be time-dependent and the permeability to be variable. Since this analysis closely approximates field conditions, it is considered that a more accurate appraisal of the action of soils under loading may be gained by its use, vice the original Terzaghi theory.

With certain simplifying assumptions, the Schiffman concepts can be used to predict the total settlement and the time-rate of settlement of compressible strata under time-dependent loading, within the limits of mathematical accuracy and the validity of the simplifying assumptions. The validity of these assumptions is the standard against which the application of Professor Schiffman's solution must be measured, if the solution is to be considered a useful contribution to the practice of Civil Engineering.

It is the specific objective of this thesis to conduct a series of tests designed to investigate the time effects of continuously varying loading on the consolidation of soils and the variation of soil permeability with pore



pressures induced by such loading.

The general objective of these investigations is to contribute to a more thorough and basic understanding of the action of compressible soils under loading, with commensurately improving accuracy in the prediction of settlements.





## I

B. Historical Review

The accurate prediction of the settlement characteristics of compressible soil strata under loading has been a major topic for research and discussion for several decades. The statement of Collingwood (1) in 1891 that sound undisturbed earth "should be penetrated to a sufficient depth to insure that it is not underlain by semi-fluid or compressible material, which may in time yield and cause trouble and danger..." while qualitative in nature, nevertheless indicates an awareness by practicing Civil Engineers of that era, of the basic cause of the settlement phenomenon.

Although the scientific approach to the understanding of soil action had been in the process of development by such pioneers as Wollny 1879-98 (2), Schlichter 1897 (3), King 1899 (4), et al it is to be noted that their work, while contributory to the broad base of fundamental soil knowledge, was primarily directed toward the agricultural uses of soils. Thus the use of engineering judgement and experience, and empirically derived formulac remained the tools of the Foundation Engineer until well into the second decade of the present century.

With the publication in 1925 of his "Theory of Consolidation", Dr. Karl Terzaghi (5) provided a major



contribution to the scientific evaluation of one of the Foundation Engineers most perplexing problems - the prediction of settlements to be expected after loading a compressible soil. Using fundamental physical laws and simplifying assumptions, Dr. Terzaghi developed a mathematical treatment of the complex functional inter-relationships of various soil properties which by thermodynamic analogue yielded a differential equation solvable by use of Fourier Series. His theory, based in part on instantaneously applied loading and constant permeability, for the first time provided a quantitative, albeit not completely accurate, measure of the consolidation of compressible soil strata under loading. By his solution of the Consolidation problem Dr. Terzaghi, in the words of Professor F.P.Tschebotarioff, "became the founder of the new science of soil mechanics" (6). In 1941 Professor E.J. Kilkawley (7) brought together the fundamental concepts underlying Dr. Terzaghi's work, and presented a solution of the differential equation under conditions of loading and drainage encountered in the field.

It is obvious that the assumption of instantaneously applied loading, while achievable in the laboratory, cannot be duplicated in the erection of a structure. In an effort to account for this incongruity in computing time-rates and total settlement, Dr. Terzaghi advanced an approximate graphical method which after



extensions by Professor Gilbuay and Professor Taylor (8) has been accepted as the closest available approach to field loading conditions. The recent work of Professor Schiffman (9) in developing a rigorous mathematical analysis of the consolidation process, as it is affected by the time-rate of loading, permits an analytical evaluation of the settlement to be encountered without recourse to graphical approximations. It is the purpose of this thesis to investigate the validity of Professor Schiffman's assumptions in extending Dr. Terzashi's work.



## PART 11.

### THEORY

#### A. The Consolidation Process

The compression of soils under externally applied loads, either natural or man-made, is the basic cause of settlement of structures. This compression is intimately associated with the pore spaces, (ie. intergranular voids) of the soil structure, and the escape of ground water, therefrom. Since both water and the soil grains are considered incompressible, the only way that the height of a soil mass can be reduced, in the vertical plane, is by the escape of the pore water from the soil structure with a concurrent, densifying, structural rearrangement of the soil grains. Thus it is seen that the rate of compression of a soil is a function of the rate of escape of pore water.

With the application of load to a saturated pervious soil mass such as clean sand, the escape of pore water is almost instantaneous, since the perviousness of the soil places no obstacle to free passage of water. On the other hand, if the loaded soil is a saturated clay, the escape of the pore water requires considerable time for completion. At the instant after load application, before any pore water has escaped, the soil structure cannot support any of the applied load, since it is in equilibrium, and any change in this condition requires rearrangement (ie. compression). It follows





that the load is supported, temporarily by the pore water, which must incur an increase in pressure to perform this task. This increase in pore water pressure is termed "hydrostatic excess pressure". Under conditions of boundary drainage, the hydrostatic excess pressure is subsequently relieved by the escape of pore water. This pressure relief by boundary drainage, requires transfer of stress from the escaping pore-water to the grains of the soil structure, which reacts to the induced forces of loading by a reduction in volume equivalent to the volume of escaping pore water, thus permitting additional intergranular contact to absorb the transferred stresses. In this manner, the stresses due to loading slowly pass from hydrostatic excess pressures to intergranular or effective pressures, with full stress assumption by the soil structure, upon complete dissipation of the hydrostatic excess. This adjustment process whether it be relatively fast, as in sands, or very slow, as in impervious clays, is termed "consolidation". In its simplest form the consolidation process is reducible at any instant of time to the equation:

$$p = u + \bar{\sigma}$$

where  $p$  is the compressive stress due to the applied load  
 $u$  is the hydrostatic excess pressure  
 $\bar{\sigma}$  is the effective pressure

For the limiting conditions of (1) no dissipation of hydrostatic excess and (2) complete dissipation of hydrostatic



excess, the equation reduces to

$$(1) \quad \underline{p = u}$$

$$(2) \quad \underline{p = \bar{u}}$$



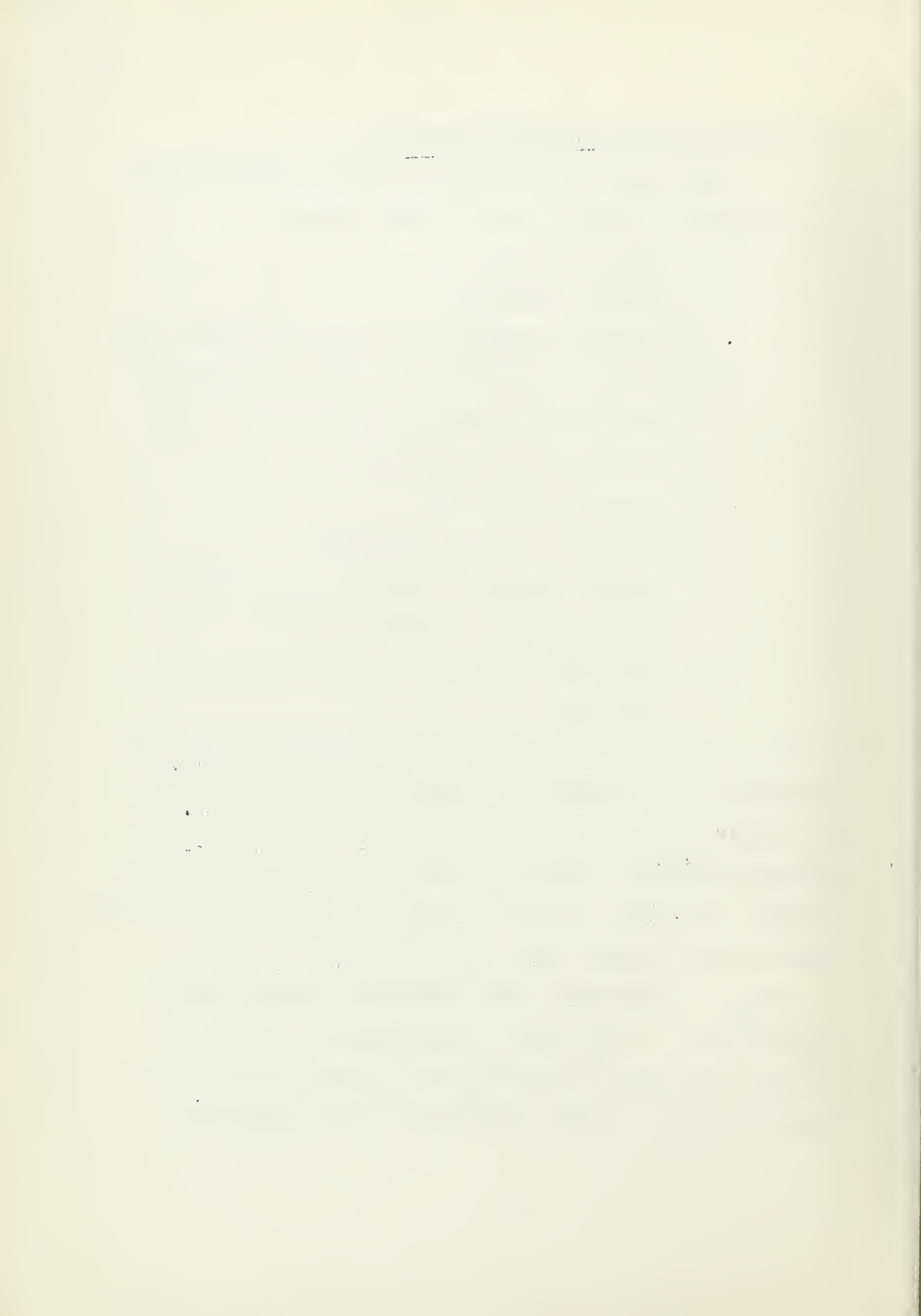
## B. The Terzaghi Theory of Consolidation

The analysis of the consolidation process developed by Terzaghi is based on the following assumptions:

1. Homogeneous soil mass
2. Complete saturation
3. Negligible compression of soil grains and water
4. Action of infinitesimal masses no different from that of larger, representative masses
5. One-dimensional compression
6. One-dimensional flow
7. Darcy's Law is strictly valid
8. Constant values for certain soil properties which actually vary with pressure
9. Void ratio varies linearly with applied pressures

With the exception of the ninth listed assumption only minor inaccuracies are considered to stem from these assumptions. The linear relationship between void-ratio and pressure introduces serious discrepancies which limit the validity of the solution. However, the solution would be well-nigh impossibly complex under any other type of functional variance.

Figure 1 illustrates the consolidation process under consideration. A clay layer of thickness  $2H$ , between two pervious sand layers is stressed by an applied unit load  $p$ . Boundary Drainage permits dissipation of the hydrostatic









excess pressures induced in the pore water. As dissipation progresses the effective pressure  $\bar{\sigma}$  increases from 0 at time  $t_0$  to  $\bar{\sigma}_p$  at time  $t_p$ , when the process is completed. At intermediate times  $t_1, t_2$ ...etc. the consolidation process is shown to be more advanced toward the surface and less advanced at the center of the stratum. Consider, now, a differential prism of soil from the upper half of the clay layer, with cross sectional area of 1 and height  $dz$  as shown in Figure 2. The piezometer tubes are considered to accurately measure pore-water pressure at top and bottom boundaries. Since pore water is escaping through the upper boundary, a drop in head is occurring in the direction of flow. This drop in head,  $dh$  is related to the dissipation of hydrostatic excess  $du$  by

$$dh = \frac{du}{\gamma_w} \quad \gamma_w = \text{unit wt of water}$$

the hydraulic gradient,  $i$ , is defined as the drop of head over a given distance.

$$i = - \frac{dh}{dz}$$

By substitution

$$i = - \frac{du}{\gamma_w dz}$$

Darcy's Law for flow of water through soil masses states that the rate of flow is proportional to the hydraulic gradient

$$v = ki \quad k = \text{coefficient of permeability}$$

$$v = \text{flow velocity}$$



Again by substitution

$$v = \frac{k}{\gamma_w} \frac{du}{dz}$$

By differentiation, the change in flow velocity over distance  $dz$  during a given time interval  $dt$  equals

$$\frac{\partial v}{\partial z} = - \frac{k}{\gamma_w} \frac{\partial^2 u}{\partial z^2}$$

Since Darcy's Law can also be stated in the form:

$$V = \frac{Q}{At}$$

where  $Q$  = discharge

$A$  = Cross Sectional Area

$t$  = time

it follows that, in time interval  $dt$  with  $A = 1$ ,  $V = Q$  (i.e.: that the flow velocity represents the amount of water entering the base of the prism sketched in figure 2) then, the increment of velocity gained over the height of the prism,  $dz$ , must equal the increase in discharge through the top of the prism, i.e.  
 $dv = dQ$

Any increase in discharge from a fully saturated soil must result in a decrease in pore volume. This Porsity change  $\Delta n$  can be expressed as:

$$\Delta n = \frac{\Delta e}{1+e}$$

where  $e$  = void ratio

and since the coefficient of compressibility  $a_v = \frac{\Delta e}{\Delta P}$

$$\Delta n = \frac{a_v \Delta P}{1+e}$$



When the change in pore volume  $\Delta n$  is completed, the pressure,  $p$ , equals the effective pressure carried by the soil grains,  $\bar{\sigma}$ , and the preceding equation can be expressed as

$$\frac{\partial n}{\partial t} = - \frac{\partial \bar{\sigma}}{\partial t} \frac{a_v}{1+e}$$

Any increase in  $\bar{\sigma}$  under constant unit load  $P$  during time interval  $dt$  must equal the decrease in Hydrostatic Excess Pressure,  $U$ , during the same time period.

$$\therefore \frac{\partial u}{\partial t} = - \frac{\partial \bar{\sigma}}{\partial t} \quad \frac{\partial n}{\partial t} = \frac{\partial u}{\partial t} \frac{a_v}{1+e}$$

now since

$$\frac{\partial v}{\partial z} = - \frac{k}{\gamma_w} \frac{\partial^2 u}{\partial z^2} \quad \frac{\partial v}{\partial z} = - \frac{\partial n}{\partial t}$$

and

$$\frac{\partial n}{\partial t} = \frac{\partial u}{\partial t} \frac{a_v}{1+e}$$

it follows that:

$$\frac{\partial u}{\partial t} \frac{a_v}{1+e} = \frac{k \partial^2 u}{\gamma_w \partial z^2}$$

$$\text{or } \frac{\partial u}{\partial t} = C_v \frac{\partial^2 u}{\partial z^2} \quad \text{The fundamental differential equation of consolidation}$$

$$\text{where } C_v = \frac{k(1+e)}{a_v \gamma_w} = \text{Coefficient of Consolidation}$$

The solution of the fundamental differential equation by Fourier Series, for the boundary conditions as shown in



Figure 1, is as follows

$$U = p \frac{4}{\pi} \sum_{n=0}^{\infty} \frac{1}{2n+1} \left[ \sin \frac{(2n+1)\pi z}{2H} \right] e^{-\frac{(2n+1)^2 \pi^2 T}{4}}$$

Where a dimensionless Time factor

$$T = \frac{t}{H}$$

With  $C_v$  = Coefficient of Consolidation

$t$  = time for Hydrostatic Excess to decrease to  $U$

$H$  = Longest Drainage path for water flow

By plotting values of  $U$  for various values of  $\frac{z}{H}$  and  $T$ , the family of curves shown in Figure 3 eliminates the tedious solution of the consolidation equation and permits the use of Figure 4 as a practical method of arriving at a prediction of settlement under loading. Since the ultimate settlement

$$\rho_v = \frac{\sum H}{1+e} \alpha_v \Delta P$$

then the settlement at any time interval equals

$$\rho = \frac{U_{avg}}{U_i} \rho_v$$

Where  $U_{avg}$  = Average Hydrostatic Excess

$U_i$  = Initial Hydrostatic Excess

However, among the factors ignored by the Terzaghi solution is the gradual, rather than instantaneously, applied loading encountered in the construction process. A graphical approximation, based on the premise that, at the end of construction, the settlement is the same as that which would have resulted in half the time, if the entire load had been





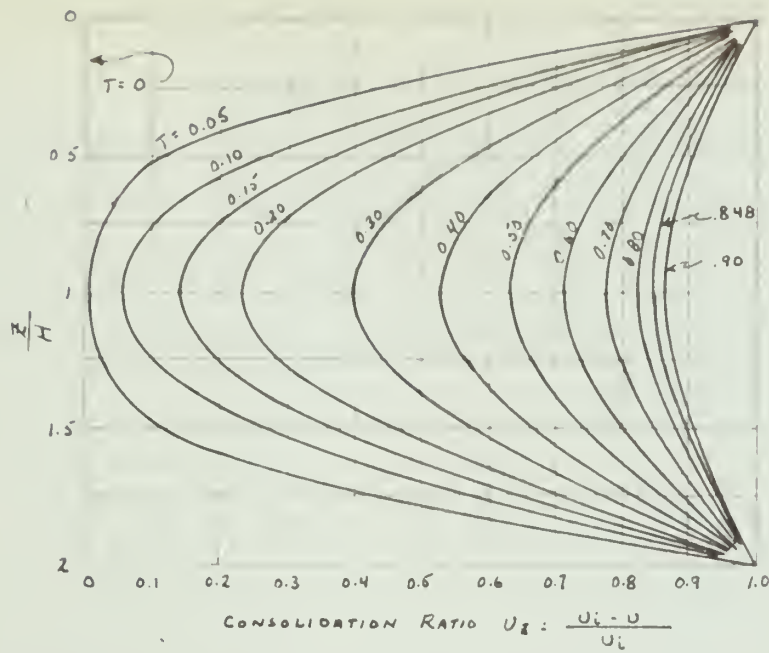


FIG 3 - CONSOLIDATION AS A FUNCTION OF DEPTH AND TIME FACTOR

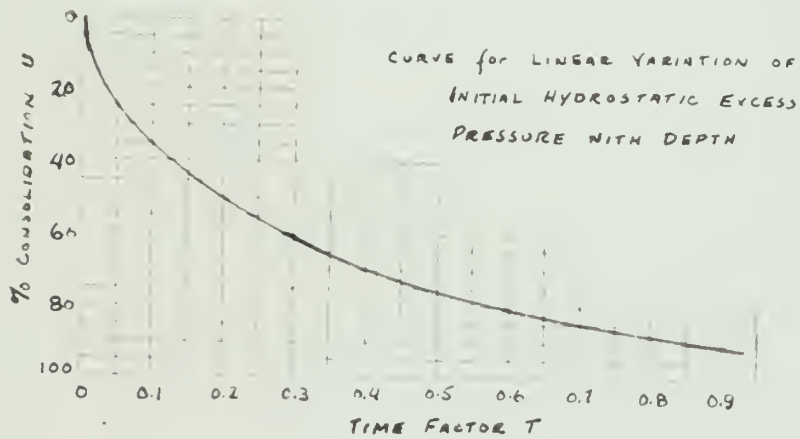


FIG 4 - CONSOLIDATION CURVE - ACCORDING TO THE TERZAGHI THEORY



applied throughout, was first proposed by Terzaghi and Gilboy. Taylor extended it to provide for predicting settlements during the loading period, by assuming that at any specified percentage of the loading period, the load acting equals this percentage of the total load; and at this time, the settlement equals the settlement at one-half the time in question from the curve of time vs. settlement for instantaneous loading. Figure 5 illustrates this correction.

The solution of the fundamental differential equation which by tabulation gives the curves of Figures 3 and 4, was based upon homogeneous boundary conditions, i.e., pressures at the top and bottom of the sample are equal. The use of a constant head permeameter imposes different boundary conditions than these, in that the applied load is resisted by the constant pressure-head of the Permeameter. The following solution to this problem has been developed by Professor Schiffman and graphical values for the loads applied are presented as Figures 6, 7a and 7b:

$$\frac{\bar{u}}{u_o} = \frac{u_i}{2u_o} \left[ 1 - \frac{\bar{\bar{u}}}{u_o} \right] - \frac{\bar{\bar{u}}}{u_o}$$

where  $\frac{\bar{u}}{u_o} = 1 - \% \text{ Consolidation}$

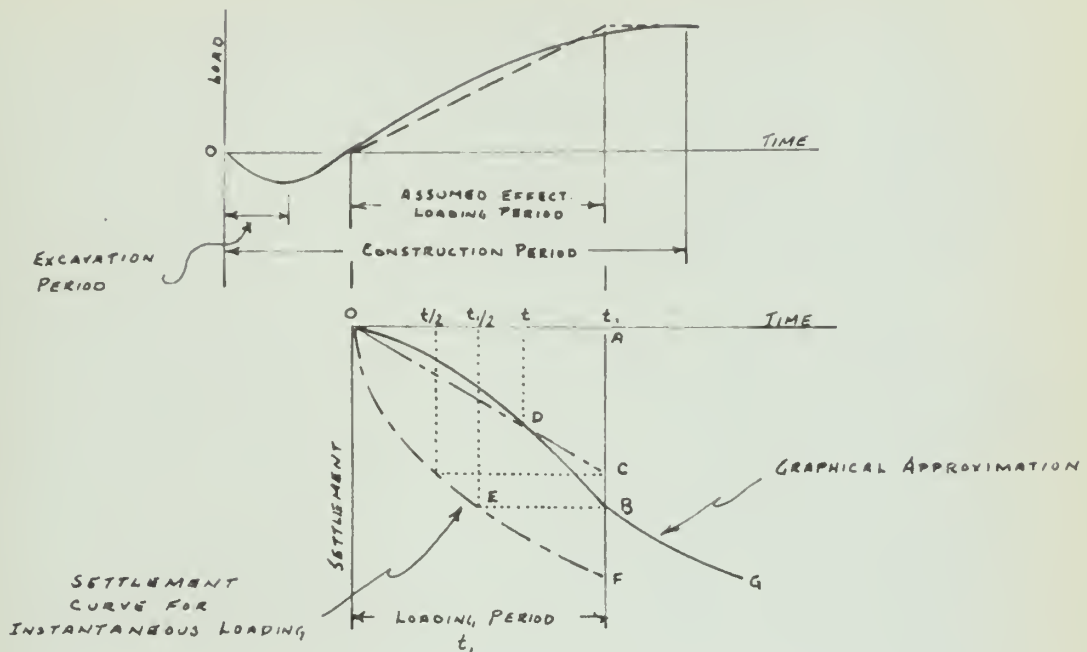
$u_i$  = Pressure due to Permeameter Head

$u_o$  = Pressure due to applied load increment

$\bar{u}$  = Average Hydrostatic Excess Pressure

$\frac{\bar{\bar{u}}}{u_o} = \% \text{ Consolidation with Homogeneous Boundary Pressures}$





#### PROCEDURE

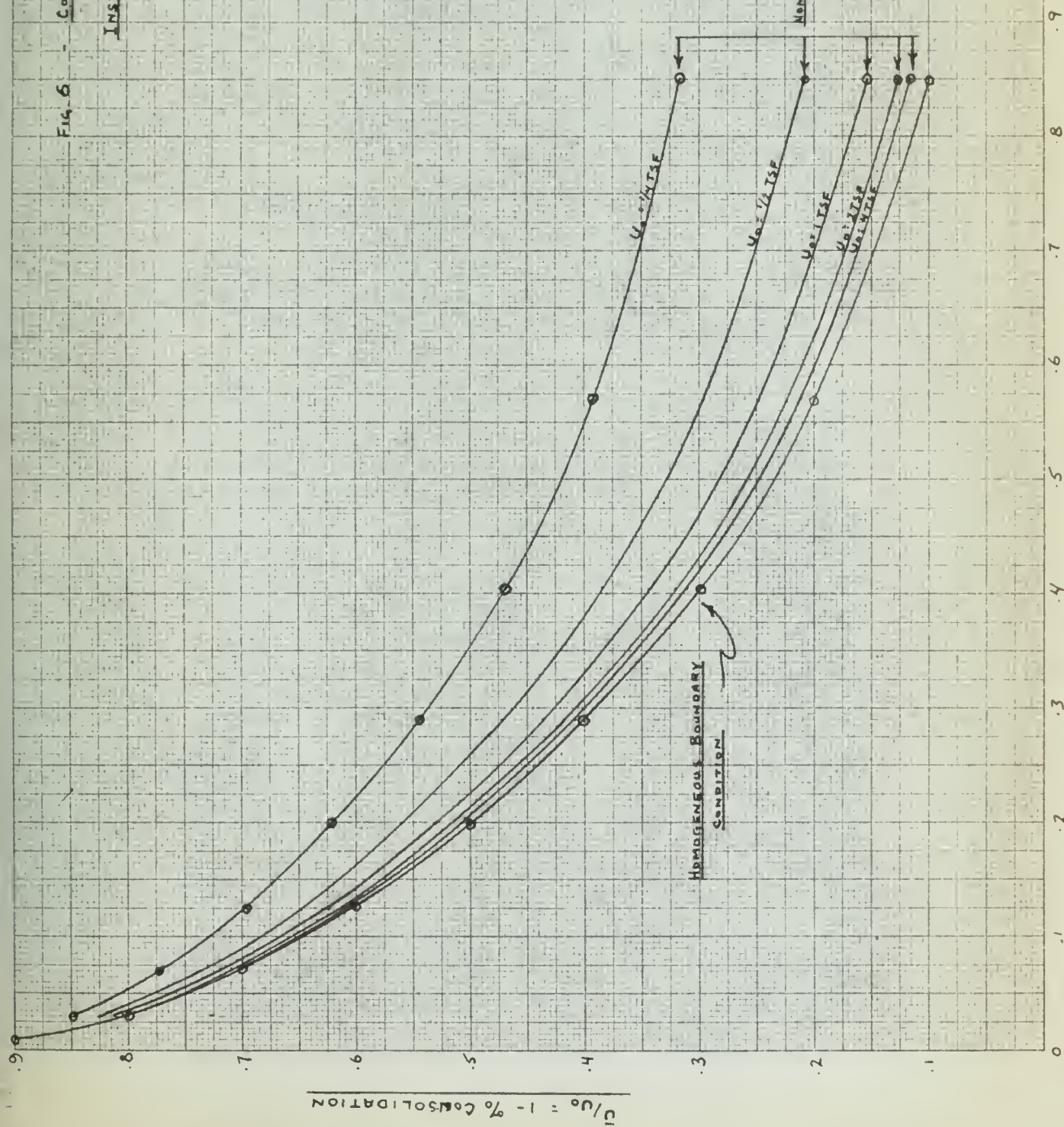
1. SETTLEMENT AT TIME  $t_1$  = SETTLEMENT AT TIME  $t_1/2$  ON INSTANTANEOUS CURVE (I.E. SETTLEMENT = AB)
2. LOAD ACTING AT TIME  $t = t/t_1 \times \text{TOTAL LOAD}$
3. MULTIPLY SETTLEMENT AC FOR TIME  $t$  BY  $t/t_1$  TO FIND SETTLEMENT VALUE FOR APPROXIMATION TO ACTUAL SETTLEMENT
4. PERFORM 3. GRAPHICALLY AS FOLLOWS:
  - a. DIAGONAL OC INTERSECTS TIME  $t$  AT  $D = t/t_1 \times AC$
  - b. D = POINT ON APPROXIMATION CURVE
  - c. OBTAIN COMPLETE CURVE BY REPETITION FOR VARIOUS TIMES
5. BEYOND B, APPROXIMATION CURVE IS OFFSET HORIZONTALLY FROM THE INSTANTANEOUS CURVE BY  $1/2$  THE LOADING PERIOD (I.E.  $BE = GF$ )

FIG 5 - GRAPHICAL APPROXIMATION OF THE SETTLEMENT CURVE DURING THE CONSTRUCTION LOADING PERIOD (AFTER TAYLOR) (B)





FIG. 6 - CONSOLIDATION CURVES  
INSTANTANEOUS LOADING







$$\bar{U}/U_0 \text{ (corrected)} = (1 - 7\% \text{ Cons.})$$

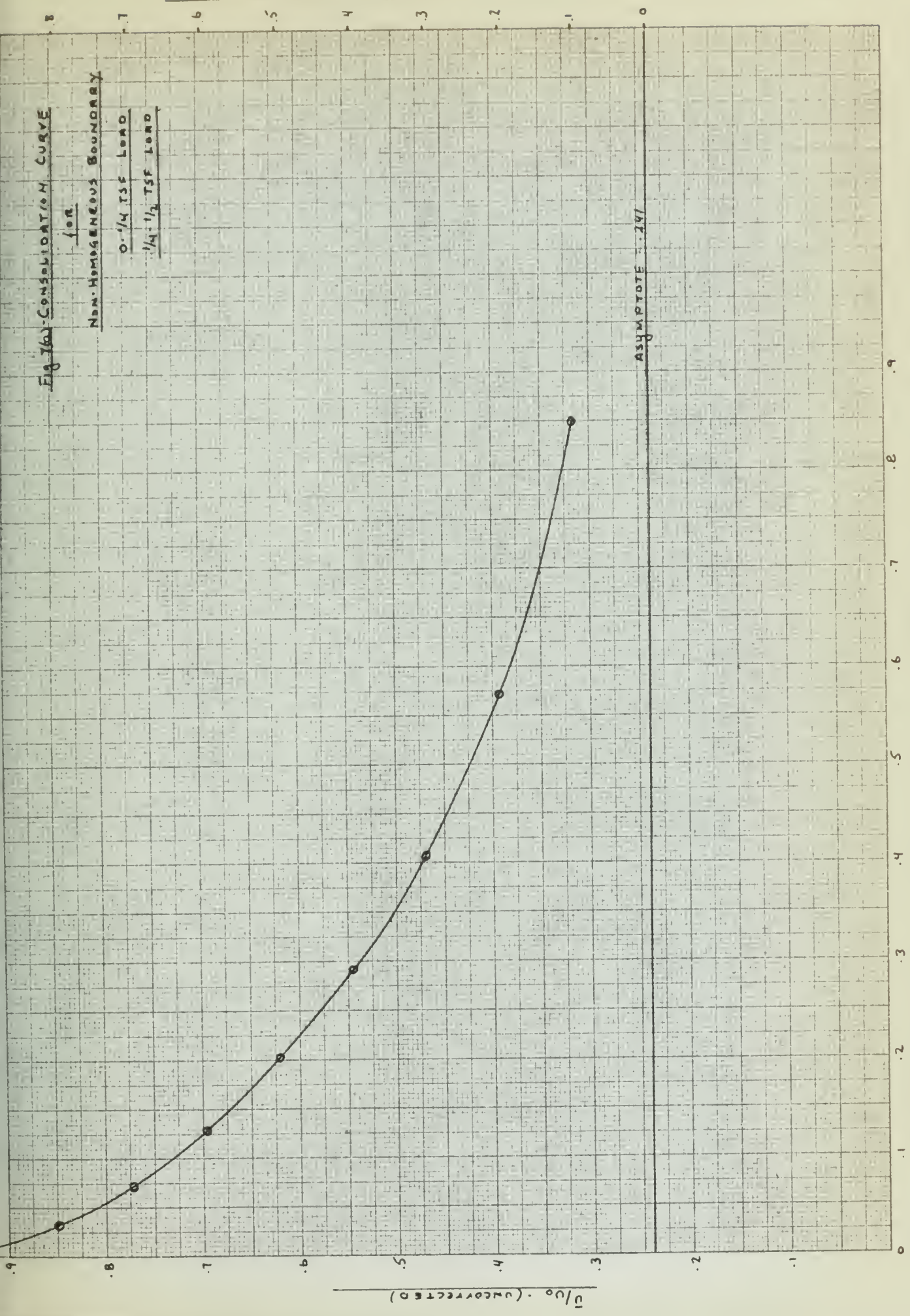
Fig 76a Consolidation Curve

for

Non-Homogeneous Boundary

$0 - 1/4$  TSF Load

$1/4 - 1/2$  TSF Load







$$\bar{u}/u_0 \text{ (corrected)} = (1 - \% \text{ Cons.})$$

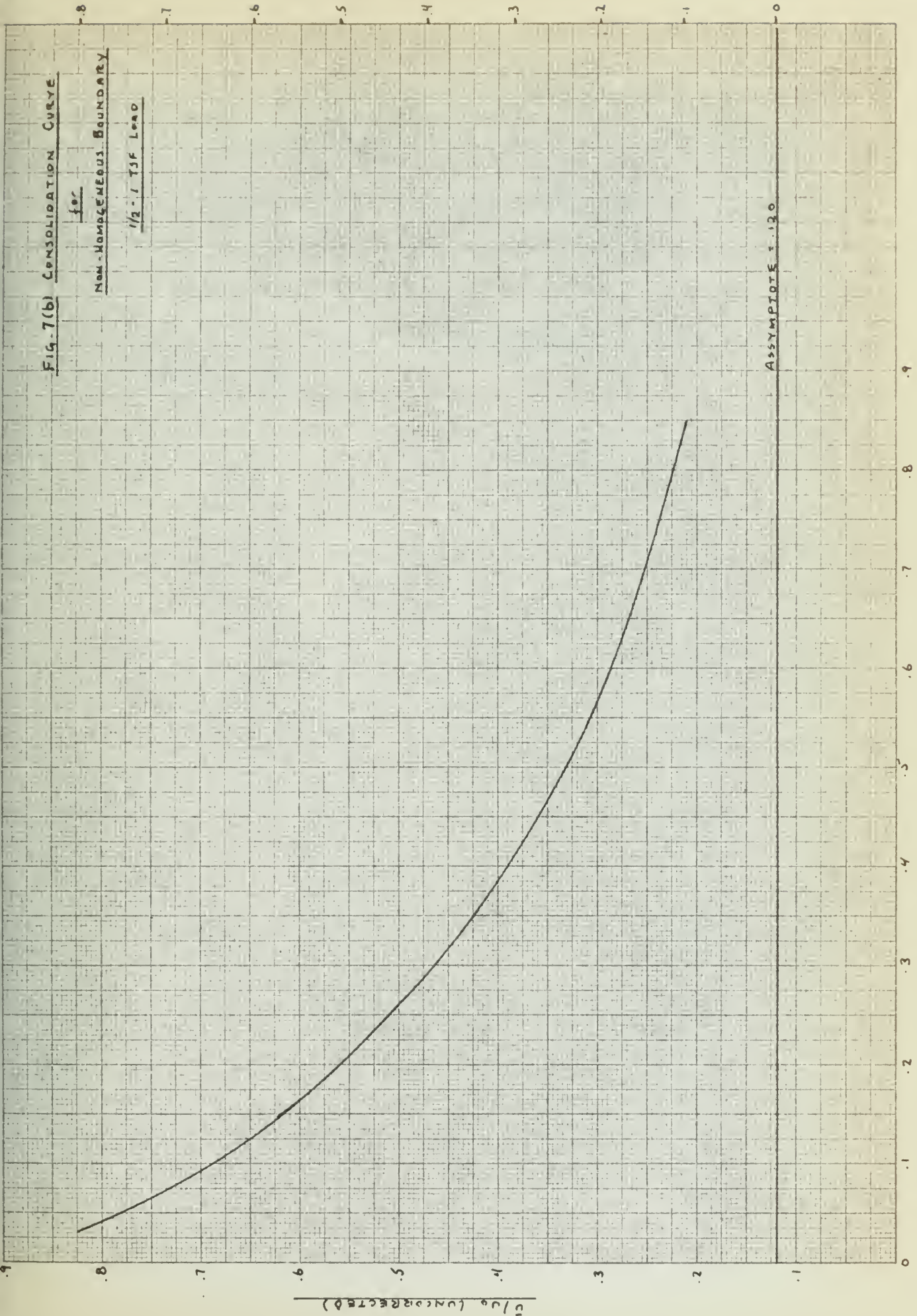
FIG-7(b) CONSOLIDATION CURVE

for

Non-Homogeneous Boundary

$1/2 - 1$  TSF Lead

Asymptote = .120





As may be noted from Figures 6, 7a and 7b the solution of the equation gives the same value for the Time Factor as that tabulated by Taylor (8). The basic assumptions of linear variation of hydrostatic excess pressure with depth thus reduces a seemingly involved problem to the use of tabulated values, instead of tedious computations for each variation in Permeameter head.



### C. Schiffman Extension to the Theory of Consolidation

Professor Schiffman's development of a three-dimensional anisotropic theory of consolidation ( 9 ) provides a working basis for the study herein conducted. His assumptions in developing this theory are:

- (1) Complete saturation of Soil Mass
- (2) Incompressible fluid
- (3) Incompressible soil solids of small particle size
- (4) Darcy's Law valid at any instant of time.
- (5) Change in volume is linear with imposed pressure
- (6) Change in volume is small compared to original volume

Consider a prism of soil of volume,  $V$ , and surface,  $S$ . In accordance with the law of conservation of mass, the fluid flow into the mass through the surface must equal the total volume change of the mass. In terms of vector functions the total instantaneous mass flow is equal to

$$-\int \vec{v} \cdot \vec{n} \, ds + \int Q \, dv$$

where  $-\int \vec{v} \cdot \vec{n} \, ds$  = flow into mass through surface  $S$

and  $\int Q \, dv$  = increase in volume due to  
internal flow generation at  
rate,  $Q$ , due to head





the volume change due to flow is equal to:

$$\frac{\partial v}{\partial t} = \frac{\partial v_v}{\partial t} + \frac{\partial v_s}{\partial t}$$

Equating, we arrive at:

$$\int_v \left[ \nabla \cdot (k \nabla h) + Q + \frac{\partial v_v}{\partial t} \right] dv = 0$$

Since the volume is arbitrarily established we can write

$$\nabla \cdot (k \nabla h) + Q + \partial v_v / \partial t = 0$$

Since only those strains due exclusively to volume change are herein considered (assumptions 5 and 6), only normal stresses need be treated. The Modulus of Volume Change,  $M$ , is defined by:

$$m = \frac{\partial v_v}{\partial \theta}$$

Where

$$\theta = \sigma_x + \sigma_y + \sigma_z$$

Since the total pressure or the Soil Mass is composed of the neutral pressure,  $u$ , and the effective mean stress  $\bar{\theta}$  we can write:

$$\theta = \bar{\theta} + u$$

Where  $u$  is the pore pressure defined by:

$$u = \gamma_w h$$

$h$  = head

Since the consolidation process involves the transfer of initially incurred stress from the water to the soil grains, we can write:

$$\partial \theta = \partial u$$



and that:

$$\partial v_v = -m \partial u$$

By substitution in the equation of mass conservation, we then arrive at the differential equation of consolidation for a variable permeability and time-dependent loading:

$$\nabla \cdot (k \nabla u) + Q \gamma_w = m \gamma_w \frac{\partial u}{\partial t}$$

the treatment of the two dependent variables,  $k$  and  $u$ , is based upon the work of Schmid (14), who proposes the relationship:

$$\bar{k} = \beta (n - n_0)$$

where

$\beta$  = Constant

$n$  = Porosity

$n_0$  = Ineffective Porosity

Using this relationship, we can extend it to say that a linear relationship also exists between  $k$  and  $u$ :

$$k = \alpha u + k_f$$

where

$k_f$  = Coefficient of Consolidation at the end  
of consolidation

$\alpha$  = Modulus of Permeability Variation

and

$$\alpha = v m$$

It is now feasible to establish a differential equation covering the general theory of consolidation under conditions of varying permeability and time dependent loading:



(a) In terms of excess pore pressure  $u$

$$\alpha(\nabla u)^2 + \nabla u \cdot \nabla k_f + \alpha u \nabla^2 u + k_f \nabla^2 u + \alpha \gamma_w = m \gamma_w \frac{\partial u}{\partial t}$$

(b) In terms of the permeability  $k$

$$\frac{1}{\alpha} (\nabla k)^2 - \frac{1}{\alpha} (\nabla k \cdot \nabla k_f) + \frac{1}{\alpha} k \nabla^2 k - \frac{1}{\alpha} k \nabla k_f + \alpha \gamma_w = \frac{m \gamma_w}{\alpha} \frac{\partial k}{\partial t}$$

(c) and

$$\begin{aligned} \nabla k_i \cdot \nabla u - \alpha (\nabla u_0 \cdot \nabla u) + \alpha (\nabla u)^2 + \alpha u \nabla^2 u + (k_0 + \alpha u_0) \nabla^2 u \\ + \alpha \gamma_w = m \gamma_w \frac{\partial u}{\partial t} \end{aligned}$$

The present study being limited to the consideration of one-dimensional consolidation, the general equation for such a case can be written:

$$\left( C_0 + \frac{\alpha u_0}{m \gamma_w} \right) \frac{\partial^2 u}{\partial z^2} - \frac{\alpha}{m \gamma_w} u \frac{\partial^2 u}{\partial z^2} - \frac{\alpha}{m \gamma_w} \left( \frac{\partial u}{\partial z} \right)^2 + R = \frac{\partial u}{\partial t}$$

where

$R$  = Rate of change of imposed excess pore pressure

$C$  = Coefficient of Consolidation at start of consolidation.

This equation can be written under the following conditions

- (1) Double Drainage
- (2) Infinite extent of soil mass horizontally
- (3) Finite thickness of soil mass
- (4) Uniform initial Coefficient of Permeability
- (5) Uniform initially imposed pore pressure



Professor Schiffman has presented several individual solutions involving the following problems:

- (1) Constant permeability and genoral time dependent loading
- (2) Constant permeability and linear loading
- (3) Constant Permeability and construction loading
- (4) Constant Permeability and harmonic loading
- (5) Variable permeability

His solutions to these problems are as follows:

- (1) Constant Permeability - time dependent loading

$$u(z,t) = \frac{1}{H} \sum_{n=1}^{\infty} \left[ \int_0^{2H} \sigma(z) \sin \frac{n\pi z}{2H} dz \right] e^{-\frac{cn^2\eta^2}{4H^2}t} \sin \frac{n\pi z}{2H} \\ + \frac{1}{H} \sum_{n=1}^{\infty} \sin \frac{n\pi z}{2H} \left\{ \int_0^t \left[ \int_0^{2H} R(z,\tau) \sin \frac{n\pi z}{2H} dz \right] e^{-\frac{cn^2\eta^2}{4H^2}(t-\tau)} d\tau \right\}$$

- (2) Constant Permeabilty - linear loading

$$u(z,t) = \frac{16u_0}{T_0\pi^3} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n^3} \sin \frac{n\pi}{2H} \left( 1 - e^{-\frac{n^2\eta^2}{4}T} \right)$$

Since the average pore pressure can be expressed as:

$$\bar{u}(\tau) = \frac{1}{2H} \int_0^{2H} u(z,t) dz$$

Then by substitution

$$\bar{u}(\tau) = \frac{32\bar{u}_0}{T_0\pi^4} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n^4} \left( 1 - e^{-\frac{n^2\eta^2}{4}T} \right)$$

Where  $T$  is a dimensionless Time Factor

$$T = \frac{c}{H^2} t$$

Figure 8a shows the curve developed from a computation based on this equation, from which all other computations for the linear case can be made.





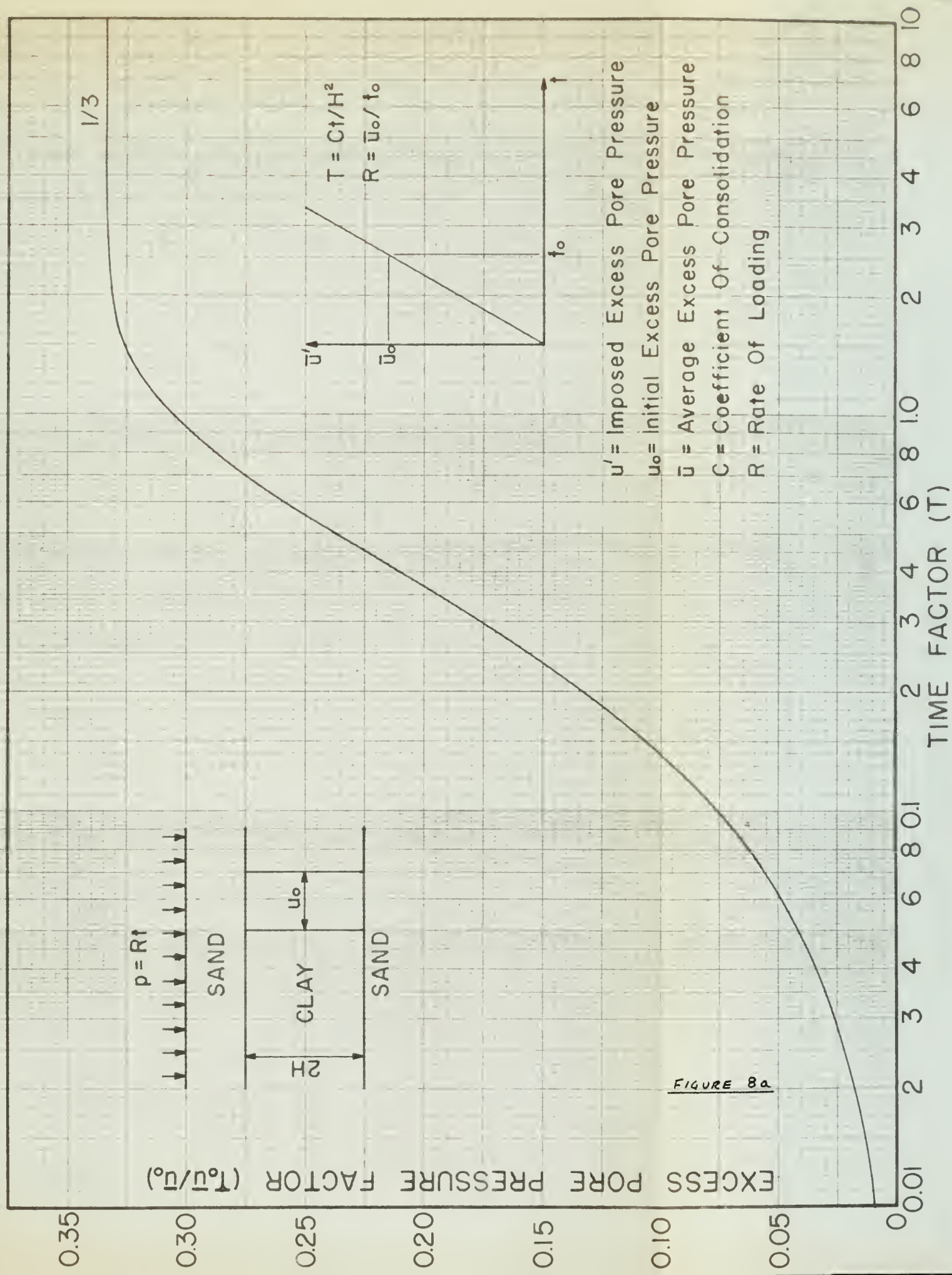


FIGURE 8a



Figure 8 (b) presents the computation involving the linear loading period ending at time  $t_0$  and the amount of excess pore pressure dissipated at that time. The percentage of settlement completed is equivalent to the amount of excess pore pressure dissipated and thus the settlement at the end of a linear type construction loading period can be computed.

As an example of the usefulness of Figure 8b, let us consider a structure founded on a clay stratum with  $C_v = 1.5 \frac{\text{cm}^2}{\text{min}}$ . If, then, the length of construction is related to the end time factor  $T_0$ :

$$t_0 = 172 T_0 \text{ days}$$

by entering Figure 8b, a table of percentage of settlement dissipated can be constructed, in terms of the length of construction. Table 1 shows this construction as developed by Professor Schiffman.

By use of such tables, the engineer can now make a rational decision as to the desired construction time period which will restrict post-construction settlements to satisfactory values, or as to selection of alternate solutions.

### (3) Constant Permeability-Construction Loading

With the results of the previous sections available, the pore pressure can now be analyzed at any instant and for any construction period. Figure 8c presents a typical load-time diagram for construction loading, wherein a load  $P_0$  is imposed at time  $t_0$ , the end of a linear construction period.





$u'$  = Imposed Excess Pore Pressure  
 $u_o$  = Initial Excess Pore Pressure  
 $\bar{u}$  = Average Excess Pore Pressure  
 $C$  = Coefficient Of Consolidation  
 $R$  = Rate Of Loading

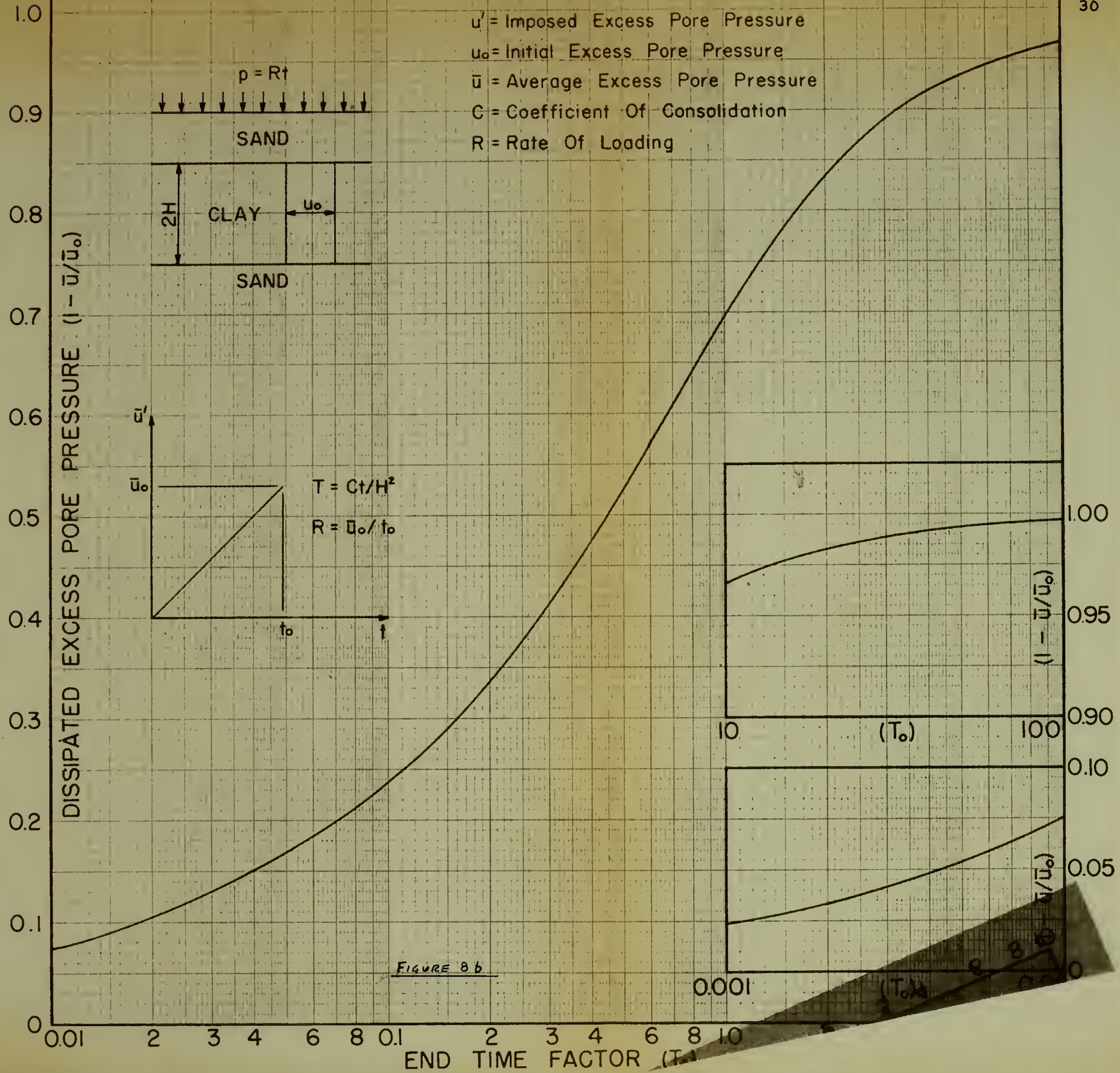


FIGURE 8b



TABLE 1

EXAMPLE OF SETTLEMENT DISSIPATED DURING A  
LINEAR CONSTRUCTION PERIOD

$H = 20 \text{ ft}$

$\dot{C} = 1.5 \text{ cm}^2/\text{min}$

% SETTLEMENT DISSIPATED	$T_0$	$t_0$
5	.00435	.75
10	.018	3
20	.071	12
30	.16	28
40	.28	49
50	.45	78
60	.68	117
70	1.03	177
80	1.65	284
90	6.20	559
95	6.70	1153





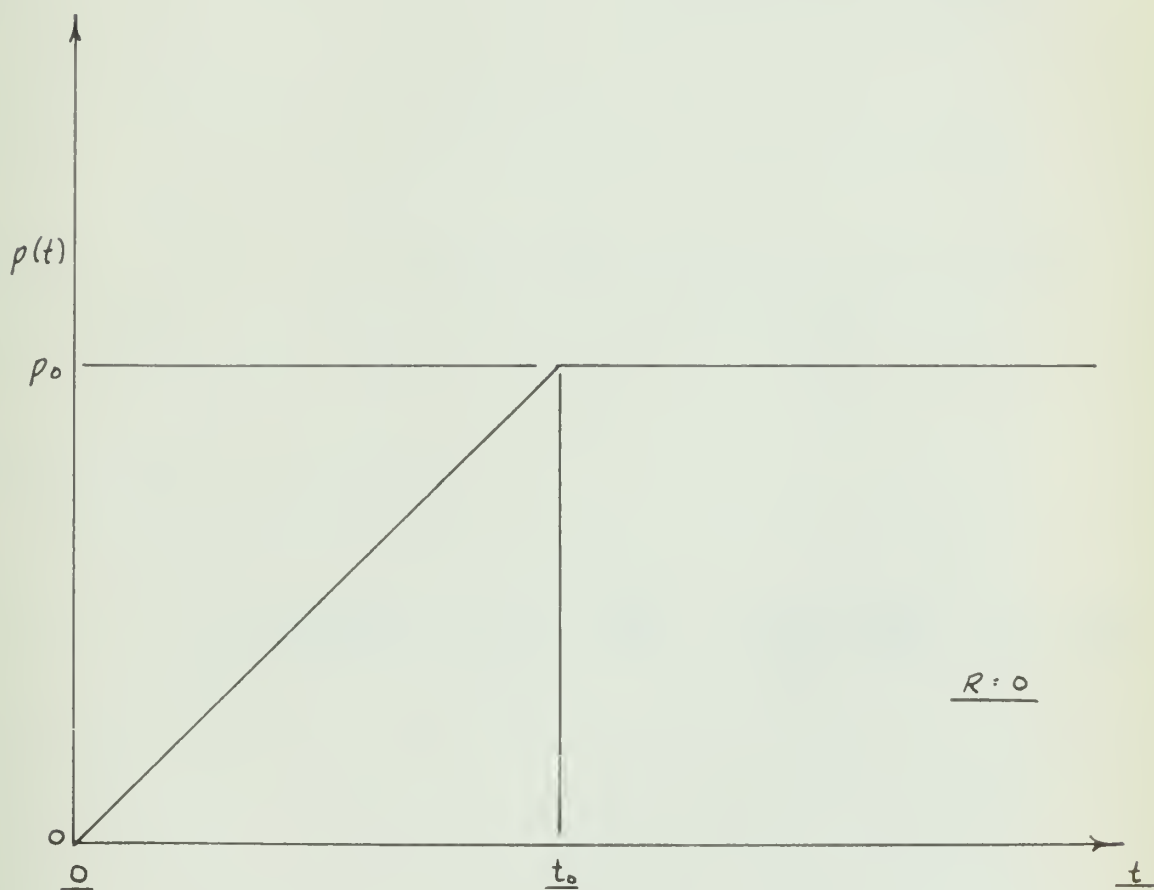


Fig. 8C      LOAD - TIME DIAGRAM FOR CONSTRUCTION LOADING



Treatment of this problem is as described in (2) above.

Figure 8d and 8e present the solution of the determination of average pore pressure during and after construction. These curves can be used to determine the theoretical consolidation curve in the following manner:

- (1) Estimate the construction time
- (2) Determine the Coefficient of Consolidation from Laboratory tests
- (3) Determine  $T_o$  from the Coefficient of Consolidation
- (4) Enter Figures 8d and 8e and select proper Consolidation Curve

#### (4) Variable Permeability

The basic equation governing this case is:

$$\left(c_v + \frac{\alpha u_o}{m \gamma_w}\right) \frac{\partial^2 u}{\partial z^2} - \frac{\alpha}{m \gamma_w} u \frac{\partial^2 u}{\partial z^2} - \frac{\alpha}{m \gamma_w} \left(\frac{\partial u}{\partial z}\right)^2 + R = \frac{\partial u}{\partial t}$$

However, the solution of this equation is hampered

by its non-linearity, for which general techniques of solution are unavailable. Solution by approximation techniques is therefore utilized, in lieu of numerical computation by analogue or digital computer methods.

The incremental time approximation is first considered. It is assumed the permeability remains constant over a finite time increment, but that the permeability varies from one increment to the next. For a finite number of time increments we have:

$$u(z, t') = \frac{4u_o}{\pi} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n} \sin \frac{n\pi}{2H} z e^{-\frac{n^2 \pi^2}{4} t'}$$





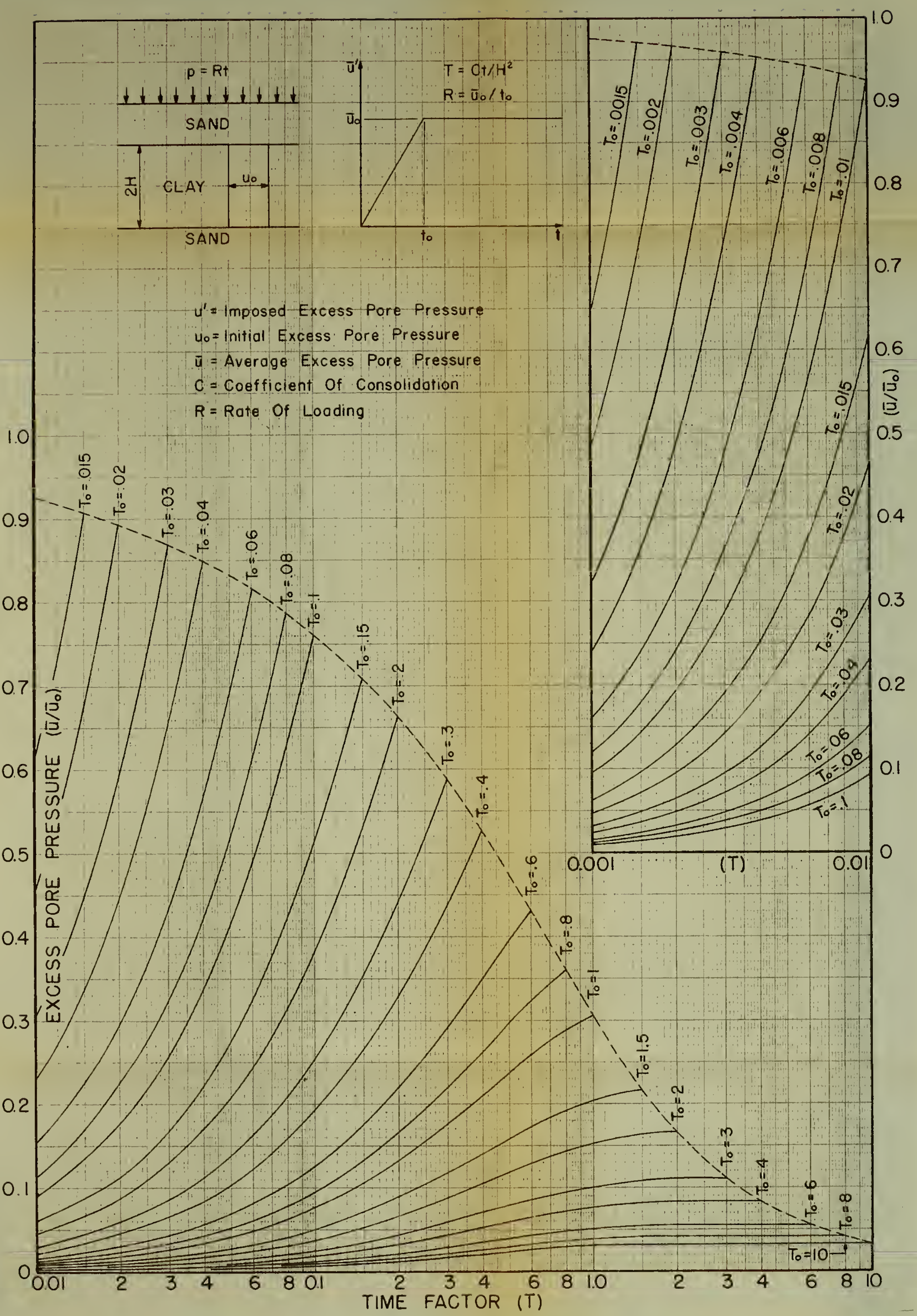
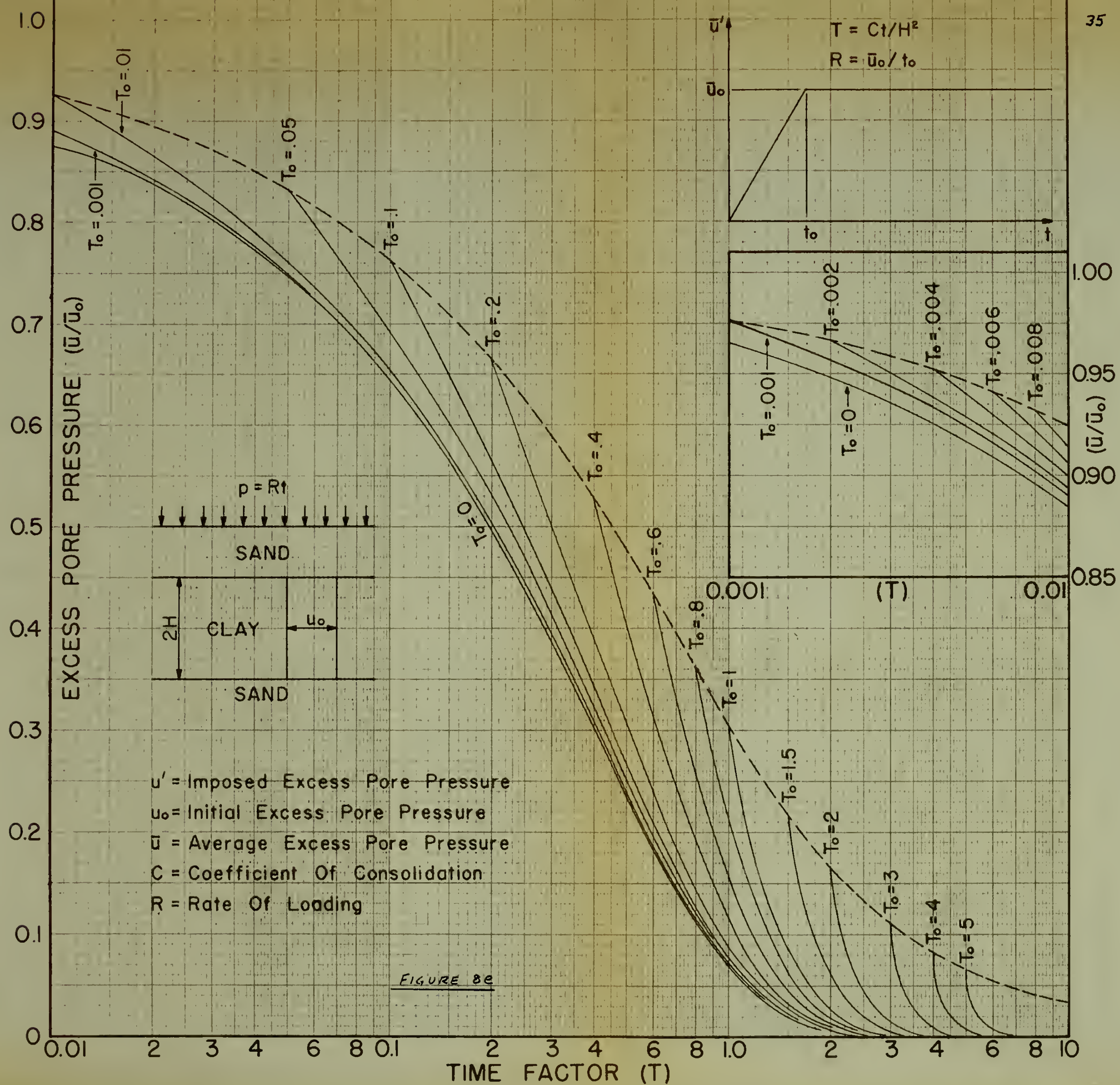


FIGURE 8d











$$\bar{u}(T') = \frac{8u_0}{\pi^2} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n^2} e^{-\frac{n^2\pi^2}{4} T'}$$

$$T' = \frac{1}{H^2} \left[ c_1 t_1 + c_2 (t_2 - t_1) + c_3 (t_3 - t_2) + \dots - c_m (t - t_m) \right]$$

By fitting incremental laboratory test curves to the theoretical curve, on the basis of theoretical values of  $u$  and  $t'$ , successive values of the bracketed term can be determined. The degree of accuracy desired can be controlled by the number of increments utilized in the fitting procedure.

A second approximation considers that an exponential permeability pore-pressure relationship will approximate the linear condition originally assumed, over the entire range of the consolidation process. The governing differential equation is:

$$B \frac{\partial^2 k}{\partial z^2} = \frac{\partial k}{\partial t}$$

With boundary conditions:

- (a)  $k(0,t) = k_f$
- (b)  $k(z,H,0) = k_f$
- (c)  $k(z,0) = \alpha u_0 + k_f$

The solution is:  $k(z,t) = k_f + \frac{4\alpha u_0}{\pi} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n} \sin \frac{n\pi}{2H} z e^{-\frac{n^2\pi^2}{4H^2} Bt}$

which when converted back to excess pore pressure is:

$$u(z,t) = \frac{4u_0}{\pi} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n} \sin \frac{n\pi}{2H} z e^{-\frac{n^2\pi^2}{4H^2} Bt}$$

where  $B$  is the Coefficient of Consolidation Permeability and is equal to:

$$B = \frac{k_0 - k_f}{\eta m \gamma_w}$$

12 17  
18 19

8 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100

where

$$\eta = LN \frac{k_o}{k_f}$$

The solution to the general case for one-dimensional consolidation can be utilized for varying permeability, if a new Time Factor  $V$  is substituted for  $T$  where:

$$V = \frac{B}{H^2} T$$

It is noted that as  $k_o$  approaches  $K_f$  the value of  $B$  approaches  $C$ .

It is essential, in this solution, to satisfy the condition that the soil have an initial and final coefficient of permeability, which is constant throughout the mass and at terminal points in any segment.



#### D. Permeability

The property of soil, concerned with the facility of travel of water through a soil mass, is termed Permeability. Since the physical properties of soils as well as the state of stress of the pore water have important effects on the mechanical behavior of a soil mass, it can be seen that this property is of major interest in the study of consolidation characteristics of soils.

The extremely small pore sizes encountered in most soils cause any flow of water through the soil mass to be laminar in nature, (i.e. the amount of head lost in friction is directly proportional to the velocity of flow). Such laminar flow takes place in accordance with dynamical equations of motion which by analysis of various simple channel shapes have been reduced to usable formulas. In engineering problems the flow through individual flow channels is not required, but it is rather the average flow through the soil mass which is important.

H. Darcy in 1856 demonstrated experimentally that the velocity of pore-water flow through a soil mass is directly proportional to the hydraulic gradient thus formulating the basic law of flow

$$v = k i$$

where  $v$  = Velocity of flow

$k$  = Coefficient of  
Permeability

$i$  = Hydraulic Gradient



The flow velocity, thus defined, is the superficial velocity through the soil mass, not the specific velocity through each flow channel.

To evaluate the coefficient of Permeability directly, the use of a constant head permeameter provides a quick, simple solution. Consider a soil sample with cross-sectional area,  $A$ , and height,  $L$ . Let there be a supply of water at constant elevation,  $H$ , above the sample, and let there be some means of measuring flow volume through the sample. With these values known, Darcy's Law can be re-written:

$$V = \frac{q}{A} = ki \quad \text{whence} \quad k = \frac{q}{iA} = \frac{qL}{AH} = \frac{QL}{AtH}$$

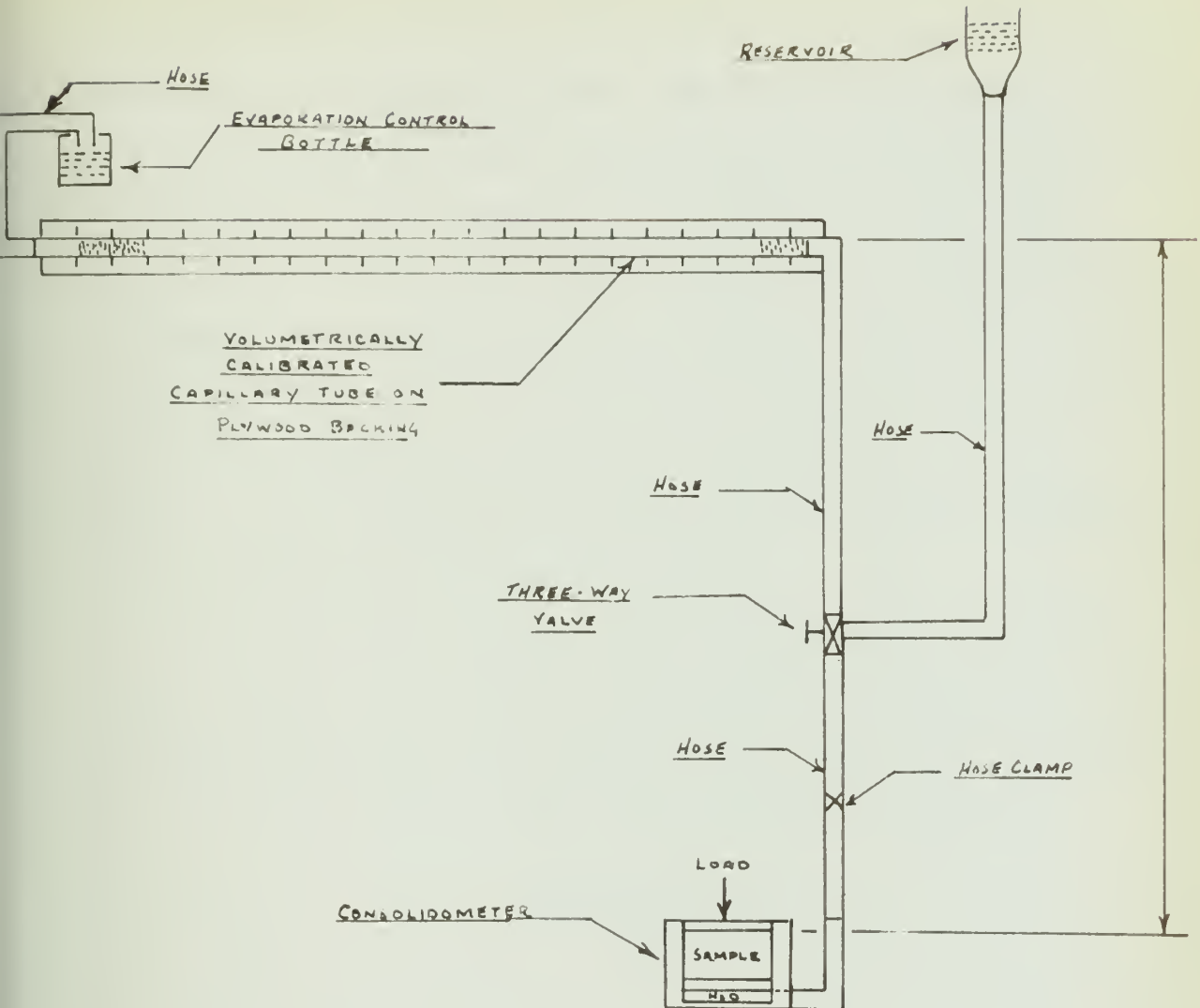
where  $Q$  = Total Volume of Flow and  $t$  = time.

The use of a constant-head permeameter has been restricted to soil types of relative coarse grading, since flow volume through fine grained soil is small. However by continuous measurement of flow volume during a consolidation test with the apparatus shown in Figure 9, flow volume measurement is a simple matter. In addition to the obvious advantages of consolidation-time values for flow volume, this apparatus eliminates the problems of air-pressure application encountered by Peterson (12) in using a variable head permeameter to measure flow through an Illite sample. In addition it makes possible, an almost instantaneous evaluation of permeability at any small finite time interval.





SCHEMATIC



OPERATING PROCEDURE

- 1 - CLEAR SYSTEM OF AIR BY FILLING CONSOLIDOMETER BASE WITH DISTILLED WATER, AND APPLYING VACUUM TO END OF CAPILLARY TUBE BY MEANS OF EVAPORATION CONTROL HOSE. CHECK FOR AIR IN RESERVOIR HOSE BY OPENING 3-WAY VALVE TO FEED INTO CAPILLARY TUBE.
- 2 - CLAMP HOSE WITH HOSE CLAMP
- 3 - PLACE SAMPLE IN CONSOLIDOMETER
- 4 - APPLY LOAD UNTIL  $\frac{1}{2}$  TSF IS ON SAMPLE
- 5 - WHEN  $\frac{1}{2}$  TSF IS ON SAMPLE, OPEN HOSE CLAMP.
- 6 - NOTE VOLUMETRIC READINGS ON PERMEAMETER, CONCURRENTLY WITH CONSOLIDATION READINGS
- 7 - REFILL PERMEAMETER DURING TEST AS REQUIRED.

FIG. 9



The evaluation of the coefficient of permeability obtained by use of the apparatus described above is a function of (1) the porosity of the soil mass (2) the shape and size of the voids and (3) the density and viscosity of the fluid.

Since we are dealing with a pure Kaolin Clay, laminar flow may be assumed. In dealing with the porosity of fine grained soils, it must be noted that the flow channel cross-sectional area is reduced by the amount of ionically "bound" water which is adsorbed on the surface of the soil particles and, being immovable, blocks part of the flow path.

The work of Schmid (13) indicates that the effect of this "bound" water can be reflected in an extension to the well-known Hagin-Poiseuille equation for laminar flow through a tube of constant cross-section (8). Schmid's equation:

$$k = \frac{\gamma_w D_e^2 (n - n_o)}{32 \mu}$$

Where  $\gamma_w$  = unit wt. of water

$D_e$  = Effective Diameter of Soil Particles

$n$  = Porosity of Soil

$n_o$  = ineffective Porosity i.e. channels blocked by "bound" water

$\mu$  = coefficient of viscosity of water

indicates that the coefficient of permeability is directly



proportional to the "effective" porosity,  $(n - n_0)$ . This concept would appear at variance with the experimental data compiled by numerous investigators, which shows that plot of  $k$  vs  $\log e$  as a straight line, i.e. an exponential relationship. However as Schmid points out, the basic relationship,  $n = \frac{e}{1+e}$  is actually only an approximation of the series expansion of the function  $\log \frac{1}{n}$  or  $\log \frac{e+1}{e}$ , which ignores the higher order terms. In actuality the relationship between  $n$  and  $e$  is logarithmic and thus Schmid's work can be reconciled with other investigators' work if this factor is recognized. The error involved in ignoring the higher order terms is less than 10% and decreases rapidly with increasing void-ratio.

The straight-line relationship between porosity and the coefficient of permeability does not hold in the region  $n \approx n_0$  and Schmid indicates that such deviation can be expected, since in deriving his equation he made two approximating assumptions:

(1) That the effective diameter,  $D_e$ , is constant.

(2) That the ineffective porosity,  $n_0$ , is constant.

which are never achieved in actual testing. It is further suggested that the consolidation process, by virtue of its reduction in rate of porosity change at large loading increments, would indicate that such deviation should be expected in such regions. Since these regions are the same



as where  $n \neq n_0$ , The straight-line relationship would thus be invalid for larger load increments where porosity changes are small relative to the applied load,

The accurate evaluation of the coefficient of permeability, during the consolidation process, is of extreme importance, since the simplifying assumptions of both Terzaghi and Schiffman, include  $k$  as a constant for the one-dimensional drainage conditions considered herein. The determination of the manner of variance of  $k$  with decreasing porosity under consolidation loading would be of assistance in the solution of the more complicated time-and-space dependent consideration of the consolidation process as proposed by Schiffman. Toward this end the evaluation of  $k$  during the consolidation process will be attempted as part of this work.





PART III  
MATERIALS AND APPARATUS

The soil samples used in the conduct of this investigation were prepared from oven-dried pure Kaolin clay secured from WARD'S NATURAL SCIENCE CORP., Rochester, N.Y. under the sample designation "Kaolinite-Dry Branch Ga. Dana #492". This relatively pure clay mineral exhibited a very sensitive reaction to moisture, as noted during the tests for determination of the liquid limit, where the addition of a few drops of distilled water changed the blow count by 10.

For the conduct of the control test, Number 1, a standard Fixed Ring Consolidometer as shown in Figure 10 was utilized.

The application of time-dependent loading to the samples during tests Number 2, 3, 4 ~~and 5~~, was accomplished by means of the apparatus shown in Figure 11. A Conbel Model No. 350 Consolidometer was adapted for use with a King Manufacturing Company visual bleed. The visual bleed, referred to throughout as a time-dependent loading device, was filled to within approximately one and one-half ( $1\frac{1}{2}$ ) inches of the air outlet with a high-quality brake fluid. The pressure accumulator and bellows on the Conbel equipment were also filled with brake fluid in accordance with the manufacturers instructions.



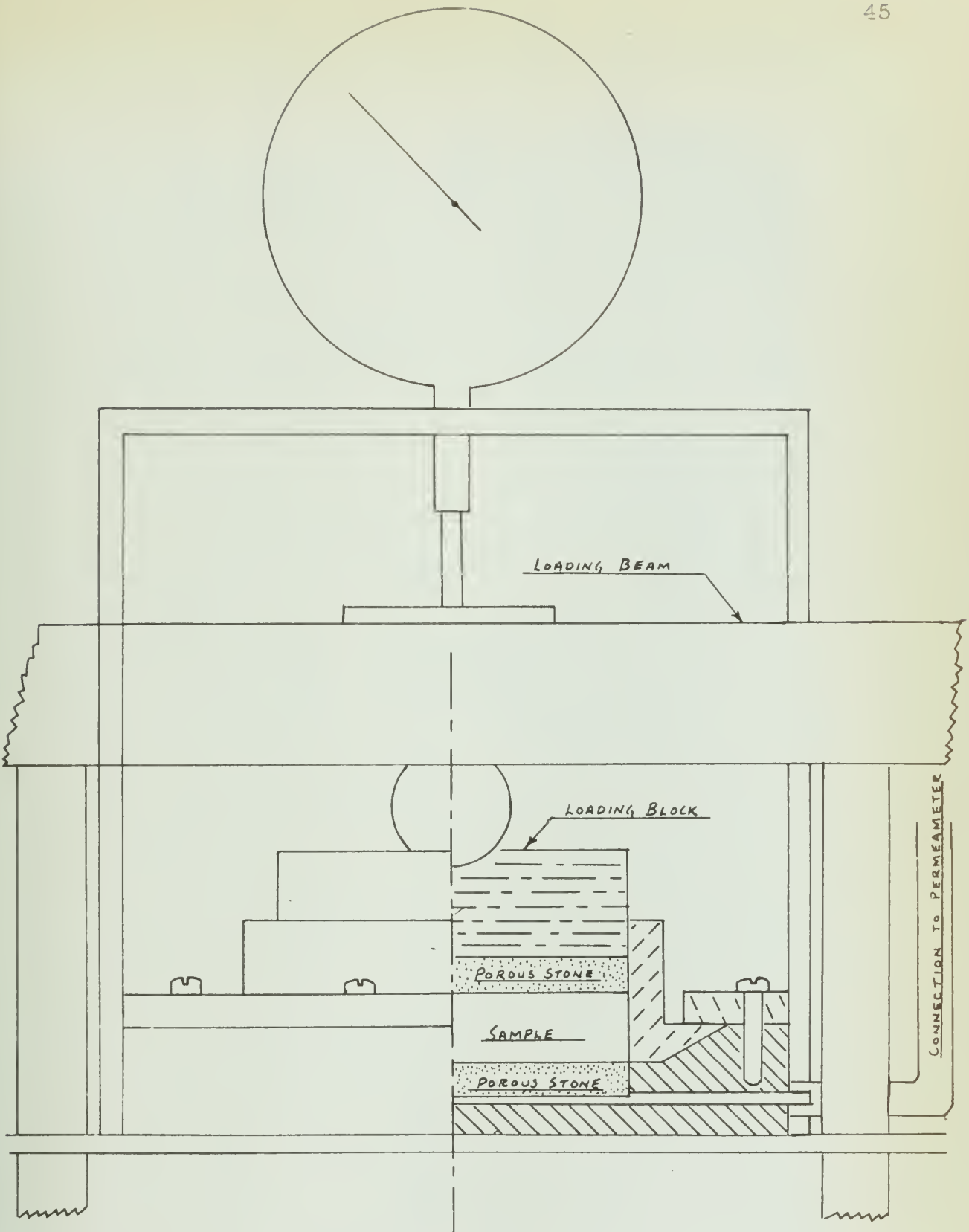


FIG. 10 STANDARD FIXED RING CONSOLIDOMETER (FULL SCALE)



SCHEMATIC

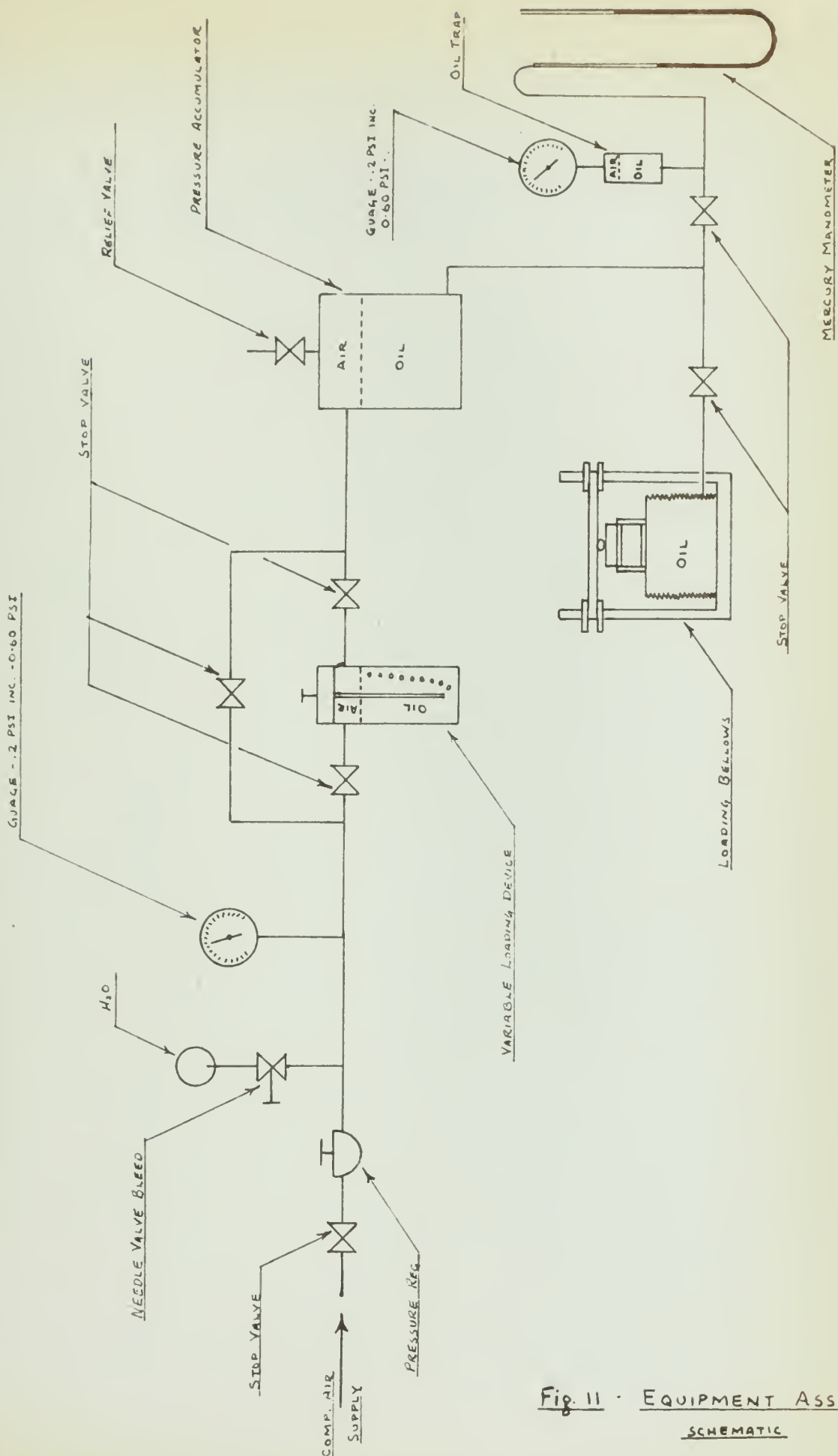


Fig. 11 · EQUIPMENT ASSY  
SCHEMATIC



For the direct measurement of permeability during all tests conducted, a constant head permeameter as shown in Figure 9 was constructed and utilized.





## PART 1V

Testing ProcedureA. Preparation of Sample

All samples were prepared at the Liquid Limit determined in accordance with ASTM "Standard Method of Test for Liquid Limit of Soils", ASTM Designation D-423-39. Flow Curves used in determining the Liquid Limit are shown in Figure 12. Reproducibility of the Liquid Limit in mixing the sample prior to testing was considered to be satisfactorily attainable by use of the Standardized Spatula Method, as may be evidenced by the moisture content deviation being less than 1% for all samples. The electric mixing of samples as proposed by Edmonds and Warren (10) was attempted but not utilized since the entrainment of air within the sample appeared excessive.

The sample was placed as follows: a 200 gram. dry weight, sample was prepared at 3% above the Liquid Limit and transferred from the evaporating dish to an open plastic cylinder 4 inches in height and 2.500 inches in diameter. The cylinder was sealed by a metal plate at one end and beaten strongly against a solid surface, concurrently rotating and tapping the sides of the cylinder with a metal rod. Entrapped air is visibly removed during this process. The sample is then extruded by means of a porous stone piston on to a glass plate covered with a filter paper. The planar surface, produced by extrusion into the glass plate, is then forced into the fixed ring and the sample accurately trimmed to the ring size.





LIQUID LIMIT DETERMINATION  
FROM CURVE

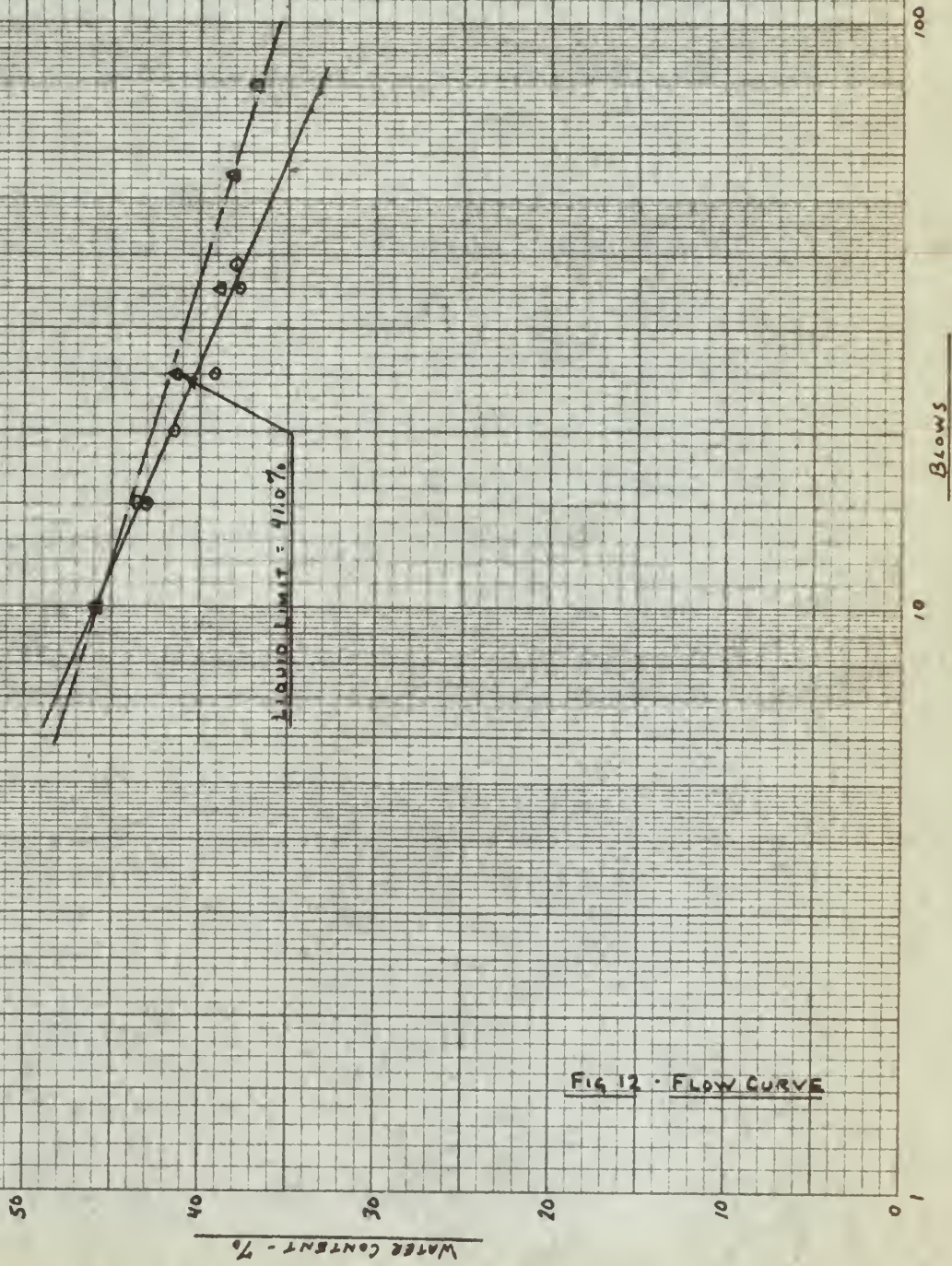


FIG 12 - FLOW CURVE





## B. Standard Consolidation Test

Test No. 1 was conducted on a standard Fixed Ring consolidometer as described in Part III. As suggested by Professor Burmister (11) this test was used as a pilot study to establish techniques of sample preparation and testing. Since no apparent swelling resulted from immersion of the sample, and the strain did not exceed .02 in. per in. it was decided that the testing cycle shown in the raw data sheets of Appendix I would be satisfactory. It is to be noted that there is a dearth of literature on the preparation of disturbed samples for consolidation testing, which factor makes a pilot test of this nature an absolute necessity for any testing of such materials. Appendix I also includes raw data from a concurrent pilot test conducted by V. McGuffey on the same material with the same equipment. McGuffey's results show that reproducible results can be attained if technique and procedure are carefully analyzed and correlated.



### C. Time Dependent Loading Tests

Tests No. 2 and 3 were conducted using the apparatus described in Part 111. The Conbel equipment was calibrated by the use of dead weights vs. air pressure and it was determined that the calibration charts furnished by the manufacturer were accurate to within one pound of load applied to the sample in the 1-2 ton range. It is suggested that future calibrations of this equipment be accomplished by a proving ring with a planar upper surface to insure axial loading. Attempts to calibrate the equipment with standard laboratory proving rings were unsuccessful, due to the tilting of the bellows at pressures above 4 psi due to lack of axial resistance to load by the proving ring.

Figure 13 shows the calibration procedure followed for the time-dependent loading device. Tables 2 and 3 indicates calibration pressures and data in tabular form.

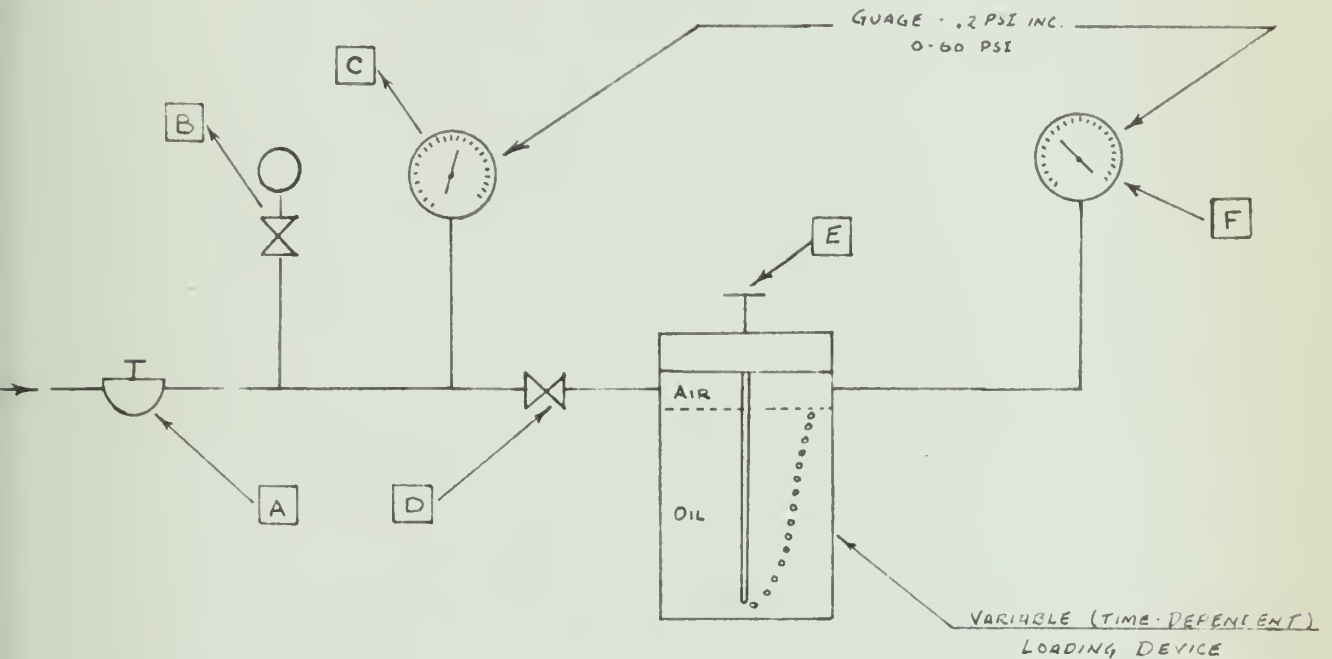
Figure 14 indicates the operational procedure followed in applying time dependent loading to the sample by means of the time-dependent loading device.

Raw data showing pressure increments and loading cycle times are contained in Appendix 2 and 3.





CALIBRATION PROCEDURE  
FOR  
VARIABLE LOADING DEVICE  
SCHEMATIC



PROCEDURE

1. CLOSE D
2. ADJUST A TO DESIRED INITIAL PRESSURE
3. ADJUST B UNTIL C READS DESIRED INITIAL PRESSURE
4. READ C AND F, NOTE READINGS
5. OPEN D, NOTE TIME
6. COUNT NUMBER OF BUBBLES PER MINUTE FOR VARIOUS SETTINGS OF E
7. NOTE TIME THAT READING ON F EQUALS READING ON C
8. NUMBER OF BUBBLE PER MINUTE CORRELATES TIME-RATE OF PRESSURE BUILD-UP BETWEEN C AND F

FIG. 13



CALIBRATION OF LOADING BELLOWS

CHECK CALIBRATION		MANUFACTURER'S CALIBRATION	
WEIGHT lbs	GAGE PSI	WEIGHT ON BELLOWS - lbs	GAGE PSI
30	1.45	30	1.50
40	1.80	40	1.80
50	2.20	50	2.25
60	2.62	60	2.65
70	3.05	70	3.05

EQUIVALENT LOAD ON SAMPLE - GAGE PRESSURE

LOAD ON 2 1/2 IN. SAMPLE TONS/SQ	LOAD ON 2 1/2 IN. SAMPLE lbs	GAGE PRESS. PSI	AREA OF 2 1/2 IN. SAMPLE SQ. IN.
.25	17.0	.75	4.909
.50	34.1	1.5	
1	68.2	3.0	
2	136.4	6.0	
4	272.7	12.0	
8	545.4	24.0	Y

CORRECTION FOR BELLOWS EXPANSION

CONSOLIDATION OF SAMPLE IN.	CORRECTION ADD IN.	CONSOLIDATION OF SAMPLE IN.	CORRECTION ADD IN.
.025	.1	.125	.5
.05	.2	.150	.6
.075	.3	.175	.7
.10	.4	.200	.8



TABLE 3

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CALIBRATION OF TIME-DEPENDENT  
LOADING DEVICE

<u>LOAD RANGE</u>	<u>DRIVE PRESSURE</u>	<u>PRESSURE ON SAMPLE</u>	<u>BUBBLES / MIN</u>	<u>TIME (MIN)</u>
0-.75 PSI		0 - 1/4 TSF		
.75-1.5 PSI	7.5 PSI	1/4 - 1/2 TSF	5	480
1.5-3.0 PSI	8 PSI	1/2 - 1 TSF	7	480
3.0-6.0 PSI	20 PSI	1 - 2 TSF	15	480
6.0-12.0 PSI	20 PSI	2 - 4 TSF	24	480
12.0-24.0 PSI	30 PSI	4 - 8 TSF	36	480

N.B. THE ABOVE CALIBRATION IS SUBJECT TO ERROR IN THAT THE VARIABLES INVOLVED ARE NOT AMENABLE TO RIGID CONTROL. THE CALIBRATION WAS CONDUCTED WITH NO SAMPLE IN PLACE AND WITH VARYING AIR TEMPERATURES. THE EXTREME VARIANCE OF TIME OF PRESSURE APPLICATION FROM THE ABOVE VALUES MAY BE NOTED IN THE RAW DATA FOR TESTS No 2 and 3. THE PRECISION OF SETTING THE BUBBLE RATE IS OF NECESSITY SUBJECT TO HUMAN APPROXIMATION, AND IS CONSIDERED TO BE THE MAJOR SOURCE OF VARIANCE.

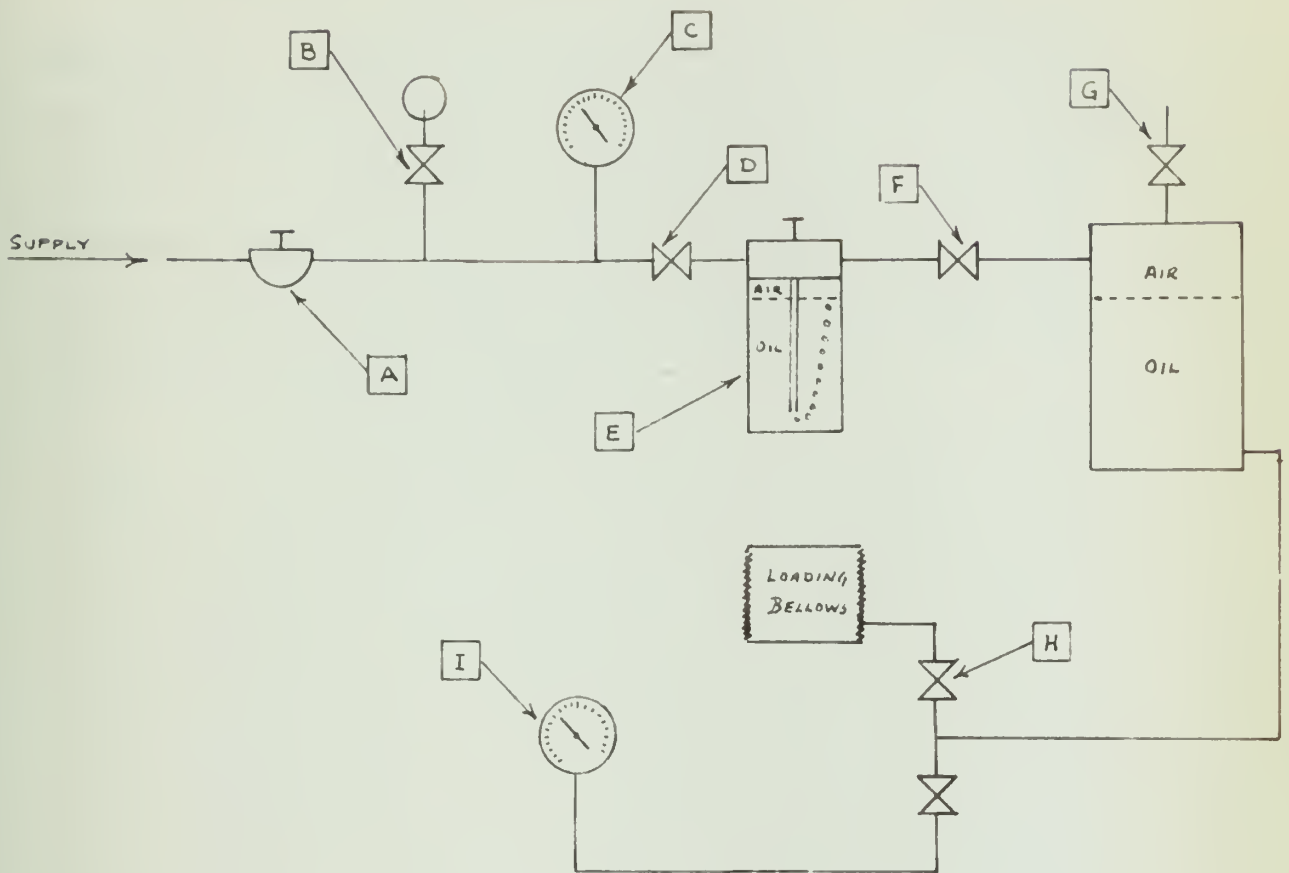


A PROCEDURE FOR APPLICATION

80

OF  
TIME DEPENDENT LOADING

SCHEMATIC



PROCEDURE

1. CLOSE H
2. CLOSE D
3. ADJUST A TO DESIRED INITIAL PRESSURE
4. ADJUST B UNTIL C READS EXACT INITIAL PRESSURE REQUIRED
5. OPEN D
6. ADJUST E TO TIME-RATE REQUIRED
7. ADJUST G TO INSURE THAT READING ON I IS THE SAME AS AT THE END OF PREVIOUS LOADING CYCLE
8. CHECK E TO INSURE THAT TIME-RATE IS AS REQUIRED
9. QUICKLY CLOSE G
10. QUICKLY OPEN H
11. READ CONSOLIDOMETER AT REQUIRED TIME INTERVALS

FIG. 14





D. Pseudo Time Dependent Loading Tests

Tests 4 ~~and 5~~ were conducted in an effort to approximate time-dependent application of load by use of small incremental loadings over small finite time intervals. Load was applied instantaneously by by-passing the time dependent loading device as shown in Figure 11. Raw data showing pressure increments and loading cycle times are contained in Appendix 4 ~~and 5~~.



### E. Permeability Measurements

Direct measurement of Permeability was achieved by means of a constant head permeater as shown in Figure 9. A capillary tube was calibrated to .1 c.c. and volume decrease noted at each reading of the consolidometer. Thus a direct relationship between permeability and void ratio was established for all points of the consolidation process.

Considerable difficulty was experienced in establishing valid permeability data under small loading conditions (i.e.  $\frac{1}{4}$  t.s.f.). The permeameter head is sufficient to cause sample uplift prior to application of load and as is shown in Appendix 4, affects the consolidation process to a considerable extent. It was therefore necessary to restrict permeability measurements to loadings of greater than  $\frac{1}{2}$  t.s.f.

It must also be noted that the direct measurement of  $k$  for such a material as Kaolinite involves extremely small measurements of flow volume. Such measurement is feasible under time-dependent loading conditions since the porosity is decreasing at a rate which permits accurate gage readings for flow volumes of sufficient magnitude as will minimize interpolation errors. However in instantaneously loaded samples, the load application:

- (1) Creates an initial surge of pressure which causes a negative flow into permeameter for a period of approximately 3 minutes.



- (2) Seriously restricts the evaluation of permeability data after the initial 3 minute surge period, because of the lack of knowledge as to the time or pressure limits of its influence after the initial 3 minutes.

The problem involved in (2) above is reflected in **widely** scattered permeability values for all load increments of Test No. 1.



PART V,  
RESULTS and DISCUSSION

A. EQUIPMENT

The test equipment, as designed and assembled, provided data of sufficient accuracy for a pilot study of this nature. For future development of test data, requiring reproducible results for purposes of definitive analysis and for publication, the equipment should be modified to provide the following:

- (1) Precise control of load application during the Time Dependent Loading cycles.
- (2) Smaller bore, equivalent volume permeameter to provide more precise calibration of flow volume.

DISCUSSION:

- (1) The application of Load at a fixed linear rate is of extreme importance in the conduct of tests designed to investigate the validity of Schiffman's extension of the theory for the one dimensional flow condition. It is noted that the rate of change of imposed excess pore pressure,  $R$ , found in the governing differential equation, is in fact the rate of application of load. Therefore for any of the cases considered in his treatment of the one-dimensional flow condition, the loading device must be capable of precise control, if correlative data is to be developed.





(2) The use of the Constant-Head Permeameter is well adapted for precise measurement of permeability during the consolidation process. However, the small flow volume, encountered with the use of clay soils, dictates a finer calibration of the horizontal tube, in order to minimize approximating errors. A smaller bore tube would provide the precision required but has the disadvantage of reduced volume availability. Such reduction in volume can only be compensated for in two ways: (1) Extreme length of tube or (2) Constant attendance to preclude evacuation of the tube. A reasonable balancing of these two factors would appear to be feasible. The increase in accuracy, resultant, cannot be estimated, but would be of extreme value in analyzing permeability variation.



## B. TEST NO.1 - STANDARD CONSOLIDATION TEST

Test Data in graphical form is presented in Figure 16.

### Discussion:

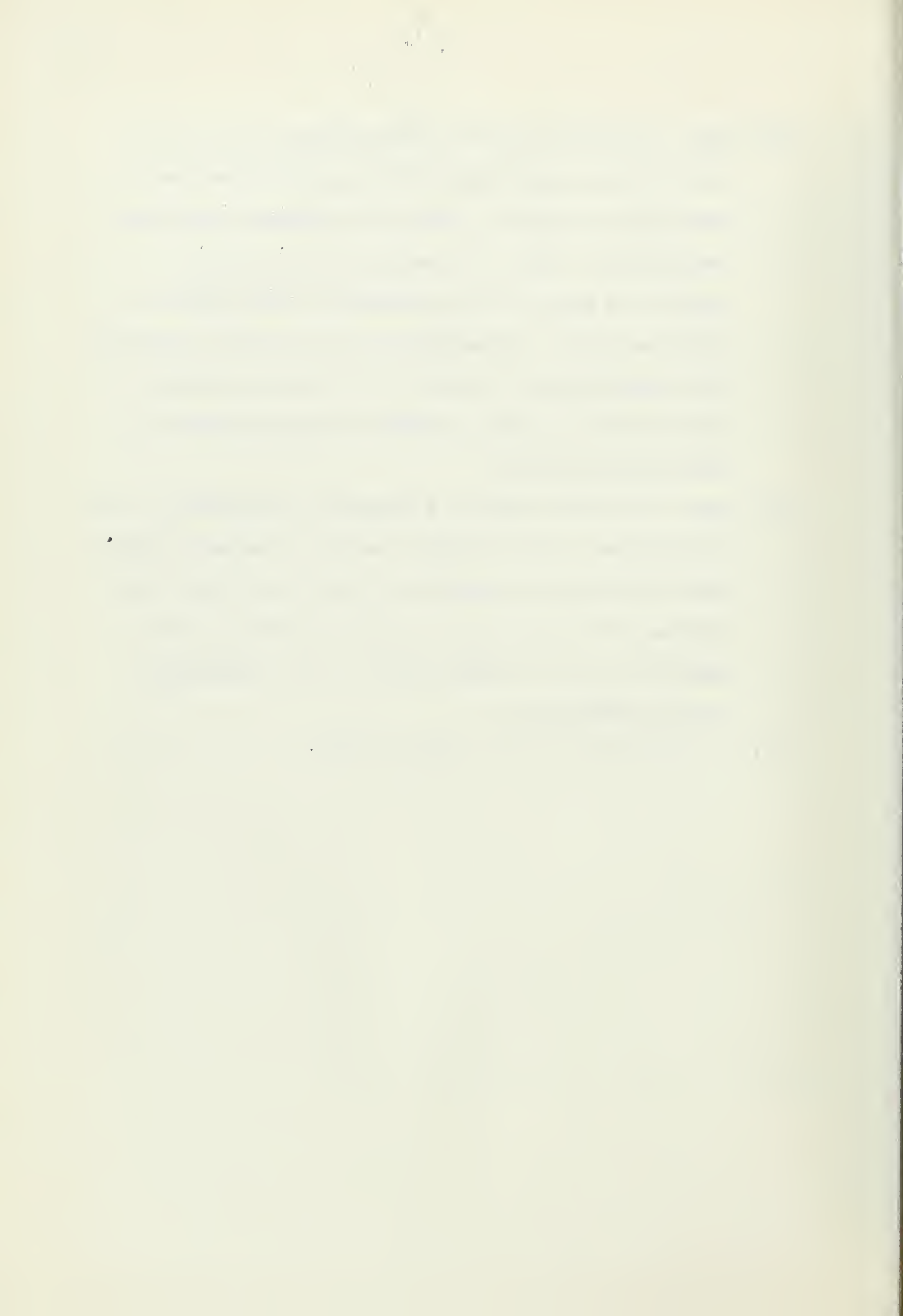
The data developed is typical of the "type" curves for the Kaolin clay used. The work of previous investigators (10) closely parallels the results achieved. The variance in  $C_v$  values is reasonable and the shape of curves is similar.

The problem of sample uplift, due to the head of the permeameter, precludes permeability measurements prior to the application of  $\frac{1}{2}$  ton per square foot loading. This, however, is not a serious difficulty since it should be noted that the loading range involved is usually on the precompression portion of the  $e$ -log  $P$  curve. Since usable data can be developed only on the straight-line portion of the curve, where the uplift problem is no longer existant, the problem does not actually affect test results.

The determination of the permeability of the test samples, under instantaneous load application, is a problem which requires a great deal of interpretative analysis during the primary consolidation period. It is noted that an initial negative flow into the permeameter persists for a period of 2-3 minutes, immediately following the application of load. This flow can be interpreted in three ways:



- (1) That the flow is due to the squeezing out of Pore water by the application of load, which process is essentially complete during the primary consolidation period. With the dissipation of such pore water, the head of the permeameter then induces a positive flow. The validity of the initial positive flow measurements is subject to serious question since there is still existant a varying amount of hydrostatic excess.
- (2) That the flow is due to a hydraulic balancing of the load-imposed pore pressure and the permeameter head. Such balancing is subject to a time lag since the transmissibility of pore pressure differs at the top and bottom boundaries due to the counterhead of the permeameter.
- (3) A combination of (1) and (2) above.





TEST No 1

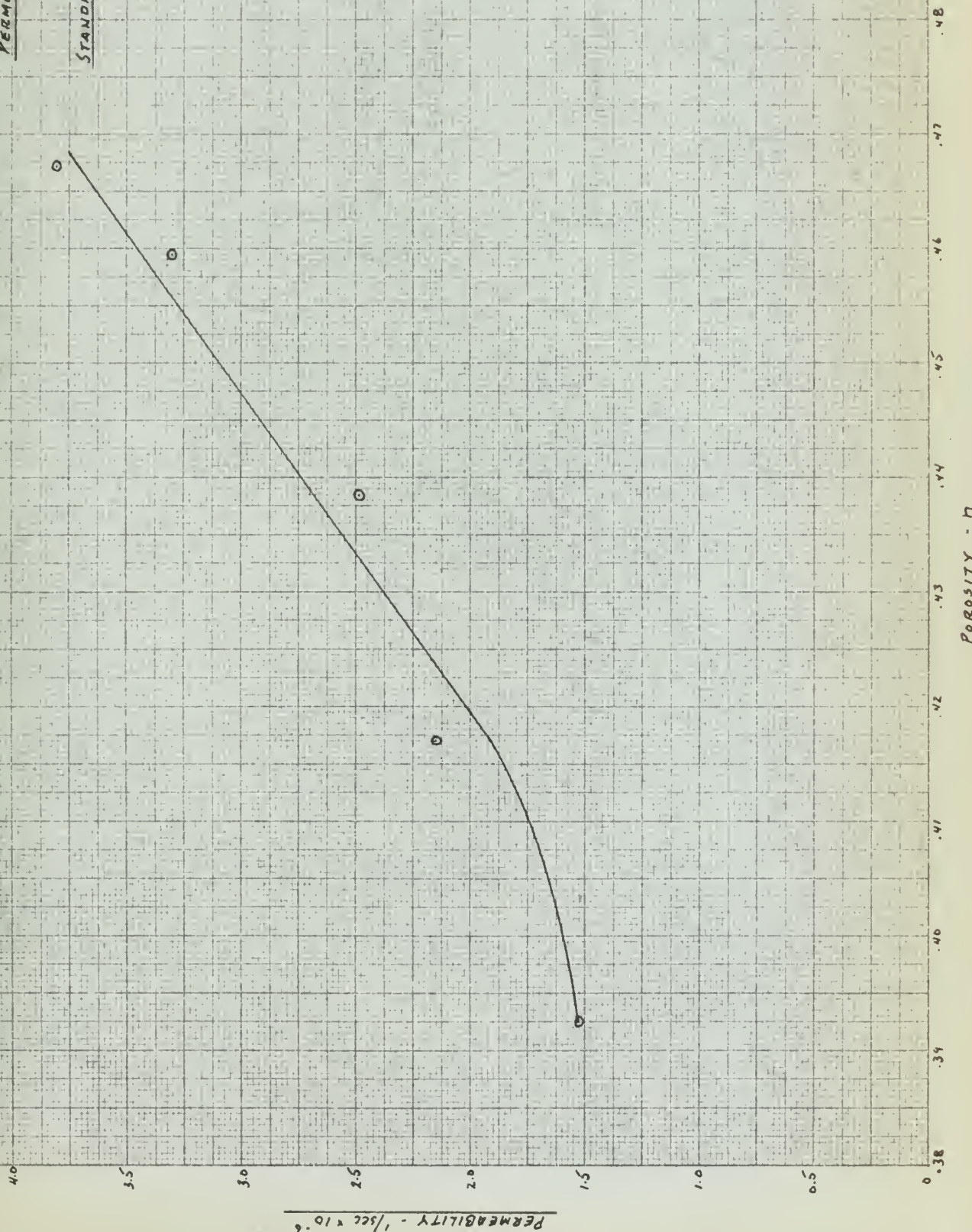
PERMEABILITY VS POROSITY

UNDER

STANDARD INSTANTANEOUS

LOADING

FIGURE 15-1







1.6  
1.4  
1.2  
1.0  
0.8  
0.6  
0.4  
0.2

TEST No. 1

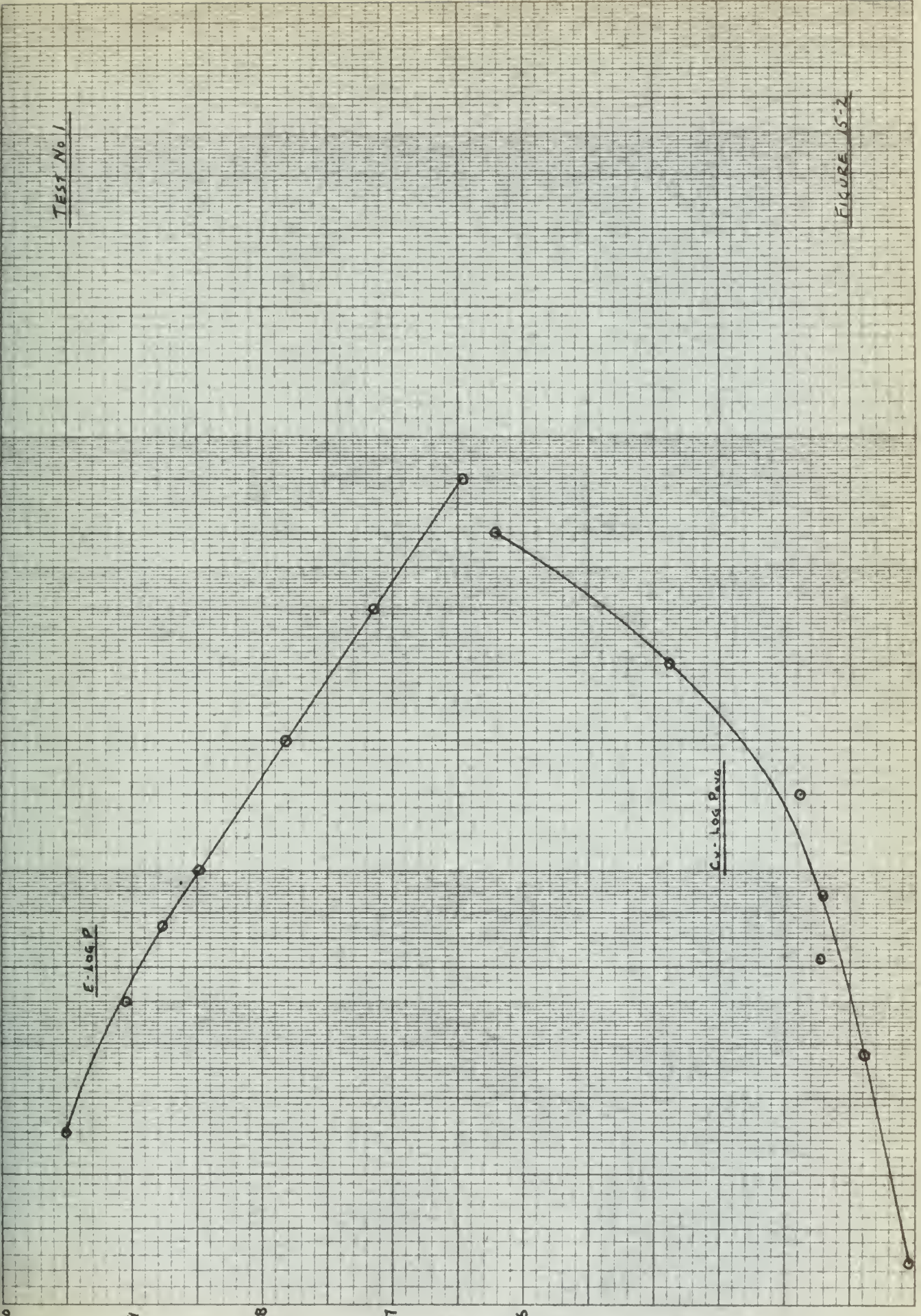
FIGURE 15-2

10.0

PRESSURE - (T/IN)

1.0

0.10



$e - \log p$

$C_v - \log p_{avg}$





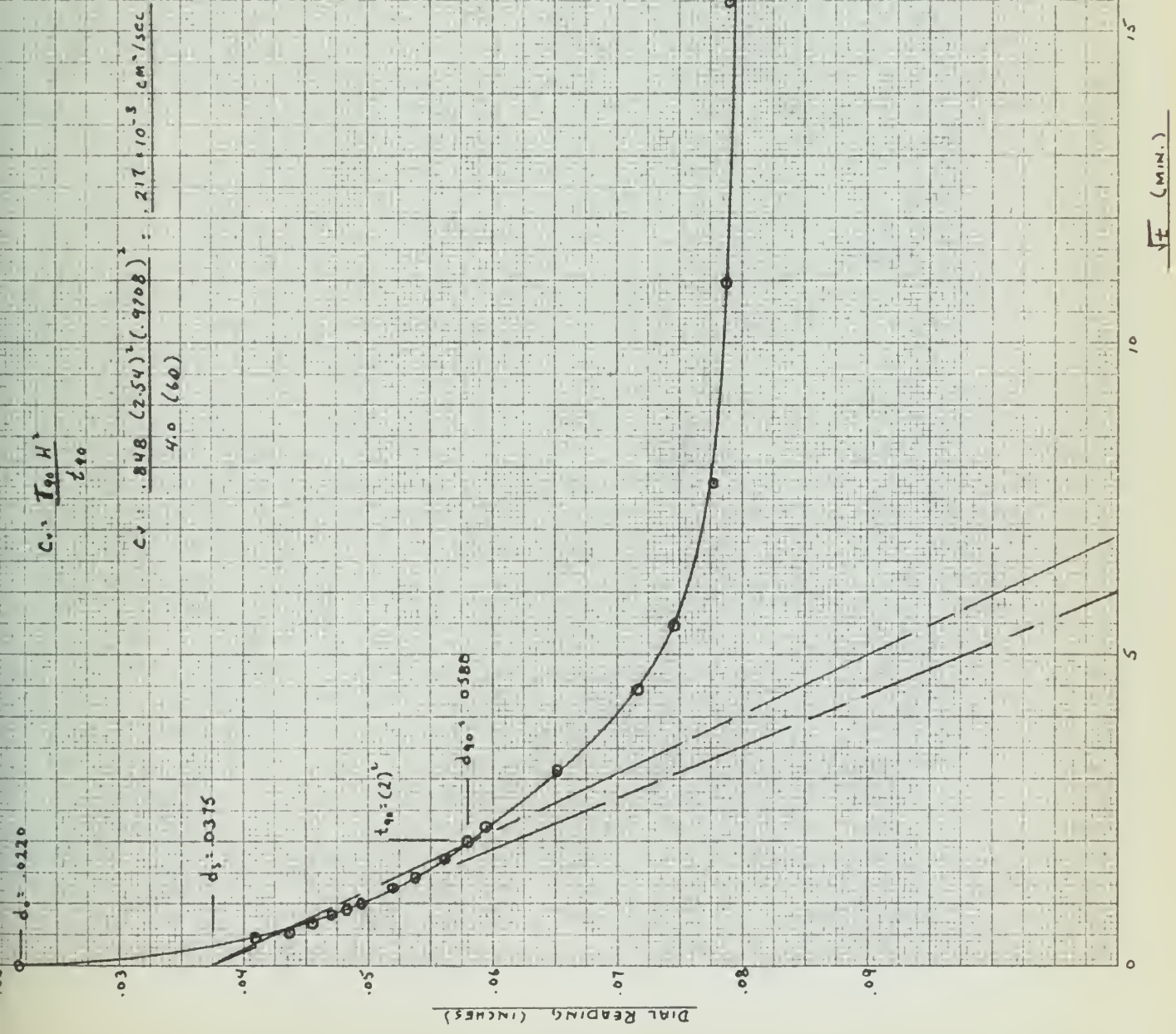
TEST No. 1

11 MARCH 1958

0-1/4 T138 LOADING

NO PERMEABILITY MEASUREMENTS TAKEN DURING THIS CYCLE

FIGURE 15-3







TEST No. 1  
12 MARCH 1958

1/4 - 1/2 T134 LOADING

NO PERMEABILITY MEASUREMENTS  
TAKEN DURING THIS CYCLE

$$C_v = \frac{T_{90} H^2}{L_{90}}$$

$$C_v = \frac{848 (2.54)^2 (1.9295)^2}{2.25 (60)} = .3525 \times 10^{-3} \text{ cm}^2/\text{SEC}$$

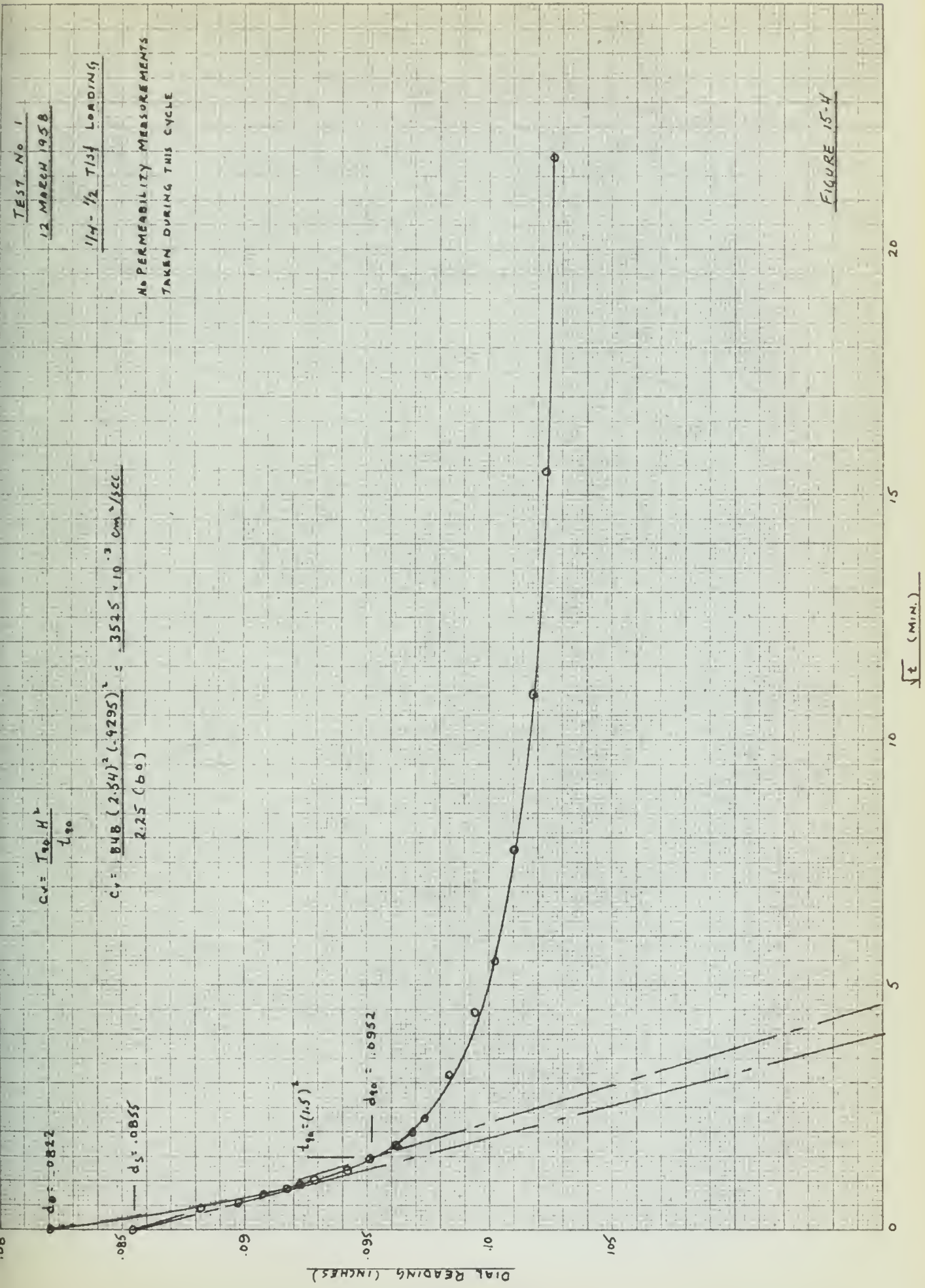


FIGURE 15-4





TEST No 1

13 MARCH 1958

112-314 T135 LOADING

PERMEABILITY MEASUREMENTS

TAKEN DURING THIS CYCLE

$$C_1 = \frac{T_{90} H^2}{t_{90}}$$

$$C_1 = \frac{848 (2.54)^2 (9.118)^2}{(1.69)(60)} = 493 \times 10^{-3} \text{ cm}^2/\text{sec}$$

$$d_s = 1063$$

$$t_{90} = (1.2)^2$$

$$d_{90} = 1110$$

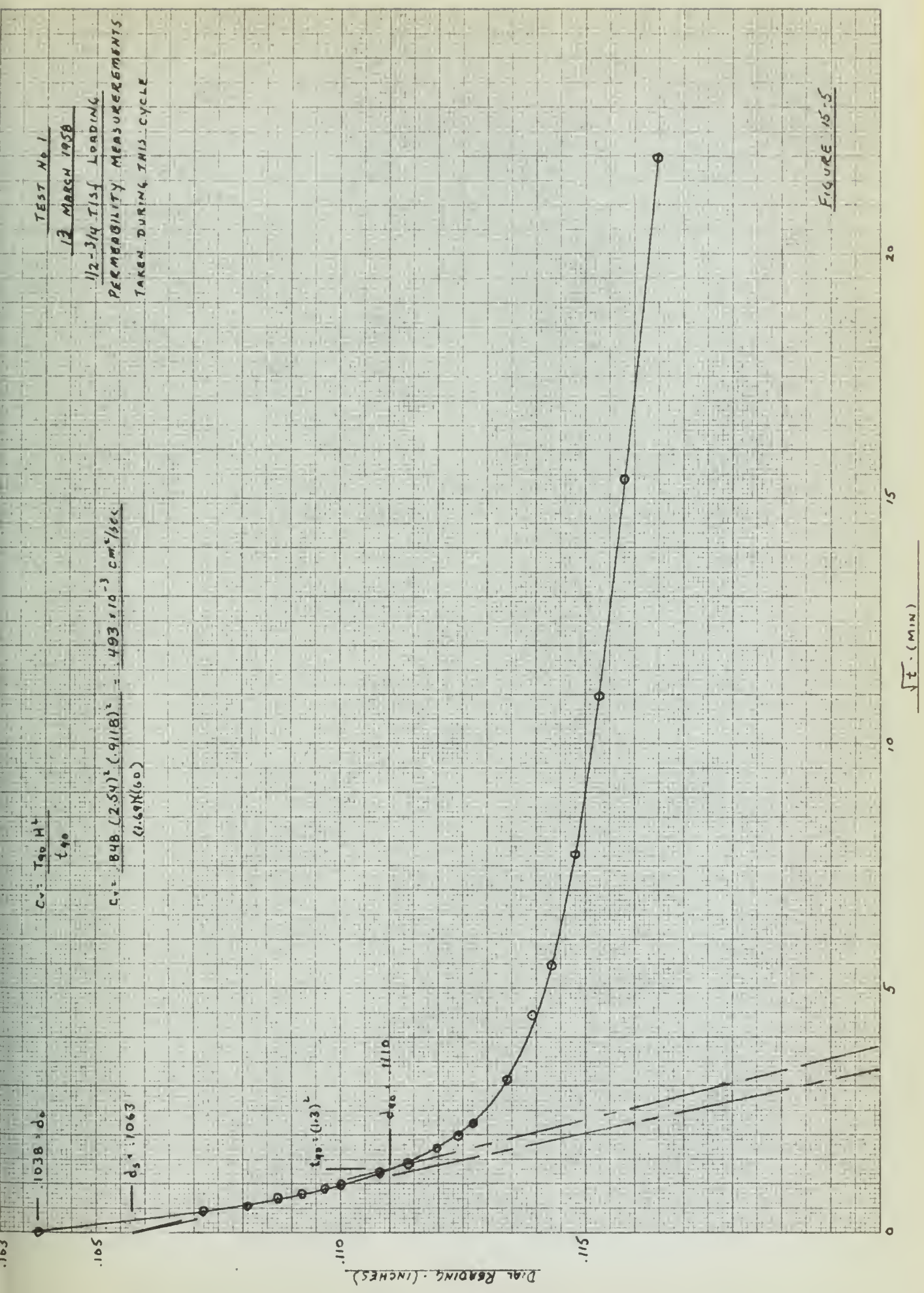


FIGURE 15-5





TEST No. 1

14 MARCH 1958

3/4" 1 TSE LOADING

PERMEABILITY MEASUREMENTS  
TAKEN DURING THIS CYCLE

$C_{TC} = \frac{T_{90} M^2}{t_{90}}$   
 $C_{TC} = .848 (2.54)^2 (0.974) = .485 \times 10^{-3} \text{ cm}^2/\text{sec}$   
 $.169 (60)$

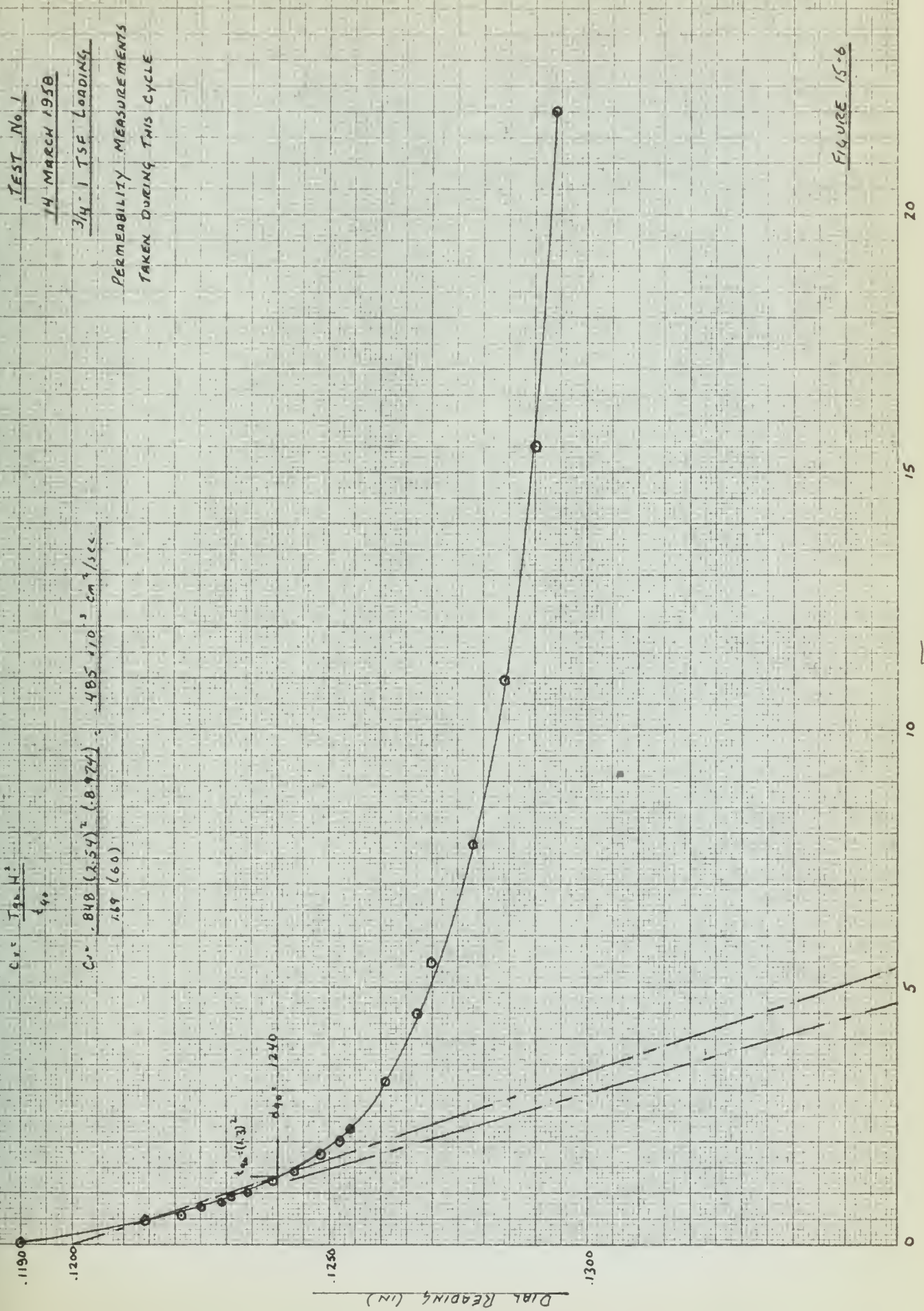


FIGURE 15-6





TEST No 1

15 MARCH 1958

1.2 T5F. LOADING

PERMEABILITY MEASUREMENTS  
TAKEN DURING THIS CYCLE

$$C_p = \frac{848 (2.54)^2 (8755)}{1.44 (60)} = 555 \times 10^{-3} \text{ cm}^2/\text{sec}$$

$$C_p = \frac{T_{90} H^2}{L^2 A_0}$$

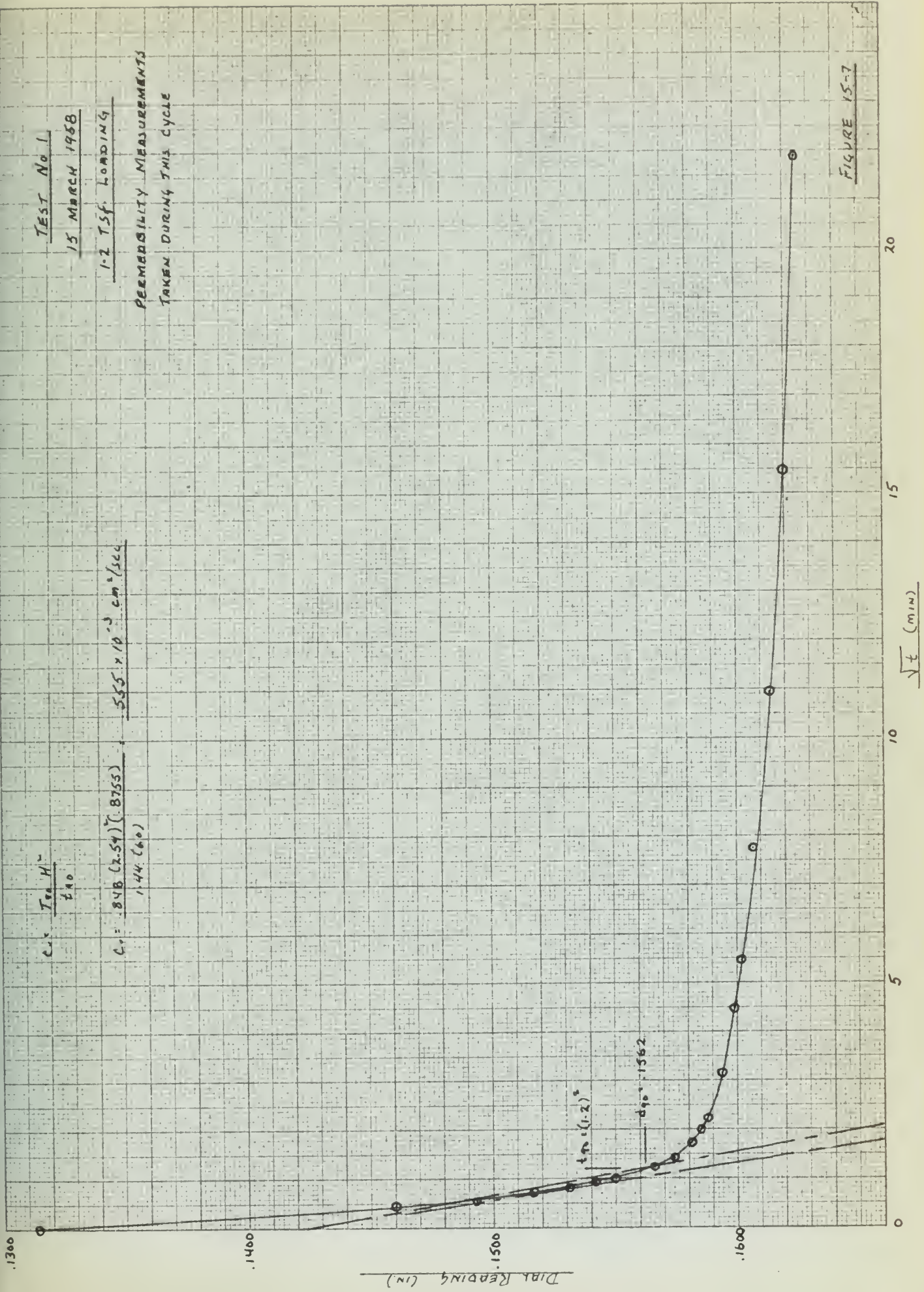


FIGURE 15-7





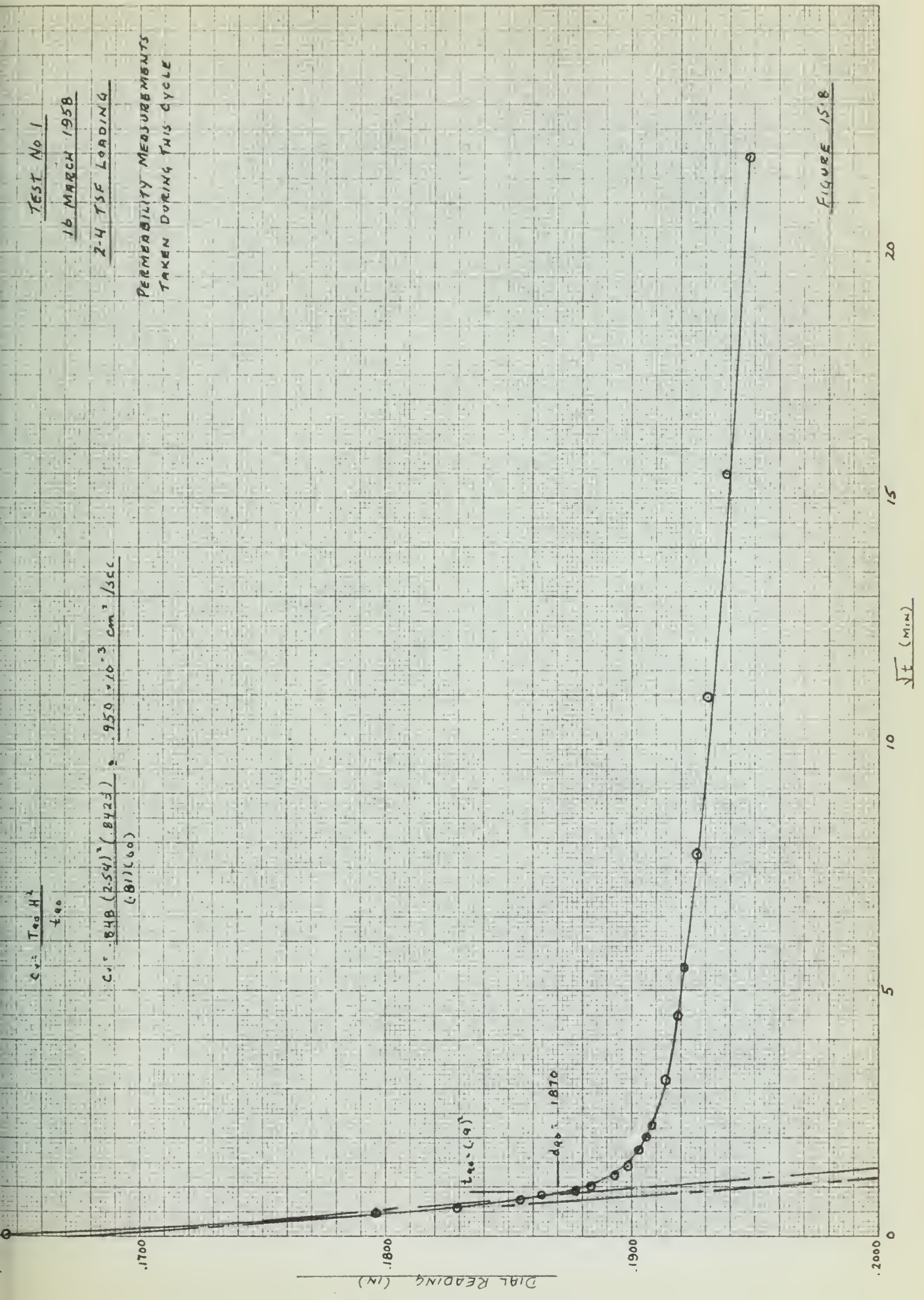
TEST No 1

16 MARCH 1958

2-4 TSF LOADING

PERMEABILITY MEASUREMENTS  
TAKEN DURING THIS CYCLE

$C_v = \frac{T_{90} H^2}{4 t_{90}}$   
 $C_v = \frac{.848 (2.54)^2 (.8425)}{4 (811.60)} = .950 \times 10^{-3} \text{ cm}^2 / \text{SEC}$







TEST No 1

17 MARCH 1958

N-B TSF LOADING

PERMEABILITY MEASUREMENTS  
TAKEN DURING THIS CYCLE

$$C_v = \frac{I_{90} H^2}{t_{90}}$$

$$C_v = \frac{.848 (2.54)^2 (1800)}{49 (60)} = \frac{1.49 \times 10^{-3} \text{ cm}^2/\text{sec}}$$

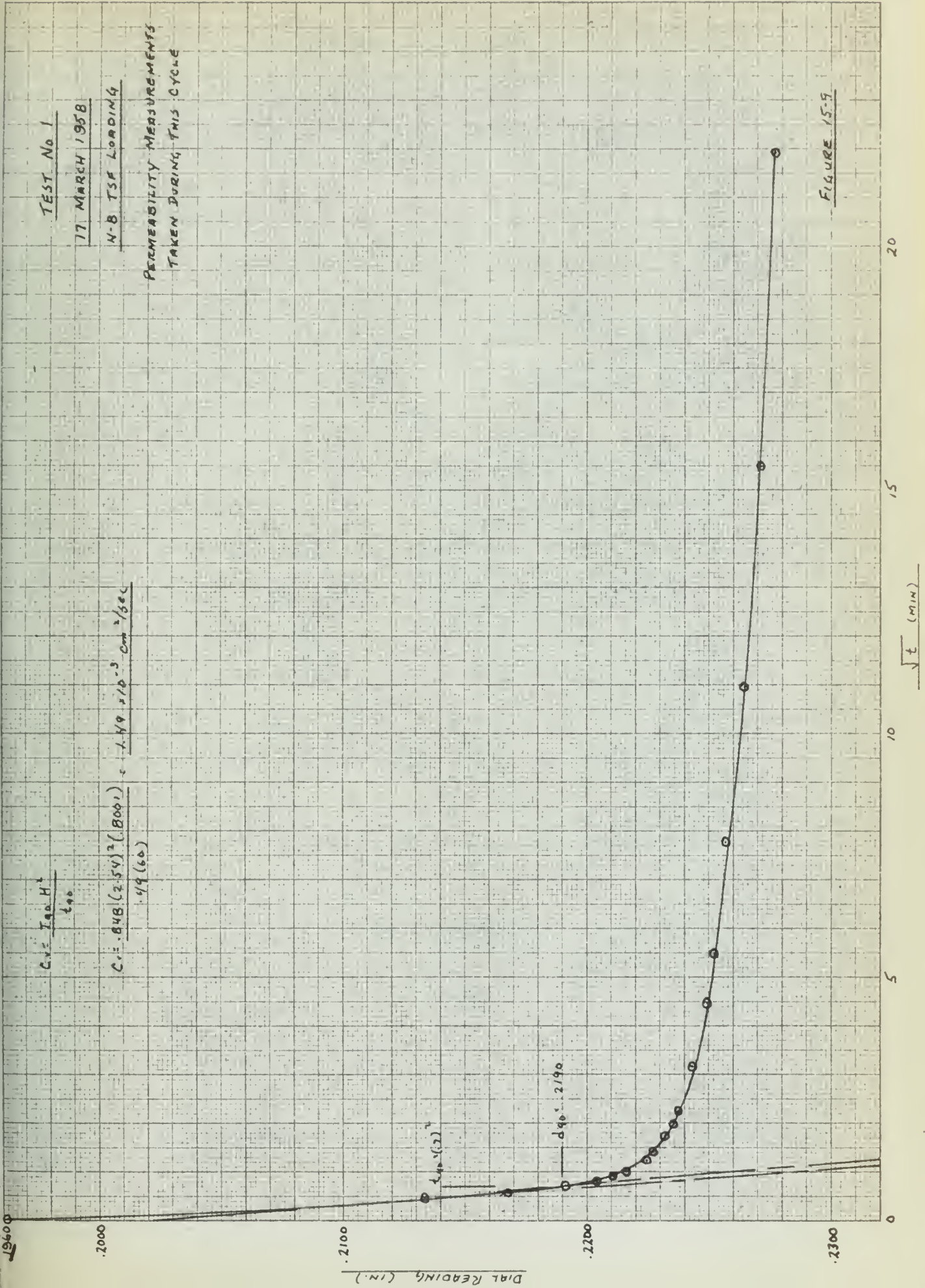


FIGURE 15-9



### C. TESTS NO. 2 and 3 - TIME DEPENDENT LOADING

Test Data in graphical form is presented in Figure 17.

#### DISCUSSION:

The rate of application of load in the majority of increments was such that the consolidation process was essentially concurrent with load application. The curves developed show the same shape and range of variation for each test.

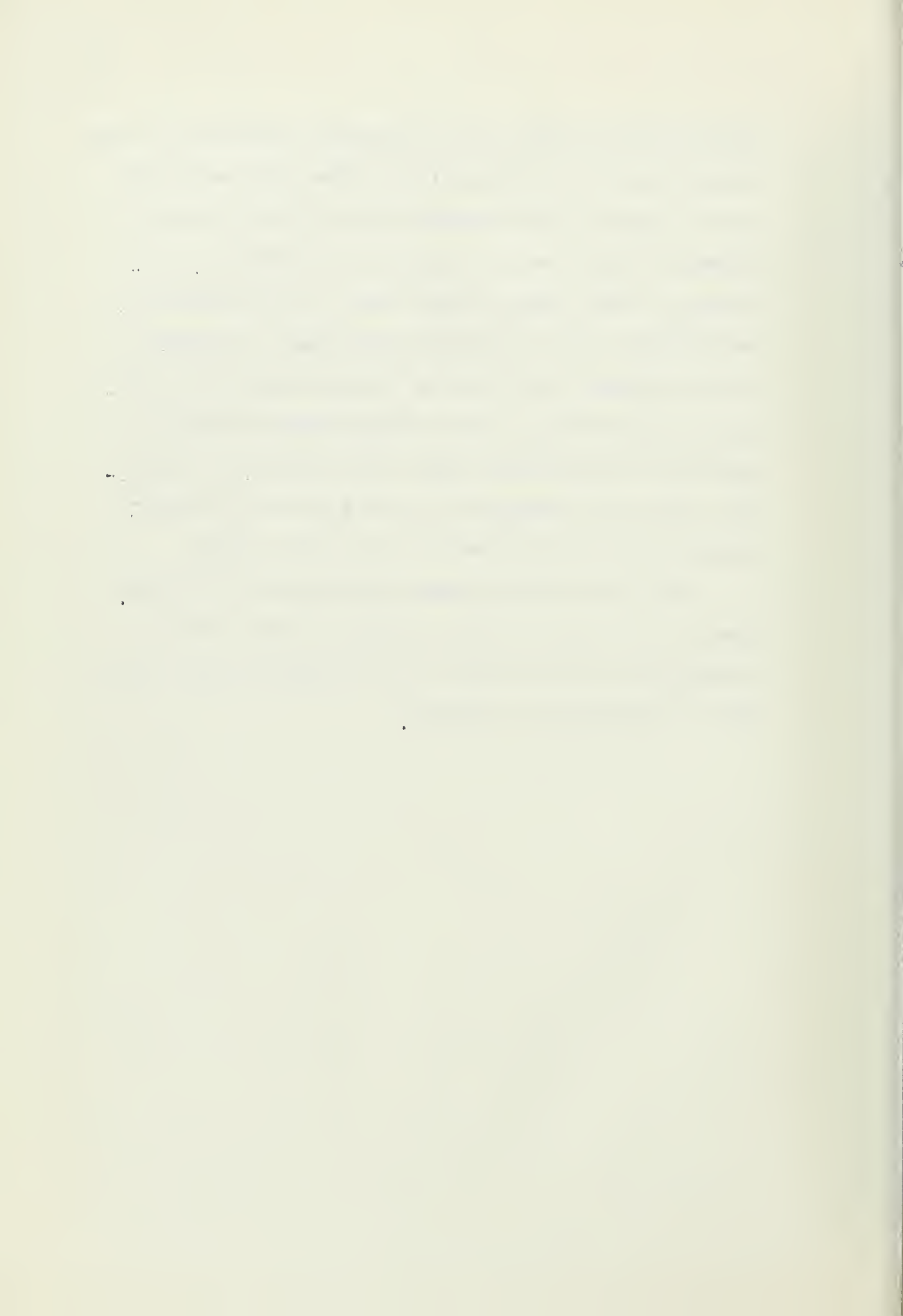
The increase in the permeability of the sample, in the later stages of the consolidation process, is a phenomenon which appears to offer a subject for future study. This increase is not predictable, nor is it always present. It would appear that, at some stage of the plastic range, there is an internal adjustment of pore-channel "effective" areas, which causes scattered increases and decreases in the permeability. The effect is such that it has been termed the "yo-yo effect". The only reasonable hypotheses proposed at the present time are:

- (1) That dissolved gases in the permeant (ie. water in these tests) are condensing and providing an increase in flow volume, which is measurable on the permeameter.
- (2) That the ionically bound water "hull" which restricts the flow of the permeant during the primary



consolidation period, is, by pressure adjustment, being sheared from the clay particles, thus increasing flow by the volume of the sheared hull and the increased volume of flow thru the enlarged pore-channel. Decrease in flow could be the result of structural rearrangement, due to particles shifting, in response to the pressure void left by the shearing of the compressed water hull. The increased stress on the particles, which would cause such shifting, is available from the dissipation of the structural pseudo-hydrostatic-excess pressure of the water hull.

(3) That errors in gauge readings have occurred. Due to the cumulative type readings taken, and the repetition of this effect, it is considered that errors due to (3) above are minimal.





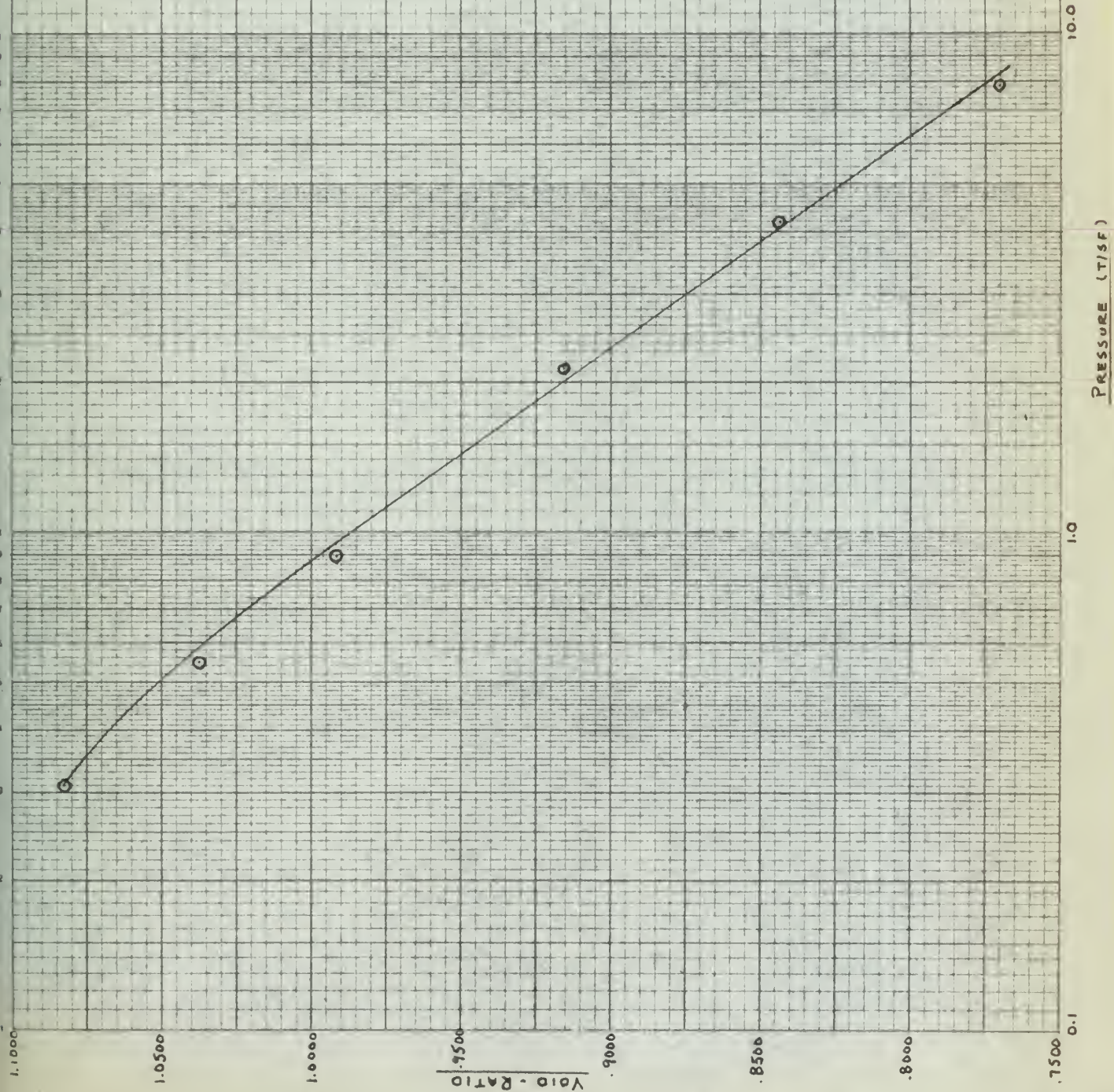
TEST No. 2

VOID RATIO VS LOG PRESSURE

UNDERS

TIME-DEPENDENT LOADING

FIGURE 16-1







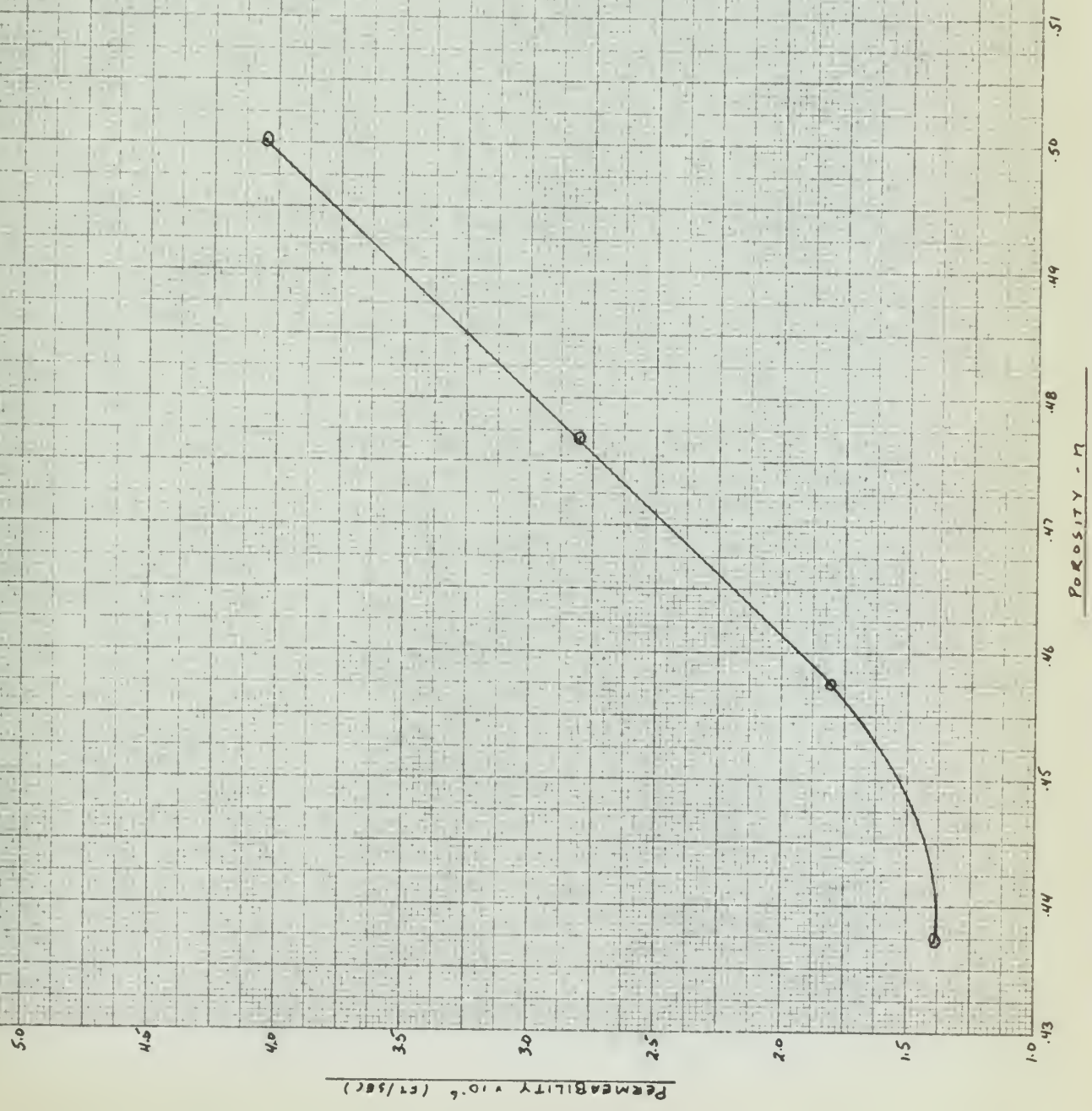
TEST No 2

PERMEABILITY VS POROSITY

UNDER

TIME-DEPENDENT LOADING

FIGURE 16-2







TEST No. 2

PERMEABILITY VS POROSITY

RANGE OF VARIATION UNDER

TIME-DEPENDENT LOADING

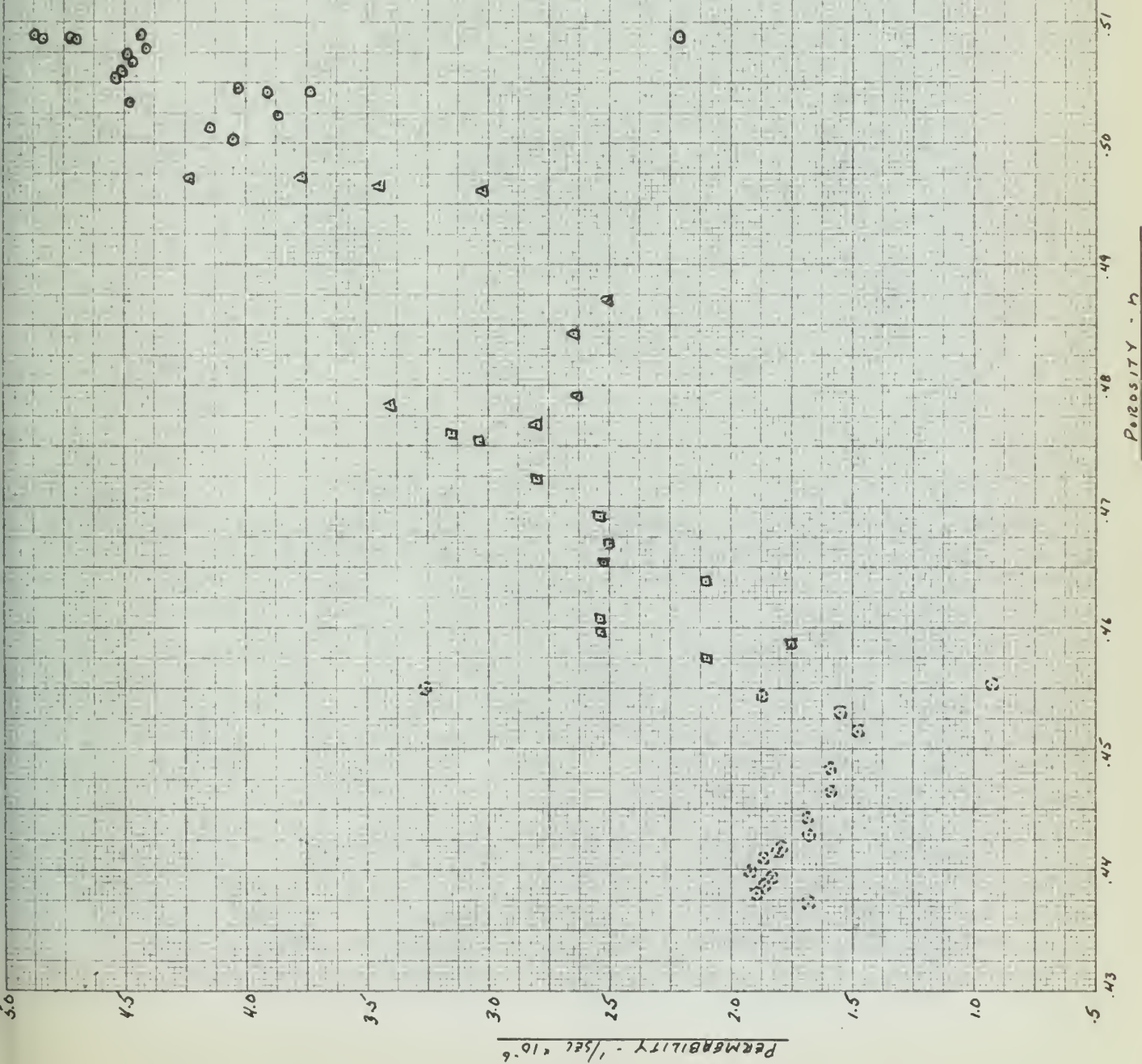
O - 1/2-1 TSF LOADING

Δ - 1-2 TSF LOADING

□ - 2-4 TSF LOADING

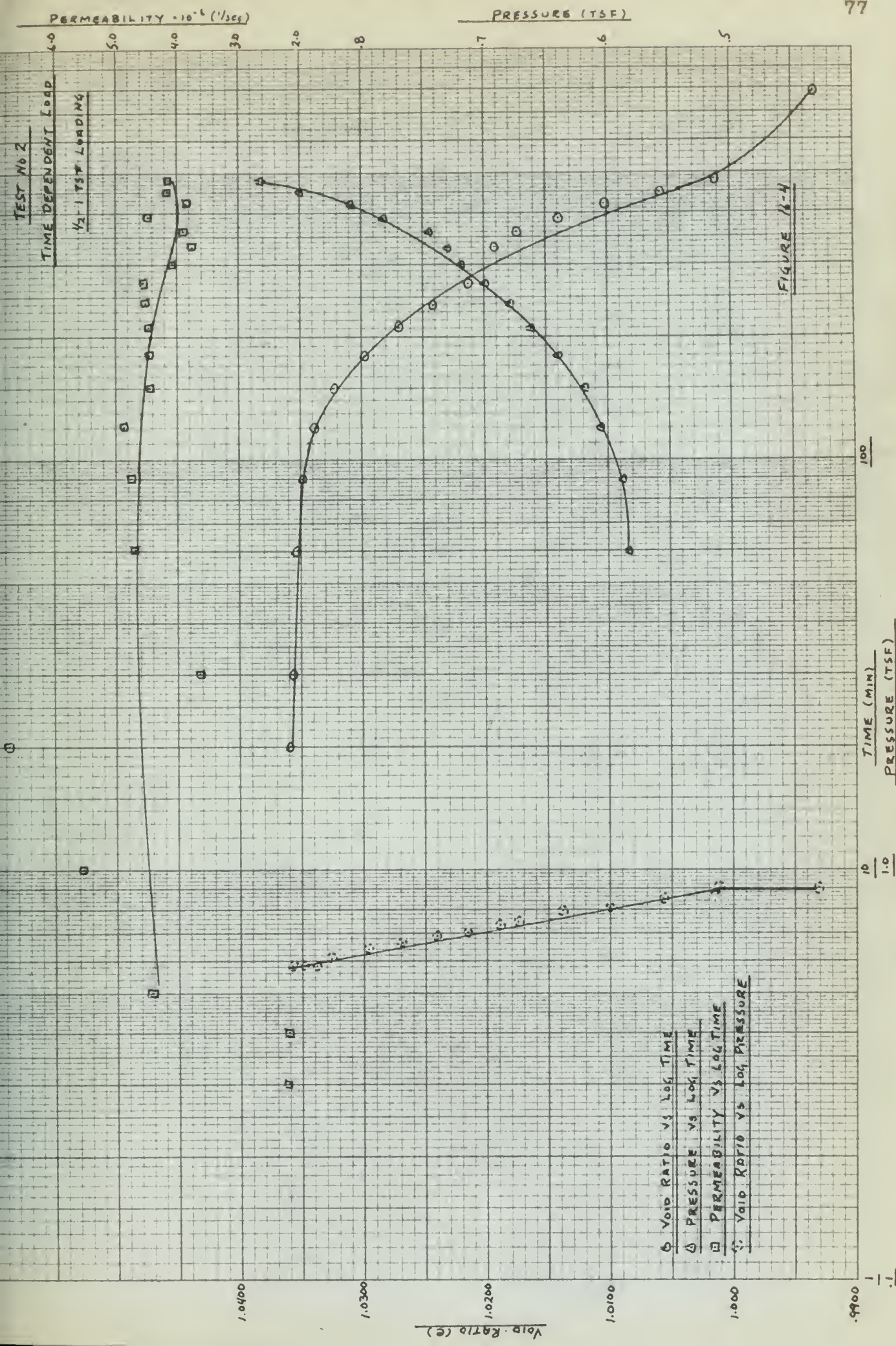
◇ - 4-8 TSF LOADING

FIGURE 16-3













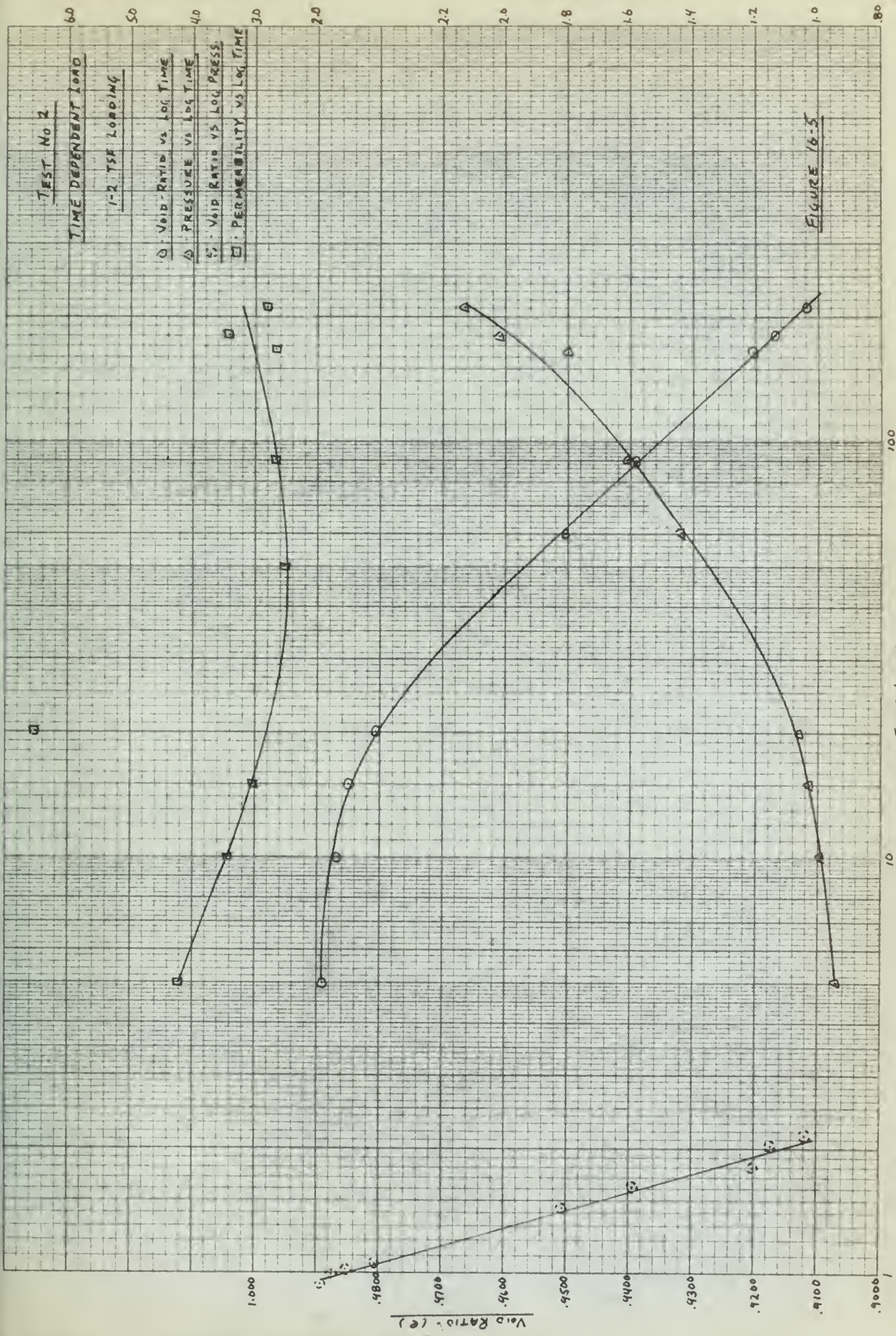
TEST No 2

TIME DEPENDENT LOAD

1-2 TSF LOADING

- VOID RATIO VS LOG TIME
- △ PRESSURE VS LOG TIME
- VOID RATIO VS LOG PRESS.
- PERMEABILITY VS LOG TIME

FIGURE 16-5



TIME (MIN.)  
PRESSURE (TSF)





PERMEABILITY =  $10^{-6}$  (FT/SEC)

PRESSURE (TSF)

TEST No 2

TIME DEPENDENT LABO

2.4 TSF LOADING

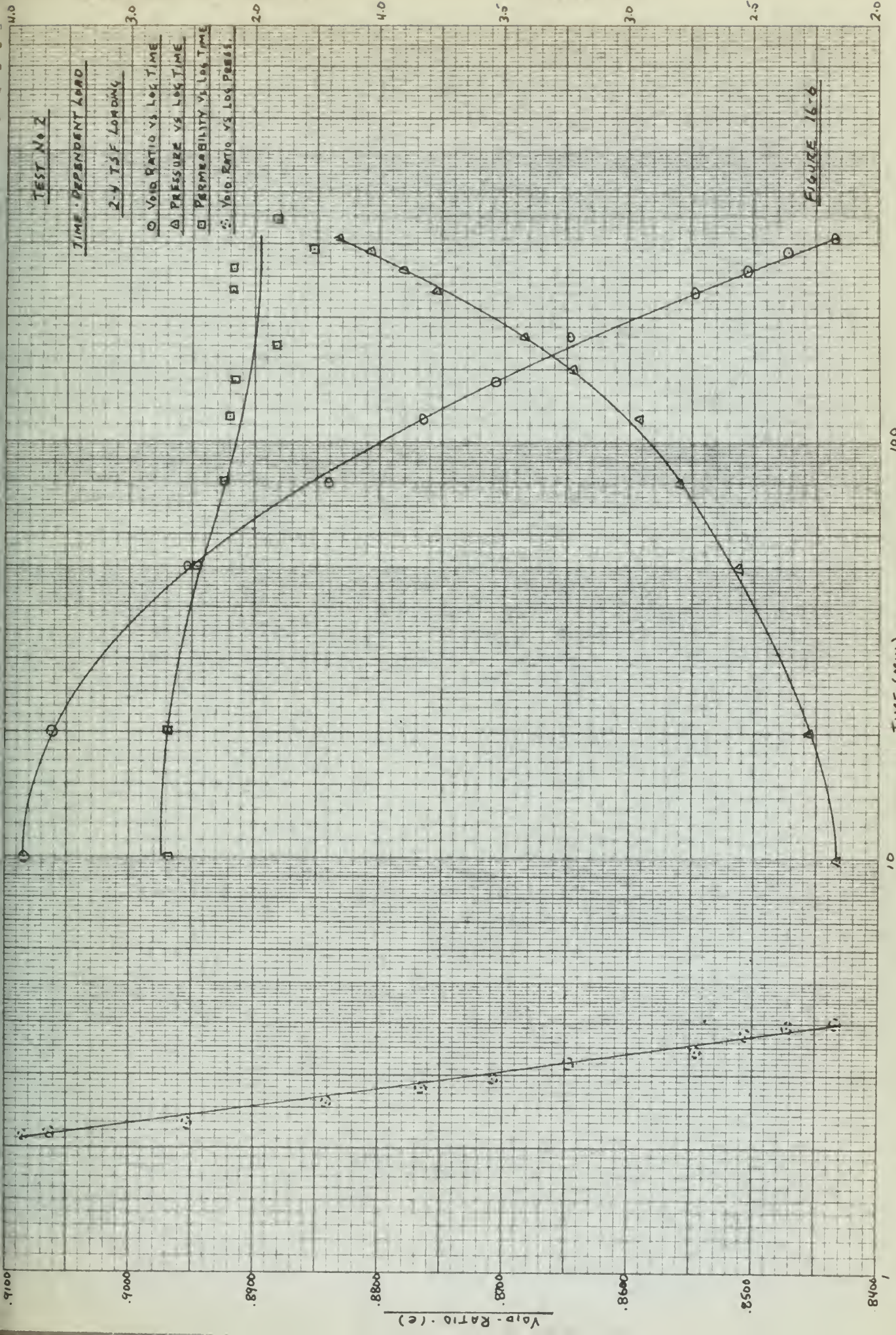
○ VOID RATIO VS LOG TIME

△ PRESSURE VS LOG TIME

□ PERMEABILITY VS LOG TIME

○ VOID RATIO VS LOG PRESS.

FIGURE 16-6



100

10

TIME (MIN)

PRESSURE (TSF)

0.8400

0.8500

0.8600

0.8700

0.8800

0.8900

0.9000

0.9100

Void - Ratio - (e)





PERMEABILITY =  $10^{-6}$  (57/350)

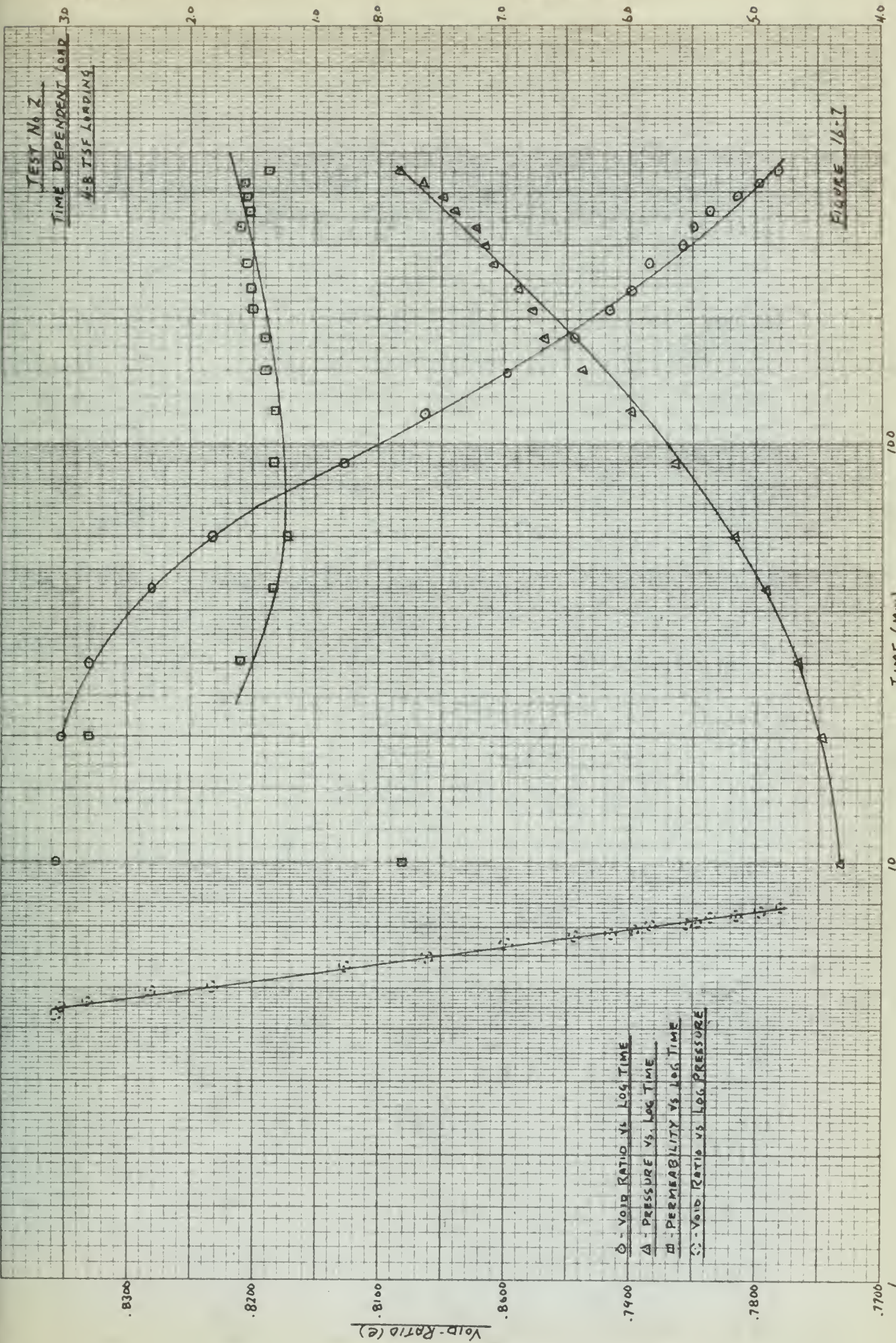
PRESSURE (TSF)

TEST No. 2

TIME DEPENDENT LOAD

4.8 TSF LOADING

FIGURE 16-7



TIME (MIN)

PRESSURE (TSF)

Void Ratio (e)

○ - VOID RATIO VS. LOG TIME

△ - PRESSURE VS. LOG TIME

□ - PERMEABILITY VS. LOG TIME

○ - VOID RATIO VS. LOG PRESSURE





PERMEABILITY =  $10^{-6}$  (FT/SEC)

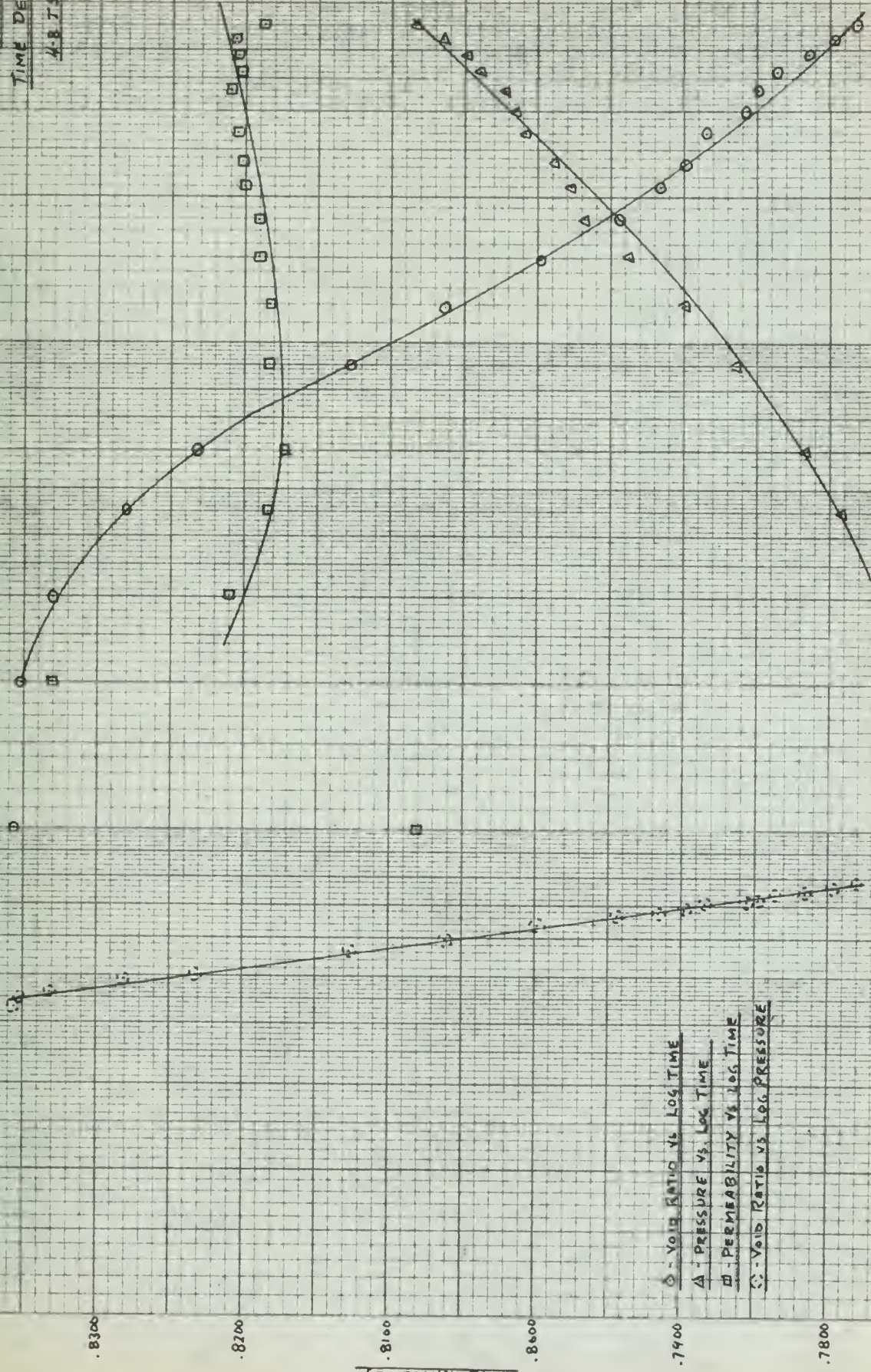
PRESSURE (TSF)

TEST No. 2

TIME DEPENDENT LOAD

4.8 TSF LOADING

FIGURE 16-7



○ - VOID RATIO VS LOG TIME

△ - PRESSURE VS LOG TIME

□ - PERMEABILITY VS LOG TIME

○ - VOID RATIO VS LOG PRESSURE

TIME (MIN)

PRESSURE (TSF)





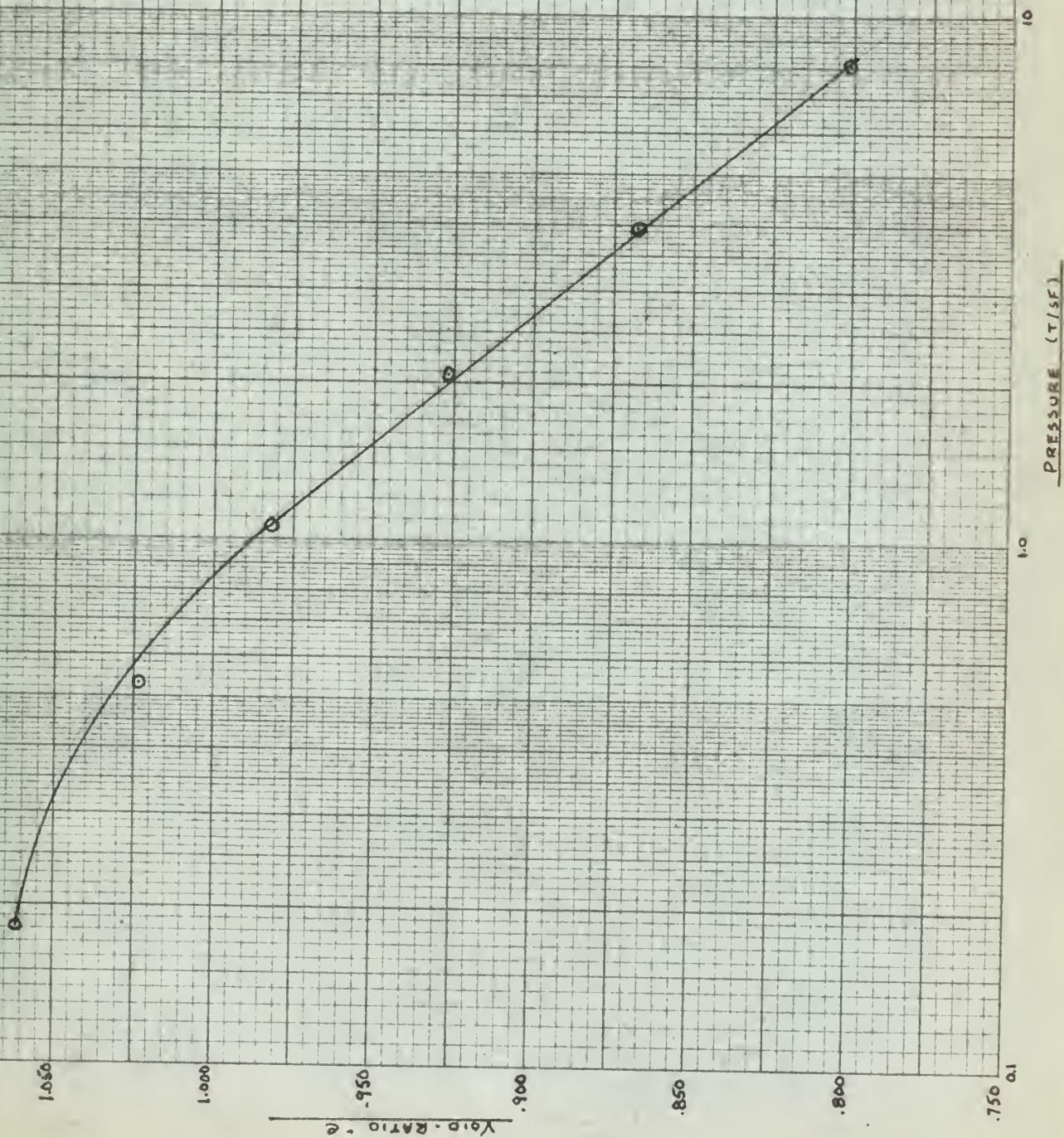
TEST No 3

VOID RATIO VS. LOG PRESSURE

NUMBER

TIME-DEPENDENT LOADING

FIGURE 17-1







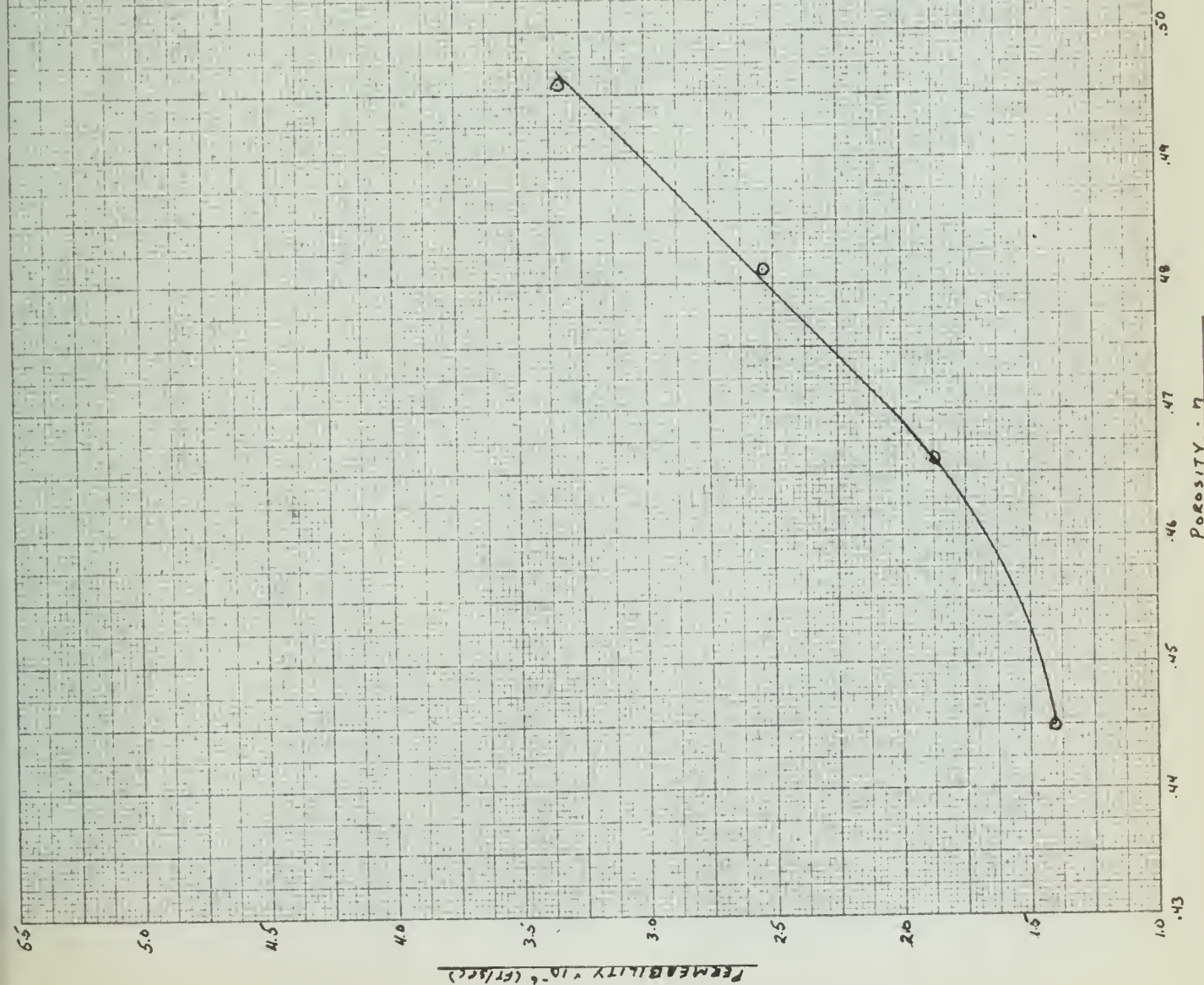
TEST No. 3

PERMEABILITY VS POROSITY

UNDER

TIME-DEPENDENT LOADING

FIGURE 17-2







TEST No. 3

PERMEABILITY VS POROSITY

RANGE OF VARIATION UNDER

TIME-DEPENDENT LOADING

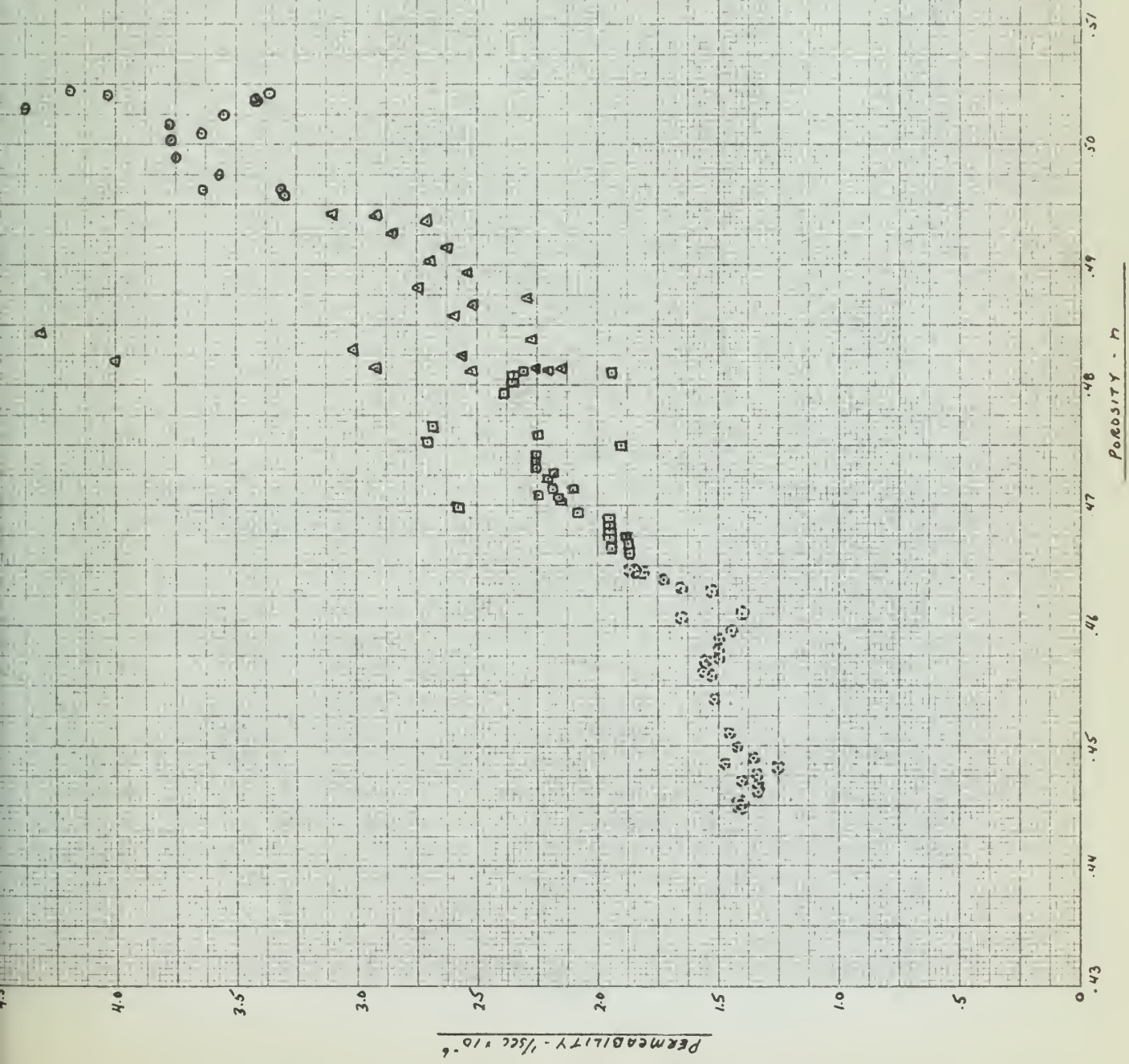
○ - 1/2-1 TSF LOADING

△ - 1-2 TSF LOADING

□ - 2-4 TSF LOADING

⊞ - 4-8 TSF LOADING

FIGURE 17-3







PERMEABILITY  $\cdot 10^{-6}$  (FI/SEC)

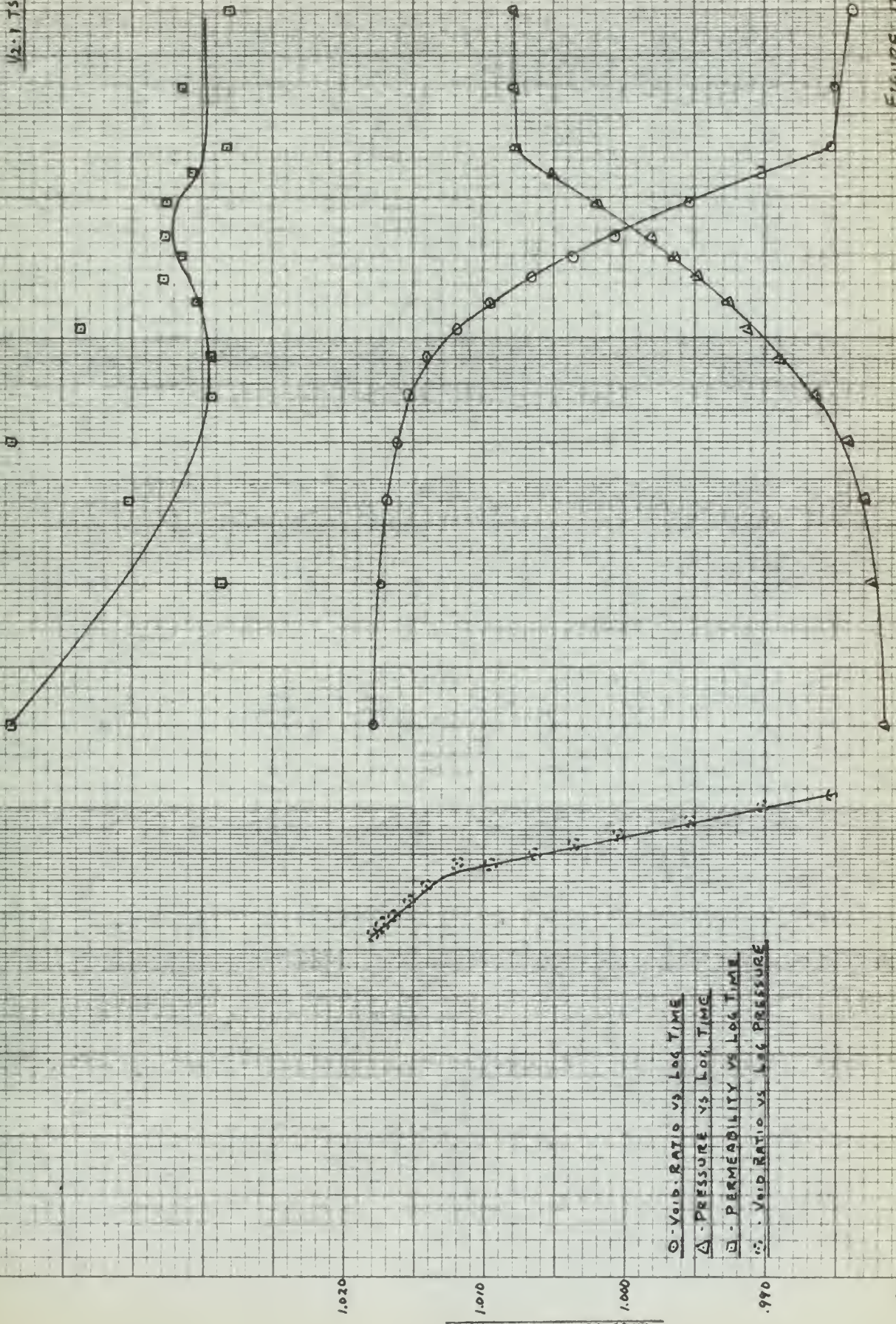
PRESSURE (TSF)

TEST No. 3

TIME DEPENDENT LOAD

12.1 TSF LOADING

FIGURE 17.4



100

1.0

TIME (MIN.)

PRESSURE (TSF)

10

1

Void Ratio - e





PERMEABILITY  $10^{-6}$  (Ft/Sec)

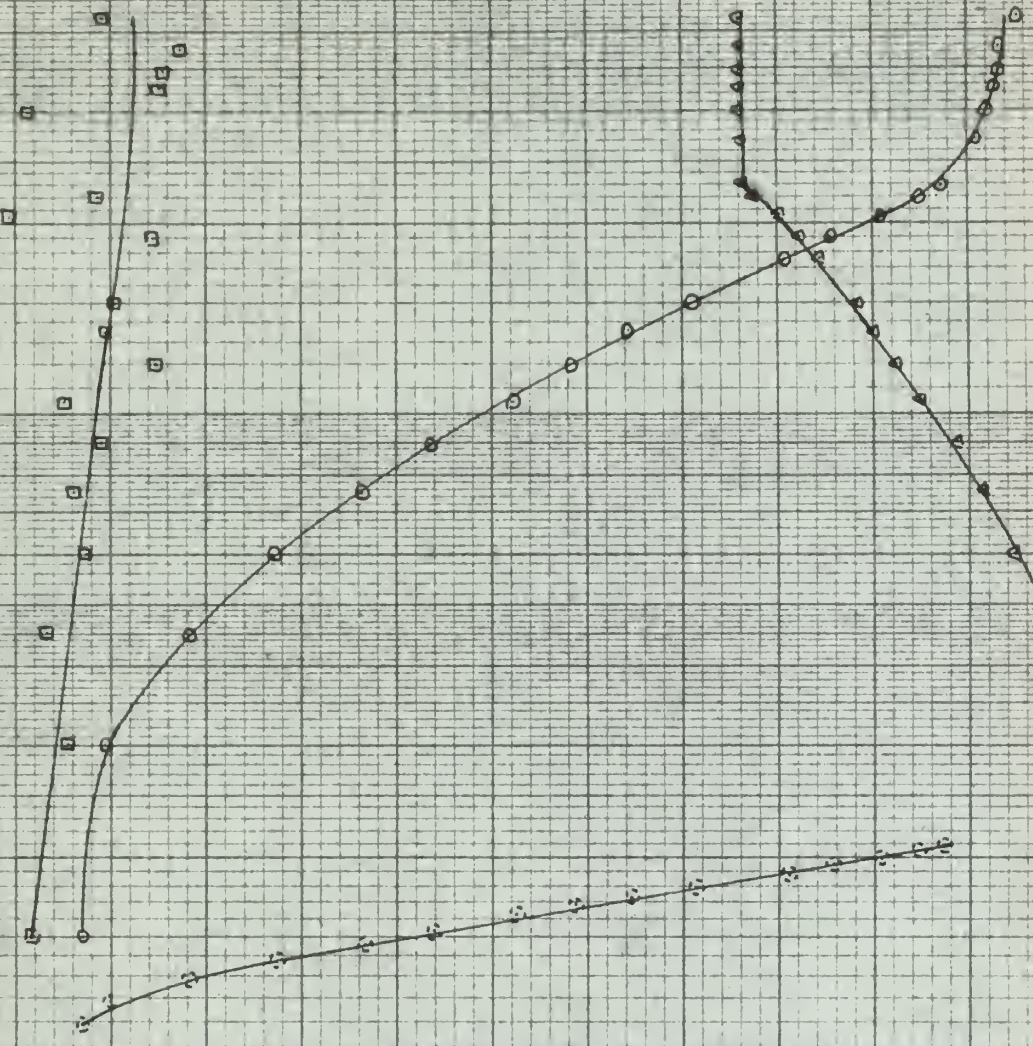
PRESSURE (TSF)

TEST No. 3

TIME-DEPENDENT LOAD

1.2 TSF LOADING

FIGURE 17-5



○ Void Ratio vs Log Time

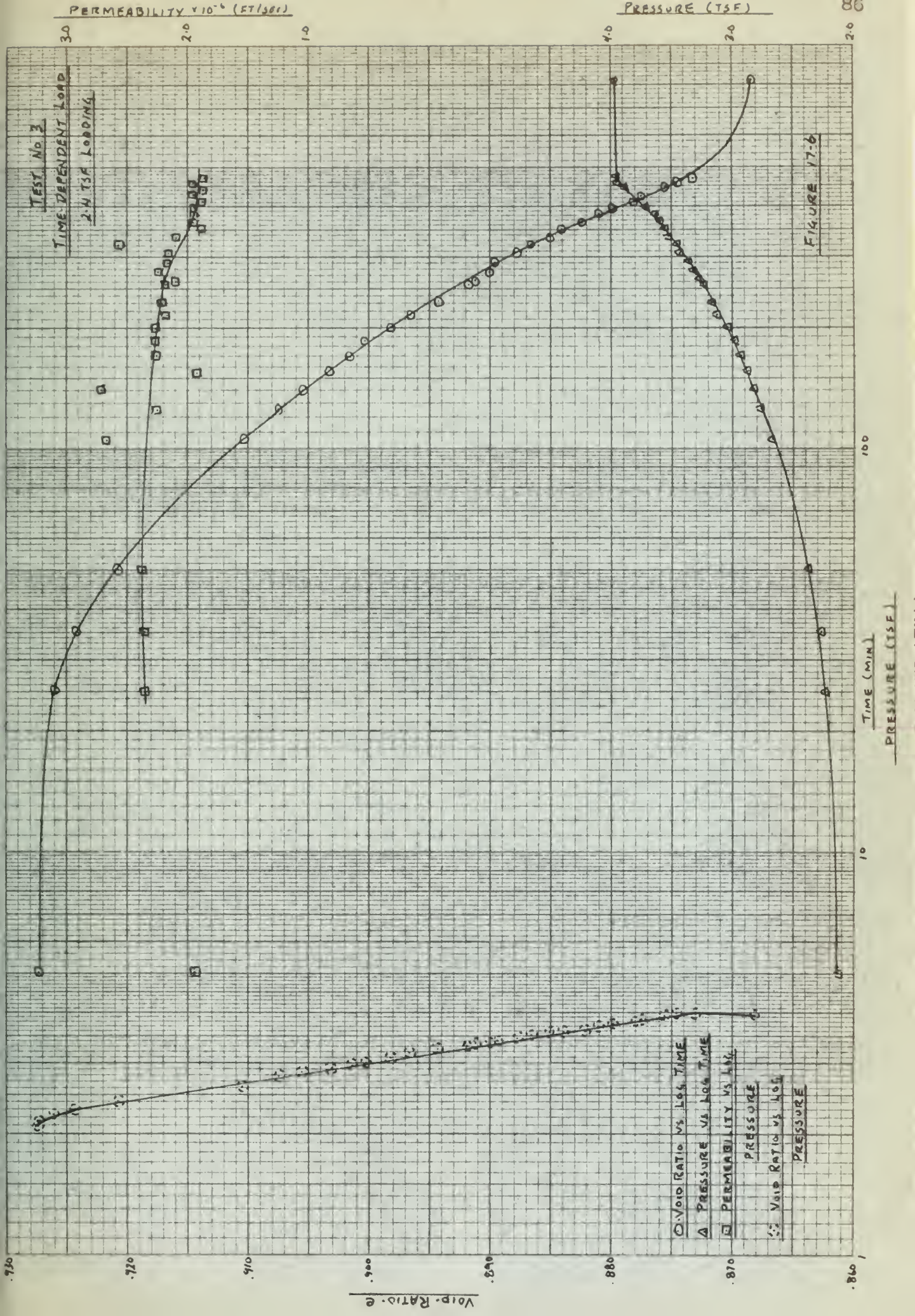
△ Pressure vs Log Time

□ Permeability vs Log Time

△ Void Ratio vs Log Pressure

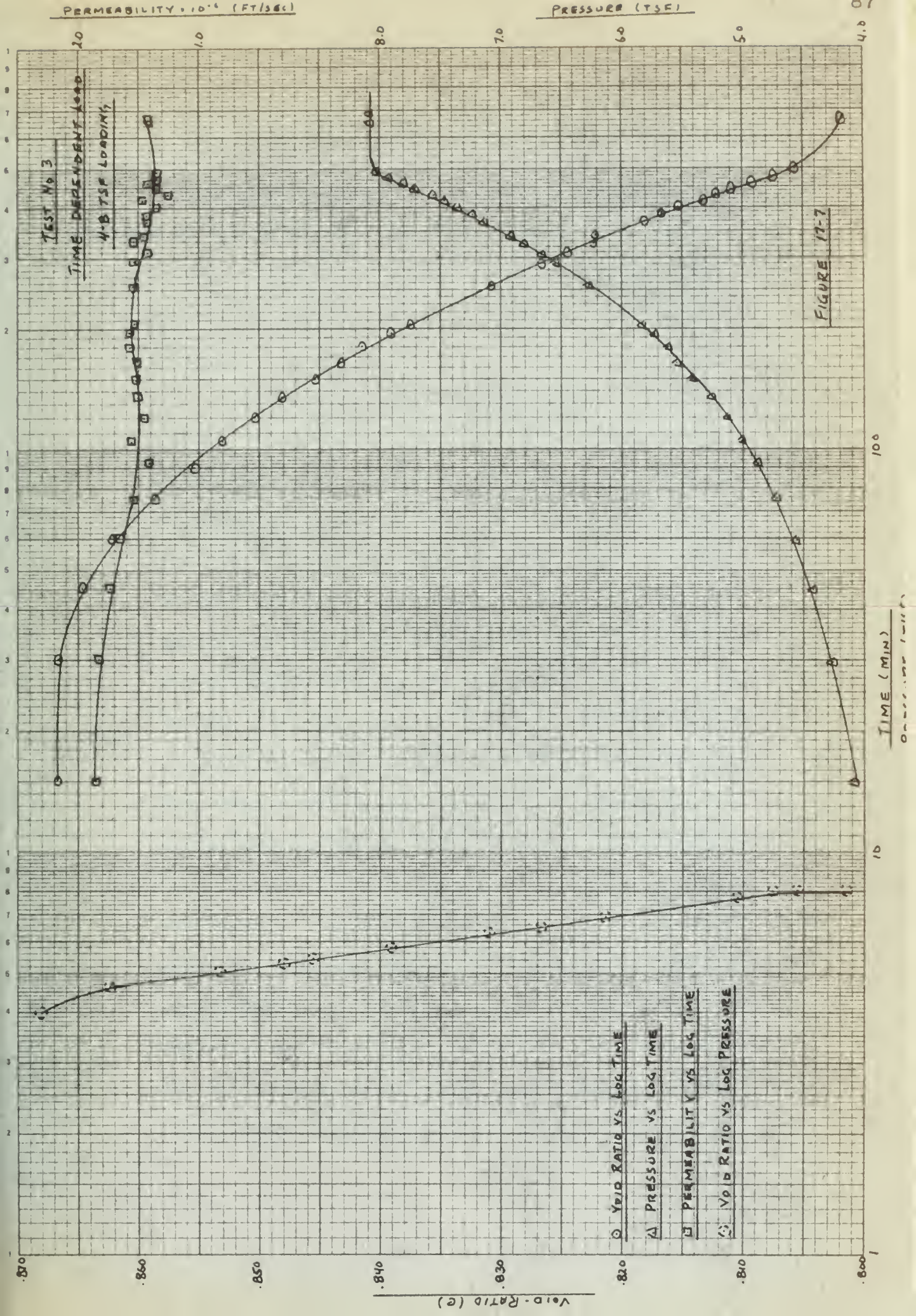
















#### D. TESTS NO. 4 - PSEUDO TIME-DEPENDENT LOADING

Test Data in graphical form is presented in Figure 18. Although it was hoped that another test of this nature could be conducted, failure of a casting in the pressure line from the bellows to the guage system precluded conducting it.

#### DISCUSSION:

The influence of the magnitude of the loading increment is quite apparent in data developed by this test. The deviation from standard load increments does not unduly affect the  $c$ -log  $P$  curve but it is in the  $k$ - $n$  relationship that the effect is most apparent and requires detailed analysis. As may be seen from a study of Figure 17, the linear relationship between the permeability and the porosity is not valid in the  $n \approx n_0$  region. It was therefore decided to utilize test 4, primarily to investigate the consolidation process in this area. The use of  $\frac{1}{2}$  ton increments of loading, shows the permeability as a linear function of the porosity up to the 6-7 TSF range. Comparing this with Figure 17, it is noted that the straight line relationship persisted only to the 4 TSF range, in Tests No. 2 and 3. This variance can only be reasonably attributable to the influence of the loading increments. It is suggested that the instantaneous application of a major portion of the





total load in each series of tests (i.e. 4TSF increments in Tests No. 2 and 3; 9 TSF in Test No. 4) causes a massive structural rearrangement which takes place in a very short time interval. The use of small increments in the early portions of both series of tests produces a gradual structural rearrangement which takes place during a much longer time interval. A comparison of the relative curve shapes at 7 TSF in each series of tests shows the effect of this load application variance. In Tests 2 and 3 the  $k$ - $n$  curve in this region is definitely exponential, whereas in Test 4 it approaches linearity

A pertinent question at this point is whether the linear relationship between  $k$  and  $n$  would continue through additional small load increment cycles until such time as a large load is applied, or whether, at some point, the permeability will asymptotically approach a condition of constancy over a large change in porosity until shear failure occurs. It is hypothesized, from the limited test data available, that the latter will occur. The physical phenomenon involved would indicate that the gradual rearrangement of structure induced by small loading increments produces a net reduction in pore-channel effective area, despite the shearing of bound water previously



discussed. In effect, the amount of shearing occurring, under small load increments, is not sufficient to retain the initial effective area and, thus, permeability decreases at a linear rate with the porosity. If however we consider the application of a large load increment, the shearing of the bound water is of such magnitude that the effective pore-channel area is reduced at a much lower rate than the sample is compressing. In effect we have retained a great portion of the effective channel area despite a reduction in porosity.

The extension of this phenomenon to include all loading, up to the point where plastic flow will occur, is of course a large jump in the process of research investigation, and is subject to justifiable criticism. However, it is proposed in the hope that future investigators in this area, may study the problem in detail and by such study arrive at a rational analysis of the cause of the phenomenon.

The importance of detailed analysis of the  $k$ - $n$  relationship is realized when one considers that the accuracy of time-settlement predictions, by either the Terzaghi Theory or the Schiffman Extension, depend upon the porosity-permeability relationship, in that the dissipation of hydrostatic excess pressure



is governed by the availability of "effective" pore channels for flow. Since by the hypothesis proposed above, this relationship is controlled not only by the rate of loading but also by the amount of load, it is apparent that further study of this problem is essential to a clearer analysis of the constant permeability over a finite time increment approximation, of the variable permeability condition, utilized by Schiffman.





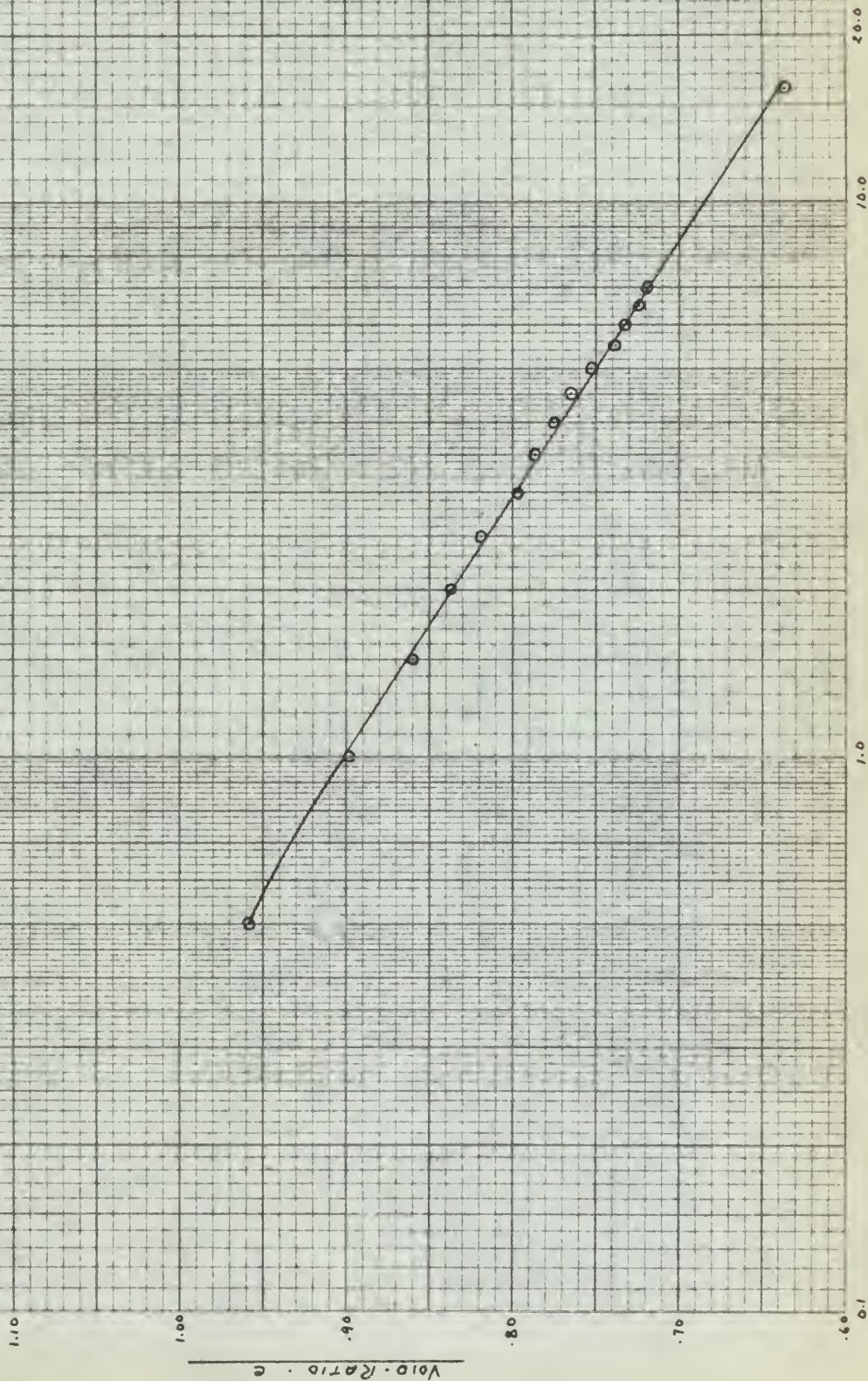
TEST No 2

VOID-RATIO VS LOG PRESSURE

UNDER

PSEUDO-TIME-DEPENDENT LOADING

FIGURE 18-1



PRESSURE ( $T_{sf}$ )





TEST NO 4

PERMEABILITY VS POROSITY

UNDER

PSEUDO-TIME-DEPENDENT LOADING

FIGURE 1B-2

4.0

3.5

3.0

2.5

2.0

1.5

1.0

0.5

0

PERMEABILITY -  $1/\text{sec} \times 10^{-6} - k$

.38

.39

.40

.41

.42

.43

.44

.45

.46

.47

.48

.49

.50

.51

.52

.53

.54

.55

.56

.57

.58

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.61

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3.00

3.01

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3.65

3.66

3.67

3.68





## PART VI.

CONCLUSIONS

1. The assumption of linear variation of permeability and porosity as proposed by Schmid, and utilized by Schiffman in developing his Extension to the Theory of Consolidation is valid for construction type loading (ie. small loads applied over long time periods in repetitive sequence).
2. The assumption of linear variation of permeability and porosity is not valid under conditions of large absolute load increments applied during a short time interval.
3. It is hypothesized that an exponential relationship exists between permeability and porosity for the conditions stated in 2 above. The value of the exponential relationship is a function not only of the rate of loading, but also of the magnitude of the load increment and it is suggested that such an effect is caused by the shearing of the water hull from the clay particles under intense densification of structure during a short time period. It is strongly recommended that further investigation be conducted at higher load increments to test the validity of this hypothesis.



4. It is further suggested that the permeability variance, previously referred to as the "yo-yo" effect, requires that, for the finite increment approximation in the Variable Permeability case, developed by Schiffman, the increments must be kept as small as possible. This limits the general usefulness of the approximation, since practical laboratory techniques preclude constant attendance. As noted by Schiffman (9) the degree of accuracy is a function of the time increments utilized. Since the variance of permeability is neither predictable nor always present, the use of the approximation technique for the solution of the variable permeability problem requires further investigation and analysis before a definitive conclusion can be drawn.
5. No conclusion is drawn relative to the consolidation-permeability-time relationship since fitting procedures for comparison of test curves and the theoretical curves developed by Schiffman, have not been established. It is inferred from the permeability-porosity relationships, developed during this study, that the rate of loading and amount of load will also govern the solution of this problem.



## PART VII

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## APPENDIX A

RAW DATA

TEST NO. 1









TEST No. 1													2
TIME	Q t	PRESSURE	DIAL	DIAL IN	HT	VOL	Vs	$C = \frac{V_s}{V_s - 1}$	$n = C / (C - 1)$	PERM. GAGE	Q - cc	K - $\frac{1}{\text{sec}} \times 10^{-6}$	
141"	0 sec	75	5-19.6	11.98	9022	4 425	2.37	9.114	40.5	62			
	10		6-14	12.11	8966	4 422		9.16	41.4	62			
	25		21	12.14	8944	4 419		9.198	41.7	61			
	30		2	12.17	8935	4 417	1.412	9.24	42.24	61			
	40		24	12.21	8941	4 415		9.27	42.72	61			
	50		31	12.31	8924	4 414		9.317	43.21	61			
	60		34	12.34	8925	4 412		9.348	43.68	61			
	1 1/2 m		39	12.39	8921	4 410		9.416	44.26	61			
	2		43	12.44	8917	4 408		9.481	44.83	61		1.06	
	3		48	12.48	8912	4 405		9.544	45.4	61		2.06	
	4		52	12.52	8908	4 402		9.606	46.07	61		3.14	
	5		54	12.54	8906	4 402		9.668	46.74	61		3.14	
	10		61	12.61	8909	4 399		9.76	47.6	61		2.77	
	20		67	12.67	8903	4 396		9.853	48.61	61		3.04	
	30		70	12.70	8950	4 394		9.942	49.67	61		3.13	
	60		78	12.78	8942	4 391		10.03	50.74	61		3.13	
151"	120		84	12.84	8936	4 388		10.17	51.9	61		3.21	
161"	200		90	12.90	8940	4 385		10.31	53.1	61		3.51	
221"	400	100	94	12.94	8926	4 383		10.46	54.4	61		3.03	
								10.61	55.7	61			
090"	0 sec	100	6-11.4	13.14	8916	4 378		10.76	57.0	61			
	10		7-60	13.17	8916	4 376		10.91	58.3	61			
	20		93	13.23	8915	4 374		11.06	59.6	61			
	30		116	13.30	8914	4 374		11.21	60.9	61			
	40		131	13.37	8913	4 374		11.36	62.2	61			
	50		142	13.42	8912	4 374		11.51	63.5	61			
	60		150	13.50	8911	4 374		11.66	64.8	61			
	1 1/2 m		166	13.56	8910	4 374		11.81	66.1	61			
	2		174	13.64	8909	4 374		11.96	67.4	61			
	3		181	13.71	8908	4 374		12.11	68.7	61			
	4		185	13.78	8907	4 374		12.26	70.0	61			
	5		188	13.85	8906	4 374		12.41	71.3	61			
	10		194	13.94	8905	4 374		12.56	72.6	61			
	20		197	14.01	8904	4 374		12.71	73.9	61			
	30		202	14.08	8903	4 374		12.86	75.2	61			
	60		207	14.17	8902	4 374		13.01	76.5	61			
1000	120		214	14.26	8901	4 374		13.16	77.8	61			
1300	240		220	14.34	8900	4 374		13.31	79.1	61			
1650	470	200	225	14.43	8899	4 374		13.46	80.4	61			
								13.61	81.7	61			
1230	0 sec	200	8	14.45	8898	4 374		13.76	83.0	61			
	10		196	14.56	8897	4 374		13.91	84.3	61			
	25		24	14.64	8896	4 374		14.06	85.6	61			
	30		254	14.71	8895	4 374		14.21	86.9	61			
	40		63	14.83	8894	4 374		14.36	88.2	61			
	50		77	14.93	8893	4 374		14.51	89.5	61			
	60		83	15.03	8892	4 374		14.66	90.8	61			
	1 1/2 m		93	15.14	8891	4 374		14.81	92.1	61			
	2		103	15.26	8890	4 374		14.96	93.4	61			
	3		108	15.36	8889	4 374		15.11	94.7	61			
	4		108	15.46	8888	4 374		15.26	96.0	61			
	5		114	15.54	8887	4 374		15.41	97.3	61			
	10		114	15.64	8886	4 374		15.56	98.6	61			
	20		114	15.74	8885	4 374		15.71	99.9	61			
	30		121	15.81	8884	4 374		15.86	101.2	61			
	60		126	15.91	8883	4 374		16.01	102.5	61			
1320	120		131	16.01	8882	4 374		16.16	103.8	61			
1330	240		136	16.11	8881	4 374		16.31	105.1	61			
1630	400	400	144	16.24	8880	4 374		16.46	106.4	61			
2020	400	400	144	16.34	8879	4 374		16.61	107.7	61			
								16.76	109.0	61			
								16.91	110.3	61			
								17.06	111.6	61			
								17.21	112.9	61			
								17.36	114.2	61			
								17.51	115.5	61			
								17.66	116.8	61			
								17.81	118.1	61			
								17.96	119.4	61			
								18.11	120.7	61			
								18.26	122.0	61			
								18.41	123.3	61			
								18.56	124.6	61			
								18.71	125.9	61			
								18.86	127.2	61			
								19.01	128.5	61			
								19.16	129.8	61			
								19.31	131.1	61			
								19.46	132.4	61			
								19.61	133.7	61			
								19.76	135.0	61			
								19.91	136.3	61			
								20.06	137.6	61			
								20.21	138.9	61			
								20.36	140.2	61			
								20.51	141.5	61			
								20.66	142.8	61			
								20.81	144.1	61			
								20.96	145.4	61			
								21.11	146.7	61			
								21.26	148.0	61			
								21.41	149.3	61			
								21.56	150.6	61			
								21.71	151.9	61			
								21.86	153.2	61			
								22.01	154.5	61			
								22.16	155.8	61			
								22.31	157.1	61			
								22.46	158.4	61			
								22.61	159.7	61			
								22.76	161.0	61			
								22.91	162.3	61			
								23.06	163.6	61			
								23.21	164.9	61			
								23.36	166.2	61			
								23.51	167.5	61			
								23.66	168.8	61			
								23.81	170.1	61			
								23.96	171.4	61			
								24.11	172.7	61			
								24.26	174.0	61			
								24.41	175.3	61			
								24.56	176.6	61			
								24.71	177.9	61			
								24.86	179.2	61			
								25.01	180.5	61			
								25.16	181.8	61			
								25.31	183.1	61			
								25.46	184.4	61			
								25.61	185.7	61			
								25.76	187.0	61			
								25.91	188.3	61			
								26.06	189.6	61			
								26.21	190.9	61			
								26.36	192.2	61			
								26.51	193.5	61			
								26.66	194.8	61			
								26.81	196.1	61			
								26.96	197.4	61			
								27.11	198.7	61			
								27.26	200.0	61			
								27.41	201.3	61			
								27.56	202.6	61			
								27.71	203.9	61			
								27.86	205.2	61			
								28.01	206.5	61			
								28.16	207.8	61			
								28.31	209.1	61			
								28.46	210.4	61			
								28.61	211.7	61			
								28.76	213.0	61			
								28.91	214.3	61			
								29.06	215.6	61			
								29.21	216.9	61			
								29.36	218.2	61			
								29.51	219.5	61			
								29.66	220.8	61			
								29.81	222.1	61			
								29.96	223.4	61			
								30.11	224.7	61			
								30.26	226.0	61			



TEST No 1												
TIME	Δt	PRESSURE	DIAL	DIAL IN	HT	VOL	Vs	e: $\frac{V_s}{V_0 - 1}$	H: $\frac{e}{1+e}$	PERM GAGE	ΔQ - cc	K: $\frac{1}{300 \times 10}$
1415	0 SEC	400	7-16.1	.1961	.0251	4.555	2.37	.7112	.415	1.20		
	10		10 13.3	.2122	.0287	3.971		.6735	.402	.20		
	20		16.8	.2162	.0652	3.174	±	.6735	.402	.7		
	30		11	.2171	.0624	3.742	Vs	.6635	.3479	.6		
	40		11 04	.2254	.0646	3.926		.6610	.3479	.1		
	50		11	.2211	.0647	3.922		.6573	.3473	.1		
	1/2 MIN		16	.2216	.0647	3.920		.6545	.3470	.58		
	2		27	.2224	.1946	2.925		.6523	.3462	.57		
	3		32	.2232	.1948	2.922		.6500	.3457	.56		
	4		35	.2235	.1965	2.921		.6484	.3456	.57		.57
5	37	.2237	.1977	2.920		.6472	.3454	.59		.61		
10	43	.2243	.1977	3.717		.6452	.3450	.65		.111		
20	49	.2247	.1971	3.914		.6427	.3445	.79		.127		
30	52	.2252	.1964	3.912		.6402	.3442	.73		.127		
60	57	.2257	.1963	3.715		.6300	.3439	.74		.125		
1515	120		64	.2264	.1950	3.906		.6443	.3433	.83	.56	.121
1615	140		71	.2271	.1947	3.923		.6410	.3424	.42	.83	.131
2215	480	800	77	.2277	.1943	3.900		.6458	.3423	.816	.391	.151

SAMPLE DATA

SPECIFIC GRAVITY 2.59  
INITIAL HT OF SAMPLE 1.0000 IN.  
FINAL HT OF SAMPLE 7943 IN  
CROSS SECTIONAL AREA 49681 IN<sup>2</sup>  
INITIAL MOISTURE CONTENT 42 %  
FINAL MOISTURE CONTENT 31.7%  
WT of SOLIDS 1625 grms  
VOL of SOLIDS 2365 IN<sup>3</sup>





## APPENDIX B

RAW DATA

TEST NO. 2



TEST NO 2

TIME	$\Delta t$ MIN	LOMO - PSI	LOMO - TSF	DIAL	DIAL - IN	HT.	VOL. = V	$V_s$	$e = \frac{V}{V_s} - 1$	$m = \frac{e}{1+e}$	PERM. GAGE	$\Delta Q - CC$	K - 1/1 sec
1015	0	0	.0166	0 - 0.0	0.0000	1.0000	4.9087	2.29	2.1431 - 1	.5333			
1024	9	.050	.0233	0.1	.0001	.9999	4.9082		2.1429	.5333			
1033	9	.070	.0233	0.2	.0002	.9998	4.9077		2.1427	.5333			
1100	45	.09	.0299	0.3	.0003	.9997	4.9072	$\perp = .4366$ $V_s$	2.1424	.5332			
1130	75	.12	.0399	1.0	.0010	.9990	4.9037		2.1409	.5329			
1200	105	.22 + .05	.0899	6.3	.0063	.9937	4.8777		2.1296	.5304			
1230	135	.25	.0899	12.8	.0128	.9872	4.8458		2.1156	.5273			
1300	165	.38	.1431	16.0	.0160	.9840	4.8301		2.1088	.5257			
1330	195	.51 + .08	.1964	3.5	.0235	.9765	4.7923		2.0927	.5231			
1400	225	.63	.2364	4.7	.0247	.9753	4.7874		2.0901	.5215			
1430	255	.85	.3096	8.2	.0282	.9718	4.7702		2.0826	.5198			
1530	315												
1000	0	.85 + .08	.3096	1 - 5.4	.0254	.9756	4.7889	2.29	2.0908 - 1	.5217			
1010	10 sec			6.9	.0264	.9731	4.7762		2.0854	.5204			
1020	20			7.4	.0274	.9726	4.7742		2.0844	.5202			
1035	30			7.5	.0275	.9725	4.7737		2.0841	.5202			
1045	40			7.6	.0276	.9724	4.7732		2.0839	.5201			
1055	50			7.7	.0276	.9723	4.7730		2.0838	.5201			
1105	1.5 MIN			7.7	.0277	.9723	4.7727		2.0837	.5201			
1115	2			7.8	.0278	.9722	4.7722		2.0835	.5200			
1125	3			7.8	.0278	.9722	4.7722		2.0835	.5200			
1135	4			7.8	.0278	.9722	4.7722		2.0835	.5200			
1145	5			7.9	.0279	.9721	4.7717		2.0834	.5199			
1155	10			8.0	.0280	.9720	4.7712		2.0831	.5199			
1205	20	.86	.3130	8.2	.0282	.9718	4.7702		2.0826	.5198			
1215	35	.87 + .12	.3163	8.6	.0286	.9714	4.7683		2.0818	.5196			
1230	45	.93	.3496	9.0	.0290	.9710	4.7663		2.0809	.5194			
1245	105	1.42	.3796	13.5	.0335	.9665	4.7442		2.0713	.5172			
1255	135	1.05	.3894	16.7	.0367	.9643	4.7285		2.0644	.5155			
1305	155	1.47	.3962	18.1	.0381	.9619	4.7216		2.0614	.5148			
1315	180	1.20 + .16	.4328	19.2	.0392	.9608	4.7162		2.0590	.5143			
1325	195	1.23	.4628	2 - 2.2	.0422	.9578	4.7015		2.0536	.5128			
1340	240	1.35	.4945	3.2	.0432	.9568	4.6966		2.0505	.5123			
1350	270	1.37	.4928	5.2	.0452	.9548	4.6824		2.0462	.5112			
1400	300	1.35	.4995	6.1	.0461	.9539	4.6774		2.0423	.5108			
1415	330	1.38	.5044	7.0	.0470	.9530	4.6745		2.0391	.5099			
1430	360	1.42	.5228	7.7	.0477	.9523	4.6706		2.0378	.5095			
1445	390	1.45 + .20	.5494	8.5	.0485	.9515	4.6676		2.0365	.5092			
1455	420	1.50	.5661	9.1	.0491	.9504	4.6583		2.0360 - 1	.5088			
1500				10.0	.0500	.9496							
0910	0	1.50 + .20	.5661	2 - 10.1	.0501	.9498	4.6632	2.29	2.0360 - 1	.5088	1.90	0	4.43 + 10.6
0920	15 sec										1.91	.01	4.43 + 10.6
0930	30										1.92	.01	4.43 + 10.6
0940	45										1.93	.01	4.43 + 10.6
0950	1 1/2 MIN										1.94	.01	4.43 + 10.6
1000	2										1.96	.02	4.43 + 10.6
1010	3										1.99	.03	6.74 + 10.6
1020	4										2.01	.02	2.21 + 10.6
1030	5										2.02	.02	2.21 + 10.6
1040	10										2.07	.04	4.43 + 10.6
1050											2.07	.04	5.54 + 10.6









## TEST No. 2 - (CONT.)

3

TIME	Δt - MIN	LOAD-PSI	LOAD-TSF	DIAL	DIAL - IN	HT.	VOL. = V	V	$V_{1/2} - 1 = C$	$n = C / 1/C$	PERM. GRADE	ΔQ : CC	K - 41/5216
0900	0	12.0 ± .57	4.1858	7-33	.1433	.8567	4.2052	2.29	1.8359-1	.4553	6.55	0	1.80
0916	16	12.4	4.3190	3.4	.1434	.8566	4.2047		1.8357	.4552	.63	.08	0.80
0920	20	12.4	4.4855	3.7	.1437	.8563	4.2033		1.8351	.4550	.63	.28	2.80
0930	30	13.4	4.6520	4.7	.1447	.8553	4.1984		1.8330	.4544	.91	.16	1.60
0945	45	14.2	4.9184	7.0	.1470	.8530	4.1871		1.8280	.4529	1.27	.20	1.33
1000	60	14.9	5.1515	9.3	.1493	.8507	4.1758		1.8231	.4514	1.48	.19	1.21
1030	90	16.3 ± .60	5.6277	14.2	.1542	.8458	4.1517		1.8126	.4483	1.89	.41	1.34
1100	120	17.4	5.9940	17.2	.1572	.8428	4.1370		1.8042	.4463	2.30	.41	1.34
1130	150	18.5 ± .65	6.3769	17.2	.1572	.8398	4.1223		1.7996	.4443	2.73	.43	1.40
1200	180	19.4	6.6766	2.7	.1602	.8373	4.1100		1.7944	.4427	3.46	.43	1.40
1230	210	19.8	6.7932	4.0	.1627	.8366	4.1036		1.7916	.4418	3.62	.46	1.50
1255	235	20.6	6.8764	4.8	.1648	.8352	4.0997		1.7899	.4413	4.02	.46	1.51
1330	270	20.6	7.0762	5.5	.1655	.8305	4.0963		1.7884	.4408	4.58	.56	1.55
1400	300	20.8	7.1428	6.8	.1668	.8332	4.0899		1.7856	.4399	5.20	.36	1.60
1430	330	21.0	7.3094	7.1	.1671	.8329	4.0884		1.7844	.4397	5.56	.47	1.54
1500	360	21.5	7.3759	8.0	.1680	.8320	4.0840		1.7830	.4391	6.03	.48	1.54
1530	390	21.8	7.4758	8.8	.1688	.8312	4.0801		1.7813	.4386	6.51	.49	1.58
1600	420	22.3	7.6423	9.7	.1697	.8303	4.0756		1.7794	.4380	7.00	.49	1.58
1700	450	22.8 ± .68	7.8188	10.8	.1708	.8292	4.0702		1.7770	.4372	7.43	.43	1.38

## SAMPLE DATA

SPECIFIC GRAVITY 2.59  
 INITIAL HEIGHT OF SAMPLE 1.0000 IN.  
 FINAL HEIGHT OF SAMPLE .8292 IN.  
 CROSS-SECTIONAL AREA 4.9087 IN<sup>2</sup>  
 INITIAL MOISTURE CONTENT 42%  
 FINAL MOISTURE CONTENT 32.15%  
 WT. OF SOLIDS 97.003 GR.  
 VOL. OF SOLIDS 2.29 IN<sup>3</sup>

## COMPUTATIONS

$$K = \frac{QL}{AtH}$$

$$K = \frac{L(2.54)}{45(2.54)(A)(2.54)^2} \times \frac{Q}{t} = \frac{.007 QL}{t}$$

$$H = 45''$$

$$L = \text{HT of SAMPLE}$$



## APPENDIX C

RAW DATA

TEST NO. 3





TEST No. 3

TIME	$\Delta t$ (min)	LOAD PSI	LOAD TSF	DIAL	DIAL IN	HT.	VOL. V	$V_s$	$e \cdot \sqrt{V_s} - 1$	$m \cdot e / 10^6$	PERM. GRADE	$\Delta Q \cdot cc$	$K \cdot 10^{-1} sec 10^{-6}$
1000	0	0	0	0-0.0	0.00	1.0000	4.909	2.326	2.1010-1	.6240			
1010	10			1.1	.0011	.9989	4.904		2.0989	.5235			
1020	20			2.2	.0022	.9978	4.898		2.0943	.5229			
1030	30			3.1	.0031	.9969	4.894		2.0946	.5225			
1045	45			4.2	.0042	.9958	4.888		2.0920	.5219			
1100	60			4.6	.0046	.9954	4.886		2.0912	.5218			
1130	90			5.1	.0051	.9949	4.884		2.0903	.5215			
1200	120	.05	.0165	6.6	.0066	.9938	4.877		2.0873	.5209			
1230	150	.15	.0495	8.2	.0082	.9913	4.869		2.0834	.5198			
1300	180	.20	.0660	8.7	.0087	.9913	4.866		2.0826	.5196			
1345	225	.35	.1155	9.1	.0091	.9908	4.864		2.0817	.5195			
1400	240	.38	.1255	9.2	.0092	.9907	4.863		2.0813	.5195			
1430	270	.45	.1485	9.3	.0093	.9906	4.863		2.0813	.5195			
1500	300	.50	.1650	9.4	.0094	.9906	4.863		2.0813	.5195			
1330		.50 + .05	.1815	18.6	.0186	.9884	4.818		2.0621	.5057			
1330	0	.75 + .05	.2540	0-18.6	.0186	.9814	4.818	2.336	2.0621-1	.5150			
1345	15	.80 + .08	.2905	1-0.8	.0208	.9792	4.807		2.0573	.5139			
1400	30	.95	.3067	3.0	.0230	.9770	4.796		2.0526	.5128			
1415	45	.90	.3230	4.6	.0246	.9754	4.788		2.0492	.5120			
1430	60	.97	.3465	5.9	.0254	.9741	4.782		2.0466	.5113			
1505	95	1.05	.3768	8.2	.0282	.9718	4.771		2.0422	.5103			
1600	150	1.15	.406	9.7	.0297	.9703	4.763		2.0385	.5094			
1636	186	1.30 + .12	.417	11.6	.0316	.9684	4.754		2.0347	.5085			
1700	210	1.42	.508	13.7	.0337	.9663	4.744		2.0304	.5074			
1700	210	1.50	.534	15.1	.0351	.9649	4.737		2.0274	.5067			
1800	300	1.50	.534	16.3	.0363	.9637	4.731		2.0248	.5061			
2100	450	1.50	.534	16.9	.0369	.9631	4.728		2.0235	.5058			
2200	510	1.50	.534	17.0	.0370	.9630	4.727		2.0231	.5057			
6945	0	1.50 + .12	.534	1-19.6	.0396	.9604	4.715	2.336	2.0180-1	.5044			4.18
1000	15	1.50	.534	19.6	.0396	.9604	4.715		2.0180	.5044	1.90	0	4.18
1015	30	1.55	.551	19.7	.0397	.9603	4.714		2.0175	.5043	2.36	.65	4.18
1030	45	1.58 + .16	.561	2-0.0	.0400	.9600	4.713		2.0171	.5042	3.00	.45	4.18
1045	60	1.61	.584	0.2	.0402	.9598	4.711		2.0163	.5040	3.54	.54	4.18
1100	75	1.75	.630	0.7	.0407	.9593	4.709		2.0154	.5038	4.19	.65	4.18
1116	91	1.90	.680	1.3	.0413	.9587	4.706		2.0141	.5035	4.65	.46	4.18
1130	105	2.05	.729	1.3	.0423	.9577	4.701		2.0120	.5029	5.20	.55	4.18
1145	120	2.15	.753	2.3	.0434	.9566	4.696		2.0098	.5024	5.75	.55	4.18
1200	135	2.25	.795	3.4	.0449	.9551	4.689		2.0068	.5016	6.22	.47	4.18
1215	150	2.35	.828	4.9	.0463	.9537	4.682		2.0038	.5016	6.73	.51	4.18
1230	165	2.45	.861	6.3	.0476	.9524	4.675		2.0004	.5004	7.22	.49	4.18
1260	180	2.65 + .20	.940	7.6	.0483	.9507	4.662		2.0004	.5002	7.73	.51	4.18
1300	225	2.85	1.007	10.3	.0503	.9497	4.650		1.9953	.4988	8.72	.99	4.18
1330	255	3.00	1.057	12.8	.0528	.9472	4.639		1.9902	.4975	9.4	.94	4.18
1400	300	3.00	.057	14.8	.0546	.9451	4.638		1.9854	.4963	20.966	.90	4.18
1530	340	3.00	.057	15.3	.0563	.9447	4.638		1.9850	.4962	2.40	2.40	4.18
1630	500	3.00	.057	15.8	.0558	.9442	4.635		1.9837	.4958	5.87	2.97	4.18
1830	600	3.00	.057								7.67	1.00	4.18



## TEST No 3 (CONT)

2

TIME	$\Delta t$	LOAD-PSI	LOAD-TSF	DIAL	DIAL-IN.	HT.	V	$V_3$	$e = \sqrt{V_3 - 1}$	$m = e / \sqrt{1 - e}$	PERM. GAGE	$\Delta Q$	$K = 1/\sqrt{1 - e}$
1005	0	3.0 +2.0	1.057	2-19.1	.0591	.9409	4.619	2.336	1.9769 - 1	.4941	0.59	0	3.10
1020	15	3.1	1.089	19.2	.0592	.9408	4.618		1.9765	.4940	0.94	.40	2.92
1035	30	3.4	1.189	19.9	.0599	.9401	4.615		1.9752	.4937	1.43	.37	2.71
1050	45	3.65 +2.5	1.287	3-19.9	.0619	.9381	4.605		1.9709	.4926	1.81	.39	2.84
1105	60	3.9	1.370	4.2	.0642	.9358	4.594		1.9662	.4914	2.17	.36	2.69
1120	75	4.15	1.452	6.1	.0661	.9339	4.584		1.9619	.4902	2.52	.37	2.54
1135	90	4.35	1.578	8.1	.0681	.9319	4.575		1.9581	.4893	2.87	.35	2.44
1150	105	4.65	1.678	10.0	.0700	.9300	4.565		1.9538	.4881	3.25	.38	2.24
1205	120	4.8	1.680	11.5	.0715	.9285	4.558		1.9508	.4873	3.58	.35	2.28
1220	135	5.0	1.743	13.0	.0730	.9270	4.551		1.9478	.4866	3.93	.35	2.52
1235	150	5.15	1.793	14.6	.0746	.9254	4.543		1.9444	.4857	4.29	.36	2.59
1250	165	5.4	1.875	16.8	.0768	.9232	4.532		1.9396	.4844	4.69	.60	4.31
1305	180	5.6	1.940	18.0	.0780	.9220	4.526		1.9371	.4837	5.22	.33	2.27
1320	205	5.75	1.941	19.2	.0792	.9208	4.520		1.9345	.4830	5.60	.42	3.01
1335	220	5.90 +3.2	2.052	4-0.2	.0802	.9192	4.515		1.9324	.4825	5.96	.36	2.57
1350	229	6.0	2.085	0.8	.0808	.9181	4.507		1.9289	.4815	7.98	.98	2.93
1365	300	6.0	2.085	1.9	.0819	.9179	4.506		1.9286	.4814	8.56	.57	2.93
1380	325	6.0	2.085	2.0	.0821	.9178	4.505		1.9281	.4813	.76	.46	2.21
1395	345	6.0	2.085	2.2	.0822	.9177	4.505		1.9281	.4813	1.36	.60	2.14
1410	375	6.0	2.085	2.3	.0823	.9174	4.503		1.9272	.4811	2.38	.60	2.52
1425	420	6.0	2.085	2.6	.0826	.9174	4.503					1.02	
1710	0	6.0 +3.2	2.085	4-2.7	.0827	.9173	4.503	2.336	1.9272 - 1	.4811	2.14	0	2.31
1715	5	6.1	2.120	2.7	.0827	.9173	4.503		1.9272	.4811	2.23	.04	1.93
1735	25	6.4	2.218	3.4	.0834	.9168	4.500		1.9260	.4807	2.72	.44	2.34
1745	35	6.4	2.285	4.2	.0842	.9158	4.496		1.9247	.4803	2.94	.22	2.35
1800	50	7.0	2.385	5.8	.0858	.9142	4.488		1.9208	.4793	3.25	.31	2.38
1815	105	7.0 +3.6	2.492	10.7	.0901	.9093	4.464		1.9105	.4765	4.40	1.15	2.68
1830	125	8.0	2.760	12.0	.0920	.9080	4.457		1.9075	.4757	4.82	.42	2.25
1845	140	8.15	2.810	13.0	.0936	.9070	4.452		1.9054	.4751	5.20	.38	2.70
1855	155	8.30	2.855	14.0	.0940	.9060	4.447		1.9033	.4745	5.47	.27	1.90
1905	170	8.50	2.925	14.8	.0948	.9052	4.443		1.9016	.4741	5.79	.32	2.25
1920	185	8.65	2.972	15.6	.0956	.9044	4.440		1.9003	.4737	6.11	.32	2.35
1935	200	8.85	3.040	16.5	.0965	.9035	4.435		1.8981	.4731	6.43	.32	2.25
1950	215	9.05	3.105	17.4	.0974	.9026	4.431		1.8964	.4726	6.74	.31	2.18
2005	230	9.20	3.185	18.3	.0983	.9017	4.426		1.8943	.4721	7.07	.33	2.21
2020	255	9.45	3.238	19.5	.0995	.9005	4.420		1.8917	.4713	7.39	.52	2.14
2035	280	9.50	3.258	19.7	.0997	.9003	4.419		1.8913	.4712	7.69	.10	2.10
2050	275	9.65	3.315	5-0.4	.1004	.8996	4.416		1.8900	.4708	8.01	.32	2.24
2065	290	9.80	3.365	0.9	.1009	.8991	4.414		1.8891	.4706	8.32	.31	2.17
2080	305	9.95	3.415	1.5	.1015	.8985	4.411		1.8879	.4705	.90	.31	2.16
2095	320	10.10	3.465	2.1	.1021	.8979	4.408		1.8866	.4699	1.20	.30	2.08
2110	335	10.25	3.517	2.7	.1027	.8973	4.405		1.8860	.4694	1.41	.27	1.88
2125	350	10.35	3.548	3.3	.1033	.8967	4.402		1.8840	.4692	1.61	.28	1.95
2140	365	10.50	3.595	4.0	.1040	.8960	4.398		1.8823	.4687	1.75	.28	1.95
2155	380	10.65	3.648	4.7	.1047	.8953	4.395		1.8810	.4683	2.02	.28	1.95
2170	395	10.85	3.700	5.3	.1053	.8947	4.392		1.8797	.4680	2.30	.28	1.95
2185	410	11.00	3.765	5.3	.1060	.8940	4.388		1.8780	.4675	2.57	.27	1.88
2200	425	11.20	3.830	6.4	.1066	.8936	4.387		1.8776	.4674	2.85	.28	1.95
2215	440	11.40	3.893	7.3	.1073	.8932	4.382		1.8754	.4667	3.12	.27	1.87
2230	455	11.55	3.943	7.8	.1078	.8927	4.380		1.8746	.4665	3.40	.28	1.94
2245	470	11.55	3.943	8.4	.1084	.8916	4.377		1.8733	.4661	3.67	.27	1.87



TEST No. 3 (CONT)

3

TIME	$\Delta t$	LOAD - PSI	LOAD TSF	DIAL	DIAL - IN	HT.	V	$V_s$	$e = \frac{V_1}{V_2} - 1$	$m = \frac{e}{1+e}$	PERM. GAGE	$\Delta Q - cc$	$K' \frac{1}{sec} = 10^{-6}$
0850	0	18.55 $\pm .45$	3.960	5-10.8	.1108	.8892	4.365	2.336	1.8682 -1	.4647	0.48	0	1.87
0905	15	11.85	4.090	11.0	.1110	.8840	4.364		1.8677	.4646	.75	.27	1.86
0920	30	12.45	4.260	11.5	.1115	.8885	4.362		1.8669	.4644	1.01	.26	1.81
0935	45	12.90	4.405	12.4	.1124	.8876	4.357		1.8647	.4637	1.26	.25	1.73
0950	60	13.40	4.570	13.7	.1137	.8863	4.351		1.8622	.4631	1.50	.24	1.66
1005	75	13.85	4.735	15.3	.1153	.8847	4.343	$\pm .4280$ $V_s$	1.8588	.4626	1.75	.22	1.52
1022	92	14.3	4.870	16.9	.1169	.8831	4.335		1.8553	.4620	1.95	.23	1.40
1035	105	14.7	5.000	18.0	.1180	.8820	4.330		1.8532	.4613	2.16	.21	1.46
1050	120	15.1	5.130	19.2	.1192	.8808	4.324		1.8506	.4596	2.37	.21	1.41
1105	135	15.5 $\pm .48$	5.275	6-0.4	.1204	.8796	4.318		1.8481	.4589	2.59	.22	1.50
1120	150	15.9	5.405	1.5	.1215	.8785	4.312		1.8455	.4581	2.81	.22	1.59
1135	165	16.3	5.535	2.6	.1226	.8774	4.307		1.8433	.4574	3.03	.22	1.50
1150	180	16.6	5.635	3.5	.1235	.8763	4.303		1.8416	.4570	3.26	.23	1.56
1205	195	16.9	5.735	4.5	.1245	.8755	4.297		1.8391	.4563	3.49	.23	1.66
1215	205	17.2	5.835	5.2	.1252	.8748	4.294		1.8378	.4558	3.64	.15	1.33
1235	225	18.5	6.260	8.5	.1285	.8715	4.278		1.8310	.4538	4.25	.61	1.32
1305	290	19.3 $\pm .52$	6.545	10.5	.1305	.8695	4.268		1.8267	.4525	4.85	.60	1.55
1400	310	19.75	6.690	11.6	.1316	.8684	4.263		1.8245	.4519	5.12	.27	1.41
1416	326	20.1	6.800	12.4	.1324	.8676	4.259		1.8228	.4513	5.36	.24	1.32
1430	340	20.4	6.900	13.0	.1330	.8670	4.256		1.8215	.4510	5.56	.20	1.45
1500	370	21.1	7.150	14.6	.1346	.8654	4.248		1.8181	.4499	5.98	.42	1.42
1515	385	21.4	7.230	15.2	.1352	.8648	4.245		1.8168	.4495	6.19	.21	1.42
1530	400	21.8	7.340	16.0	.1360	.8646	4.241		1.8151	.4490	6.39	.20	1.35
1547	417	22.15	7.480	16.8	.1368	.8632	4.237		1.8134	.4485	6.64	.25	1.47
1609	450	22.4	7.560	17.4	.1374	.8626	4.234		1.8121	.4481	6.80	16	1.25
1615	445	22.8	7.700	18.2	.1382	.8618	4.230		1.8104	.4476	7.00	20	1.34
1630	460	23.15	7.85	18.9	.1389	.8611	4.227		1.8091	.4472	7.21	21	1.41
1645	475	23.5	7.925	19.6	.1396	.8604	4.223		1.8074	.4467	7.41	20	1.34
1700	490	23.85 $\pm .57$	8.025	7-0.4	.1404	.8596	4.219		1.8057	.4461	7.61	20	1.34
1950	660	23.90	8.080	2.3	.1423	.8577	4.210		1.8019	.4450	8.14	20	1.41
2005	675	23.90	8.080	2.3	.1423	.8577	4.210		1.8019	.4450	8.35	21	1.41

SAMPLE DATA

SPECIFIC GRAVITY	2.59
INITIAL HEIGHT OF SAMPLE	1.0000 IN
FINAL HEIGHT OF SAMPLE	.8577 IN
CROSS SECTIONAL AREA	4.9087 IN <sup>2</sup>
INITIAL MOISTURE CONTENT	40.5%
FINAL MOISTURE CONTENT	31.75%
WT. of SOLIDS	99.148 Gr.
VOL. of SOLIDS	2.336 IN <sup>3</sup>





## APPENDIX D

RAW DATA

TEST NO. 4







TEST No. 4 (Cont.)													2
TIME	$\Delta t$	PRESSURE	DIAL	H.T.	DIAL IN.	VOL. V	V <sub>s</sub>	e. V/V <sub>s</sub> -1	n = e/1/e	PERM. GAGE	$\Delta Q$ -cc	K-f/1/sec $\times 10^6$	
0730	0 sec	1.0	4-16.4	9036	0964	4-4362	2.3419	8942	4720	3.48		3.24	
	5		5-0.8	8992	1006	4-4146		8850	4694	3.35			
	10		5-1.8	8982	1018	4-4097		8829	4684	3.32			
	20		5-3.0	8970	1030	4-4038		8804	4674	3.30			
	30		5-4.2	8958	1042	4-3979		8766	4666	3.27			
	40		5-5.1	8949	1051	4-3929		8749	4662	3.26			
	50		5-5.6	8944	1056	4-3911		8737	4656	3.25			
	60		5-6.2	8938	1062	4-3881		8716	4656	3.23			
	1 1/2 MIN		5-7.2	8928	1072	4-3832		8688	4656	3.22			
	2		5-7.8	8922	1078	4-3847		8680	4644	3.23			
	3		5-8.5	8915	1085	4-3868		8676	4646	3.24			
	4		5-8.9	8911	1089	4-3799		8676	4645	3.25			
0830	5	5-9.1	8909	1091	4-3739		8665	4645	3.37			2.44	
	10	5-9.6	8904	1096	4-3714		8655	4639	3.64			2.80	
	20	5-10.1	8899	1101	4-3690		8649	4637	3.92			2.83	
	30	5-10.4	8896	1104	4-3675		8642	4635	4.33			2.83	
	45	5-10.7	8893	1107	4-3660		8638	4634	4.74			2.96	
	60	5-10.9	8891	1109	4-3650		8636	4634	5.17			2.96	
	75	5-11.0	8890	1110	4-3645		8634	4633	5.60			2.96	
	90	5-11.1	8889	1111	4-3641		8632	4632	6.03			2.96	
	120	5-11.2	8888	1112	4-3636		8630	4632	6.46			2.96	
	135	5-11.3	8887	1113	4-3631		8628	4630	6.84			2.96	
	150	5-11.4	8886	1114	4-3626		8625	4628	7.32			2.96	
	165	5-11.5	8885	1115	4-3621		8623	4627	8.19	1.55		3.01	
0930	180	5-11.6	8884	1116	4-3616		8621	4624	2.04	2.41		3.10	
	195	5-11.7	8883	1117	4-3611		8619	4624	2.41	4.1		2.83	
	210	5-11.8	8882	1118	4-3606		8614	4624	2.75	3.4		2.34	
	225	5-11.8	8882	1118	4-3606		8617	4624	3.16	3.16		2.83	
	240	5-11.9	8881	1119	4-3601		8617	4628	3.58	3.58		2.90	
	255	5-11.9	8881	1119	4-3601		8617	4628	4.00	4.00		2.90	
	270	5-11.9	8881	1119	4-3601		8617	4628	4.42	4.42		2.90	
	285	5-11.9	8881	1119	4-3601		8615	4627	5.27	5.27		2.93	
	315	5-12.0	8880	1120	4-3596		8615	4627	5.68	5.68		2.83	
	330	5-12.0	8880	1120	4-3596		8612	4627	7.42	7.42		2.83	
	1400	0	1.50	5-12.2	8878	1122	4-3587		8612	4627			2.83
		5		5-14.0	8860	1140	4-3448		8573	4615	7.40		
10		5-14.6		8854	1146	4-3464		8561	4612				
15		5-15.3		8847	1153	4-3434		8546	4608				
20		5-15.6		8844	1156	4-3420		8540	4606	7.31			
30		5-16.4		8836	1164	4-3380		8523	4601	7.28			
40		5-17.0		8830	1170	4-3351		8510	4597	7.27			
50		5-17.3		8827	1173	4-3336		8504	4595	7.25			
60		5-17.6		8824	1176	4-3321		8496	4594	7.26			
1 1/2		5-18.3		8817	1183	4-3287		8483	4589	7.27			
2		5-18.8		8812	1188	4-3263		8473	4584	7.27			
3		5-19.2		8808	1192	4-3243		8464	4584	7.28			
1500	4	5-19.5	8805	1195	4-3228		8458	4582	7.29			2.46	
	5	5-19.8	8802	1198	4-3213		8451	4580	7.30			2.66	
	10	6-0.3	8797	1203	4-3199		8445	4578	7.42			2.66	
	20	6-0.8	8792	1208	4-3164		8431	4574	7.48			2.66	
	30	6-1.1	8789	1211	4-3150		8425	4572	7.49			2.66	
	45	6-1.4	8786	1214	4-3135		8418	4570	8.33	1.55		2.66	
	60	6-1.6	8784	1216	4-3125		8414	4569	2.60	2.60		2.52	
	75	6-1.8	8782	1218	4-3115		8410	4568	2.97	2.97		2.52	
	90	6-1.9	8781	1219	4-3111		8408	4567				2.52	





TEST No. 4. (CONT.)

TIME	$\Delta t$	PRESSURE	DIAL	DIAL IN	HT.	VOL. = V	$V_s$	$e = \frac{V_s}{V_0} - 1$	$n = \frac{e}{1+e}$	PERM GAGE	AQ. CC	K. FT/SEC $10^{-6}$
1545	105		6-2.0	.1220	.8780	4.3106	2.3419	1.8404	.4566	3.36	.39	2.66
1615	120		2.1	.1221	.8779	4.3101		1.8401	.4566	4.13	.77	2.60
1630	135		2.2	.1222	.8778	4.3096		1.8401	.4566	4.52	.39	2.63
1645	150		2.3	.1223	.8777	4.3091		1.8399	.4566	4.91	.34	2.63
1700	165		2.4	.1224	.8776	4.3086		1.8397	.4566	5.30	.40	2.72
1715	180		2.4	.1224	.8776	4.3086		1.8397	.4566	5.71	.40	2.72
1730	195		2.6	.1226	.8774	4.3076		1.8393	.4563	2.45	1.87	2.55
1800	270		2.7	.1227	.8773	4.3071		1.8393	.4563	2.82	.38	2.59
1845	285		2.7	.1227	.8773	4.3071		1.8393	.4563	3.29	.39	2.66
1900	300		2.8	.1228	.8772	4.3066		1.8391	.4561	3.97	.37	2.57
1915	315		2.8	.1228	.8772	4.3066		1.8389	.4561	4.75	.78	2.66
1930	330		2.8	.1228	.8772	4.3066		1.8389	.4561			
2000	360		2.8	.1228	.8772	4.3066		1.8389	.4561			
0845	0	2.00	6-4.5	.1245	.8745	4.2934		1.8332	.4545	2.74		2.50
	5		5.8	.1258	.8742	4.2919		1.8326	.4543			
	10		6.3	.1263	.8737	4.2894		1.8315	.4539			
	15		6.5	.1265	.8735	4.2885		1.8311	.4538			
	20		6.8	.1268	.8734	4.2880		1.8309	.4538	2.68		
	30		7.2	.1272	.8728	4.2850		1.8296	.4534	2.67		
	40		7.6	.1276	.8724	4.2831		1.8288	.4531	2.67		
	50		7.8	.1278	.8722	4.2821		1.8284	.4530	2.67		
	60		7.9	.1279	.8721	4.2816		1.8282	.4529	2.67		
	1/12 MIN		8.3	.1283	.8717	4.2796		1.8273	.4527	2.67		
	2		8.6	.1286	.8714	4.2781		1.8267	.4525	2.67		
	3		9.0	.1290	.8710	4.2762		1.8261	.4523	2.68	.01	
	4		9.2	.1292	.8708	4.2752		1.8255	.4522	2.70	.02	
	5		9.4	.1294	.8706	4.2742		1.8250	.4520	2.72	.02	
0915	10		9.8	.1298	.8702	4.2723		1.8242	.4518	2.83	.23	2.33
	20		10.3	.1303	.8697	4.2698		1.8232	.4515	3.05	.23	2.33
	30		10.6	.1306	.8694	4.2683		1.8225	.4513	3.28	.35	2.32
	40		10.8	.1308	.8692	4.2673		1.8221	.4511	3.63	.47	2.38
	50		11.2	.1312	.8688	4.2654		1.8213	.4509	4.10	.24	2.43
1015	75		11.3	.1313	.8687	4.2651		1.8213	.4509	4.34	.34	2.43
	90		11.4	.1314	.8686	4.2644		1.8211	.4508	4.68	.34	2.43
1045	105		11.4	.1314	.8685	4.2644		1.8208	.4507	5.05	.37	2.50
	120		11.5	.1315	.8684	4.2639		1.8204	.4507	5.42	.37	2.50
	135		11.6	.1316	.8683	4.2634		1.8204	.4506	5.79	.37	2.50
1145	150		11.7	.1317	.8683	4.2629		1.8202	.4506	6.16	.37	2.50
	165		11.8	.1318	.8682	4.2624		1.8200	.4505	6.92	.76	2.56
	180		11.9	.1319	.8681	4.2620		1.8198	.4504	0.22	.32	2.62
	195		12.0	.1320	.8680	4.2615		1.8196	.4504	.54	.32	2.62
1245	210		12.0	.1320	.8680	4.2615		1.8196	.4504	.91	.37	2.62
	225		12.0	.1320	.8680	4.2615		1.8196	.4504	1.26	.35	2.66
	240		12.1	.1321	.8679	4.2610		1.8194	.4503	1.60	.34	2.66
1400	255		12.1	.1321	.8679	4.2610		1.8194	.4503	2.34	.79	2.66
	270		12.1	.1321	.8679	4.2610		1.8194	.4503	3.00	.61	2.66
1405	315		12.1	.1321	.8679	4.2610		1.8194	.4503			
1406	0	2.50	6-12.2	.1322	.8678	4.2605		.8192	.4503	3.12		
	5		13.4	.1334	.8666	4.2546		.8167	.4495			
	10		13.8	.1338	.8662	4.2534		.8158	.4492	3.08		
	15		14.1	.1341	.8659	4.2511		.8151	.4490			
	20		14.3	.1343	.8657	4.2502		.8148	.4489			
	30		14.8	.1352	.8652	4.2477		.8137	.4486	3.07		
	40		15.2	.1362	.8648	4.2457		.8129	.4483	3.06		
	50		15.4	.1364	.8646	4.2448		.8125	.4482	3.06		
	60		15.5	.1365	.8645	4.2445		.8124	.4482	3.06		
	1/12 MIN		16.0	.1366	.8646	4.2418		.8112	.4478	3.06		
1407	2		16.3	.1363	.8637	4.2403		.8102	.4476	3.06		



TEST No. 4 (CONT)

Time	$\Delta t$	Pressure	DIAL	DIAL-IN	HT	VOL	Vs	$e = \sqrt{V_s - 1}$	$h = e/e_{41}$	PERM-GAGE	$\Delta Q - cc$	$K \cdot f + 1/sec \times 10^{-6}$	4
			6-16.6	.1366	.8634	4.2389	2.3414	.8100	.4475	3.06	.02		
	3		16.8	.1368	.8632	4.2379		.8095	.4473	3.08			
	4		17.0	.1370	.8630	4.2364		.8091	.4472	3.10	.02		
	5		17.5	.1375	.8625	4.2345		.8081	.4469	3.14	.04	1.81	
	10		17.8	.1378	.8622	4.2330		.8074	.4467	3.28	.04	1.81	
	15		18.0	.1380	.8620	4.2320		.8070	.4465	3.39	.11	2.20	
	20		18.3	.1383	.8617	4.2305		.8064	.4464	3.61	.22	2.20	
	30		18.7	.1387	.8613	4.2286		.8065	.4461	3.95	.34	2.22	
	45		18.8	.1388	.8612	4.2281		.8063	.4460	4.29	.34	2.27	
1505	60		19.0	.1390	.8610	4.2271		.8049	.4459	4.63	.34	2.27	
	75		19.2	.1392	.8608	4.2261		.8045	.4458	4.98	.35	2.34	
	90		19.2	.1392	.8608	4.2261		.8045	.4458	5.42	.44	2.34	
	110		19.3	.1393	.8607	4.2256		.8043	.4457	5.66	.24	2.41	
1605	120		19.3	.1393	.8607	4.2256		.8043	.4457	6.00	.34	2.27	
	135		19.5	.1395	.8605	4.2246		.8039	.4456	6.59	.54	2.36	
	160		19.5	.1395	.8605	4.2246		.8039	.4456	7.13	.14	2.80	
	165		19.6	.1396	.8604	4.2241		.8036	.4455	7.43	.34	2.27	
1705	180		19.6	.1396	.8604	4.2241		.8036	.4455	7.43	.34	2.27	
	195		19.9	.1399	.8601	4.2237		.8030	.4453	8.09	.14	2.40	
	265		19.9	.1399	.8601	4.2237		.8030	.4453	8.43	.34	2.27	
1900	280		20.0	.1400	.8600	4.2227		.8028	.4453	9.10	.34	2.27	
	295		20.0	.1400	.8600	4.2222		.8028	.4453	9.44	.34	2.27	
	310		20.0	.1400	.8600	4.2222		.8028	.4453	9.78	.34	2.27	
	325		20.0	.1400	.8600	4.2222		.8028	.4453	10.12	.34	2.27	
	340		20.0	.1400	.8600	4.2222		.8028	.4453	10.46	.34	2.27	
2000	355		20.0	.1400	.8600	4.2222		.8028	.4453	10.80	.34	2.27	
0845	1125		7-2.4	.1424	.8676	4.2104		.7978	.4437	5.12	.34	2.27	
												2.19	
1415	0	3.00	7-2.8	.1428	.8572	1.7970		Vol	.4435	6.49			
	5		3.3	.1433	.8567	1.7959		4.2084	.4431	6.48			
	10		3.4	.1434	.8566	1.7957		4.2085	.4431				
	15		3.5	.1435	.8565	1.7955		4.2085	.4430				
	20		3.6	.1436	.8564	1.7953		4.2045	.4429	6.48			
	30		3.7	.1437	.8563	1.7951		4.2040	.4429	6.47			
	40		3.8	.1438	.8562	1.7949		4.2035	.4428	6.48			
	50		3.8	.1438	.8562	1.7949		4.2035	.4428	6.48			
	60		3.9	.1439	.8561	1.7947		4.2030	.4427	6.48			
	1 1/2 MIN		4.0	.1440	.8560	1.7944		4.2035	.4427	6.49			
	2		4.1	.1441	.8559	1.7942		4.2031	.4426	6.50			
	3		4.1	.1442	.8558	1.7940		4.2016	.4425	6.51			
	4		4.3	.1443	.8557	1.7938		4.2011	.4425	6.53			
	5		4.4	.1444	.8556	1.7936		4.2006	.4424	6.56			
	10		4.8	.1448	.8552	1.7928		4.1986	.4422	6.65	.10	1.49	
	15		5.0	.1450	.8550	1.7923		4.1976	.4420	6.75	.10	1.49	
	20		5.1	.1451	.8549	1.7921		4.1971	.4419	6.85	.10	1.49	
	30		5.3	.1453	.8547	1.7917		4.1962	.4418	7.07	.22	2.18	
	40		5.5	.1455	.8545	1.7915		4.1957	.4418	7.10	.33	2.18	
1510	45		5.7	.1457	.8543	1.7909		4.1947	.4416	7.73	.33	2.18	
	60		5.8	.1458	.8542	1.7907		4.1937	.4415	8.06	.33	2.18	
	75		6.1	.1461	.8539	1.7900		4.1922	.4413	8.49	.63	2.09	
	90		6.2	.1462	.8538	1.7898		4.1917	.4412	8.60	.30	1.48	
1745	120		6.2	.1462	.8538	1.7898		4.1917	.4412	2.31	.31	2.05	
	135		6.3	.1463	.8537	1.7896		4.1913	.4412	2.60	.29	2.01	
	150		6.3	.1463	.8537	1.7896		4.1913	.4412	2.82	.29	2.01	
	165		6.5	.1465	.8535	1.7897		4.1910	.4410	4.15	.23	2.04	
1845	225		6.5	.1465	.8535	1.7897		4.1910	.4410	5.14	.23	2.04	
	270		6.6	.1466	.8534	1.7890		4.1890	.4410		.23	2.10	



TEST NO 4													5
TIME	Δt	Pressure	DIAL	DIAL-IN	HT	VOL	Vs	e = Vs-1	n = e/1.0	PERM. (mD)	Δa - cc	K-Factor 10 <sup>-6</sup>	
1900 1915	285	3.56	7-6.7	.1467	.8533	4.1893	2.3419	.7888	.4404	5.45	.31	2.05	
	300		.1467	.8533	4.1893	2.3419	.7888	.4404	5.78	.33	2.14		
	315		.1467	.8533	4.1893	2.3419	.7888	.4404	6.07	.34	2.19		
	330		.1468	.8532	4.1888	2.3419	.7886	.4404	6.41	.34	2.25		
	345		.1468	.8532	4.1888	2.3419	.7886	.4404	6.74	.36	2.11		
2015	360		.1468	.8532	4.1888	2.3419	.7886	.4404	7.06	.36	2.11		
	375		.1468	.8532	4.1888	2.3419	.7886	.4404	7.39	.37	2.11		
	390		.1469	.8531	4.1883	2.3419	.7884	.4404	7.71	.37	2.11		
	405		.1469	.8531	4.1883	2.3419	.7884	.4404	8.03	.37	2.11		
	420		.1470	.8530	4.1878	2.3419	.7882	.4404	8.38	.37	2.32		
2115	435	.1470	.8530	4.1878	2.3419	.7882	.4404	8.76	.37	2.11			
2900			.1480	.8530	4.1878	2.3419	.7886	.4400			1.92		
0900	0 sec	3.50	7-8.0	.1480	.8529	4.1829		.7866	.4404	3.62			
	5	8.7	.1487	.8529	4.1829	4.1795		.7846	.4296				
	10	8.9	.1487	.8511	4.1851	4.1785		.7846	.4296				
	15	9.1	.1490	.8510	4.1850	4.1785		.7846	.4296				
	20	9.1	.1491	.8509	4.1850	4.1785		.7846	.4296				
	30	9.2	.1492	.8509	4.1850	4.1785		.7846	.4296				
	40	9.3	.1493	.8507	4.1850	4.1785		.7846	.4296				
	50	9.4	.1494	.8506	4.1850	4.1785		.7846	.4296				
	60	9.5	.1495	.8504	4.1850	4.1785		.7846	.4296				
	1 1/2 min	9.6	.1496	.8504	4.1850	4.1785		.7846	.4296				
1000	2	9.8	.1498	.8502	4.1850	4.1785		.7846	.4296				
	3	10.0	.1500	.8500	4.1850	4.1785		.7846	.4296				
	4	10.1	.1501	.8499	4.1850	4.1785		.7846	.4296				
	5	10.2	.1502	.8498	4.1850	4.1785		.7846	.4296				
	10	10.6	.1506	.8494	4.1850	4.1785		.7846	.4296				
	20	11.0	.1510	.8490	4.1850	4.1785		.7846	.4296				
	30	11.3	.1513	.8487	4.1850	4.1785		.7846	.4296				
	45	11.5	.1515	.8485	4.1850	4.1785		.7846	.4296				
	60	11.7	.1517	.8483	4.1850	4.1785		.7846	.4296				
	80	11.9	.1519	.8481	4.1850	4.1785		.7846	.4296				
1100	90	12.1	.1520	.8480	4.1850	4.1785		.7846	.4296				
	105	12.1	.1521	.8479	4.1850	4.1785		.7846	.4296				
	120	12.2	.1522	.8478	4.1850	4.1785		.7846	.4296				
	135	12.3	.1523	.8477	4.1850	4.1785		.7846	.4296				
	150	12.4	.1524	.8476	4.1850	4.1785		.7846	.4296				
1200	165	12.5	.1525	.8475	4.1850	4.1785		.7846	.4296				
	180	12.5	.1526	.8475	4.1850	4.1785		.7846	.4296				
	195	12.6	.1526	.8474	4.1850	4.1785		.7846	.4296				
	210	12.7	.1527	.8473	4.1850	4.1785		.7846	.4296				
	225	12.8	.1528	.8472	4.1850	4.1785		.7846	.4296				
1300	240	12.8	.1528	.8472	4.1850	4.1785		.7846	.4296				
	255	12.9	.1529	.8471	4.1850	4.1785		.7846	.4296				
	270	12.9	.1529	.8471	4.1850	4.1785		.7846	.4296				
	285	13.0	.1530	.8470	4.1850	4.1785		.7846	.4296				
	300	13.1	.1531	.8469	4.1850	4.1785		.7846	.4296				
1400	315	13.1	.1531	.8469	4.1850	4.1785		.7846	.4296				
	330	13.2	.1532	.8468	4.1850	4.1785		.7846	.4296				
	345	13.2	.1532	.8468	4.1850	4.1785		.7846	.4296				
1500	360	4.00											





TEST No 4

[illegible]







TEST No. 4												
TIME	Δt	PRESSURE	DIAL	DIAL IN	HT	VOL	Vs	C = $\frac{V_s}{V_b - 1}$	n = $\frac{C}{1+C}$	PERM. GAGE	ΔQ · CC	K · $\frac{1}{V_{SC}} \cdot 10^{-6}$
0930	0 sec	5.50	8-10.1	1701	8294	4.0734	23419	7355	4251	0.22		
	5		10.3	1703	8297	4.0729		7391	4241			
	10		10.3	1703	8297	4.0729		7391	4241			
	15		10.3	1703	8297	4.0729		7391	4241			
	20		10.3	1703	8297	4.0729		7391	4241			
	30		10.3	1703	8297	4.0729		7391	4241			
	40		10.4	1704	8297	4.0729		7391	4241			
	50		10.4	1704	8297	4.0729		7391	4241			
	60		10.4	1704	8297	4.0729		7391	4241			
	1 1/2 MIN		10.5	1705	8297	4.0729		7391	4241			
	2		10.6	1706	8297	4.0729		7391	4241			
	3		10.6	1706	8297	4.0729		7391	4241			
	4		10.7	1707	8297	4.0729		7391	4241			
	5		10.7	1707	8297	4.0729		7391	4241			
	10		10.8	1708	8297	4.0729		7391	4241			
	20		11.0	1710	8297	4.0729		7391	4241			
	30		11.1	1711	8297	4.0729		7391	4241			
	40		11.2	1712	8297	4.0729		7391	4241			
	60		11.3	1713	8297	4.0729		7391	4241			
1030	75		11.4	1714	8297	4.0729		7391	4241			
	90		11.5	1715	8297	4.0729		7391	4241			
	105		11.6	1716	8297	4.0729		7391	4241			
	120		11.6	1716	8297	4.0729		7391	4241			
1130	135		11.7	1717	8297	4.0729		7391	4241			
	150		11.7	1717	8297	4.0729		7391	4241			
	165		11.8	1718	8297	4.0729		7391	4241			
1230	180		11.8	1718	8297	4.0729		7391	4241			
133	195		11.9	1719	8297	4.0729		7391	4241			
	210		12.0	1720	8297	4.0729		7391	4241			
	225		12.1	1721	8297	4.0729		7391	4241			
	240		12.1	1721	8297	4.0729		7391	4241			
1415	255		12.2	1722	8297	4.0729		7391	4241			
1445	270		12.2	1722	8297	4.0729		7391	4241			
1515	285		12.3	1723	8297	4.0729		7391	4241			
1545	300		12.3	1723	8297	4.0729		7391	4241			
1630	315		12.3	1723	8297	4.0729		7391	4241			
	420		12.3	1723	8297	4.0729		7391	4241			
1420	0 sec	6.00	8-13.8	1778	8262	4.0558		7315	4224			
	5		14.1	1741	8259	4.0543		7311	4223			
	10		14.1	1741	8259	4.0543		7311	4223			
	15		14.2	1742	8258	4.0538		7304	4222			
	20		14.2	1742	8258	4.0538		7304	4222			
	30		14.2	1742	8258	4.0538		7304	4222			
	40		14.2	1742	8258	4.0538		7304	4222			
	50		14.2	1742	8258	4.0538		7304	4222			
	60		14.3	1743	8257	4.0528		7309	4221			
	1 1/2 MIN		14.3	1743	8257	4.0528		7309	4221			
	2		14.4	1744	8256	4.0523		7307	4221			
	3		14.4	1744	8256	4.0523		7307	4221			
	4		14.4	1744	8256	4.0523		7307	4221			
	5		14.5	1745	8255	4.0523		7305	4221			
	10		14.6	1746	8254	4.0518		7305	4221			
1450	20		14.8	1748	8252	4.0507		7303	4220			
	30		15.0	1750	8250	4.0499		7301	4219			
1520	45		15.1	1751	8249	4.0494		7292	4218			
	60		15.2	1752	8248	4.0489		7290	4216			
								7285	4215			





TEST No 4

TEST No 4												
TIME	$\Delta t$	Pressure	DIAL	DIAL-IN	HT	VOL	$V_s$	$e = \frac{V_s}{V_s - 1}$	$n = e / (e - 1)$	Perm. Gage	$\Delta Q - cc$	$K \cdot \frac{1}{\sqrt{sec}} \cdot 10^{-6}$
1135	75	6.50	8 - 15.3	1753	8247	4.0484	2.34119	.7286	.4214	3.08	.22	1.41
1150	90		15.4	1750	8247	4.0479		.7286	.4214	3.12	.22	1.41
1200	105		15.5	1751	8247	4.0474		.7287	.4213	3.15	.22	1.41
1210	120		15.6	1756	8244	4.0469		.7280	.4212	3.17	.22	1.41
1220	135		15.6	1756	8244	4.0469		.7280	.4212	3.17	.22	1.41
1230	150		15.7	1759	8243	4.0461		.7278	.4210	4.17	.22	1.41
1240	165		15.9	1759	8243	4.0455		.7274	.4209	4.17	.22	1.41
1250	180		16.0	1760	8245	4.0450		.7272	.4208	5.32	.22	1.41
1260	195		16.2	1762	8245	4.0440		.7267	.4206	5.32	.22	1.41
1270	210		16.3	1763	8237	4.0435		.7265	.4205	6.68	.22	1.41
1280	225	7.00	16.3	1763	8237	4.0435		.7265	.4205	6.68	.22	1.41
1290	240		16.3	1763	8237	4.0435		.7265	.4205	6.68	.22	1.41
1300	255		16.3	1763	8237	4.0435		.7265	.4205	6.68	.22	1.41
1310	270		16.3	1763	8237	4.0435		.7265	.4205	6.68	.22	1.41
1320	285		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1330	300		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1340	315		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1350	330		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1360	345		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1370	360		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1380	375	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1390	390		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1400	405		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1410	420		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1420	435		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1430	450		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1440	465		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1450	480		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1460	495		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1470	510		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1480	525	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1490	540		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1500	555		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1510	570		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1520	585		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1530	600		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1540	615		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1550	630		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1560	645		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1570	660		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1580	675	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1590	690		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1600	705		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1610	720		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1620	735		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1630	750		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1640	765		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1650	780		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1660	795		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1670	810		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1680	825	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1690	840		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1700	855		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1710	870		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1720	885		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1730	900		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1740	915		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1750	930		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1760	945		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1770	960		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1780	975	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1790	990		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1800	1005		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1810	1020		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1820	1035		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1830	1050		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1840	1065		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1850	1080		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1860	1095		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1870	1110		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1880	1125	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1890	1140		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1900	1155		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1910	1170		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1920	1185		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1930	1200		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1940	1215		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1950	1230		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1960	1245		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1970	1260		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1980	1275	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
1990	1290		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2000	1305		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2010	1320		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2020	1335		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2030	1350		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2040	1365		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2050	1380		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2060	1395		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2070	1410		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2080	1425	7.00	16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2090	1440		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2100	1455		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2110	1470		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2120	1485		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2130	1500		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2140	1515		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2150	1530		16.4	1764	8236	4.0435		.7265	.4205	6.68	.22	1.41
2160	1545		16.4	1764	8236	4.						



TEST No										10			
TIME	DT	PRESSURE	DIAL	DIAL IN	HT	VOL	V <sub>s</sub>	C <sub>s</sub> V <sub>s</sub> -1	M <sub>r</sub> C <sub>s</sub> /V <sub>s</sub>	PERM GAGE	ΔQ - cc	K' / (sec/v) <sup>1/2</sup>	
0900	0 sec	9-07	.1807	7.00	.8173	4.0219	2.3419	.7175	.417	0.79			
	5	176	.1876		.8024	3.9364		.6819	405.4				
	10	28	.2028		.7972	3.9134		.6710	412				
	20	70	.2070		.7930	3.8428		.6577	3482				
	30	120	.2120		.7800	3.8482		.6577	371				
	40	135	.2135		.7865	3.8669		.6486	3434				
	50	141	.2141		.7859	3.8574		.6470	3728				
	60	145	.2145		.7855	3.8560		.6465	3426				
	1/2 MIN	158	.2158		.7842	3.8496		.6432	3315				
	2	159	.2159		.7841	3.8491		.6435	3412				
1000	3	160	.2160		.7840	3.8486		.6433	3410				
	4	163	.2163		.7837	3.8468		.6425	3410				
	5	164	.2166		.7834	3.8457		.6421	3410				
	10	171	.2171		.7827	3.8432		.6400	3410				
	20	176	.2176		.7824	3.8408		.6393	3410				
	30	179	.2179		.7821	3.8393		.6387	3410				
	40	182	.2182		.7818	3.8378		.6381	3410				
	50	183	.2183		.7817	3.8373		.6383	3410				
	60	184	.2184		.7816	3.8368		.6378	3410				
	70	186	.2186		.7814	3.8354		.6377	3410				
1100	105	187	.2187		.7813	3.8349		.6375	3410				
	120	188	.2188		.7812	3.8344		.6372	3410				
	155	189	.2189		.7811	3.8344		.6370	3410				
	190	190	.2190		.7810	3.8339		.6368	3410				
	195	191	.2191		.7809	3.8334		.6366	3410				
	210	192	.2192		.7808	3.8329		.6366	3410				
	225	192	.2192		.7808	3.8324		.6366	3410				
	240	192	.2193		.7807	3.8324		.6366	3410				
	255	193	.2193		.7807	3.8324		.6366	3410				
	270	193	.2193		.7807	3.8324		.6366	3410				
1300	285	194	.2194		.7806	3.8319		.6366	3410				
	300	194	.2194		.7806	3.8319		.6366	3410				
	315	195	.2195		.7805	3.8314		.6366	3410				
	330	195	.2195		.7805	3.8314		.6366	3410				
	345	195	.2195		.7805	3.8314		.6366	3410				
	360	195	.2195		.7805	3.8314		.6366	3410				
	1500												



TEST N H11SAMPLE DATA

SPECIFIC GRAVITY	2.59
INITIAL HEIGHT of SAMPLE	1.000 IN.
FINAL HEIGHT of SAMPLE	.7805 IN.
CROSS SECTIONAL AREA	4.9087 IN <sup>2</sup>
INITIAL VOLUME CONTENT	41%
FINAL MOISTURE CONTENT	29%
WEIGHT of SOLIDS	97.4 grams
VOLUME of SOLIDS	2.3419 IN <sup>3</sup>















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An investigation of the consolidation of



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